

Physics Program of the experiments at Large Hadron Collider

Lecture 5

**Physics with
W and Z bosons:
part I**



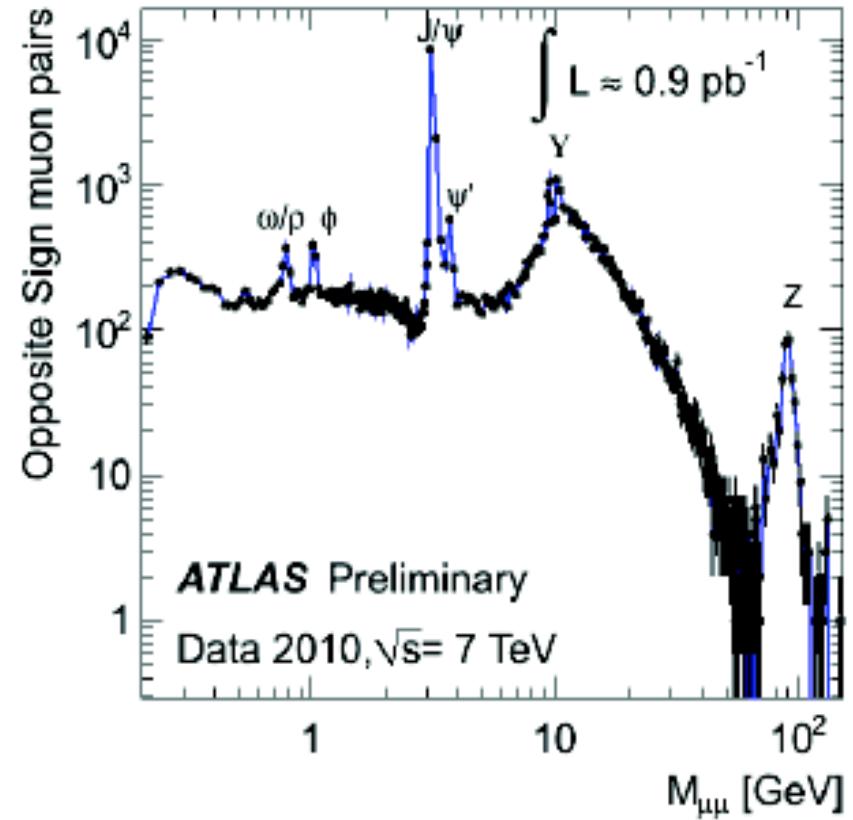
Latest news!!!



- 150ns period ended Friday last week,
 - 48.9 pb⁻¹ delivered (total)
 - 19 pb⁻¹ delivered last week
 - Max peak luminosity 2.1×10^{32}
- Friday (last week) started commissioning period of 50ns
- Tonight: planned last stable pp beam 2010
- Heavy-ion run starts on Thursday (this week)
- Technical stop (winter) :
 - 11 weeks, starting Xmass break

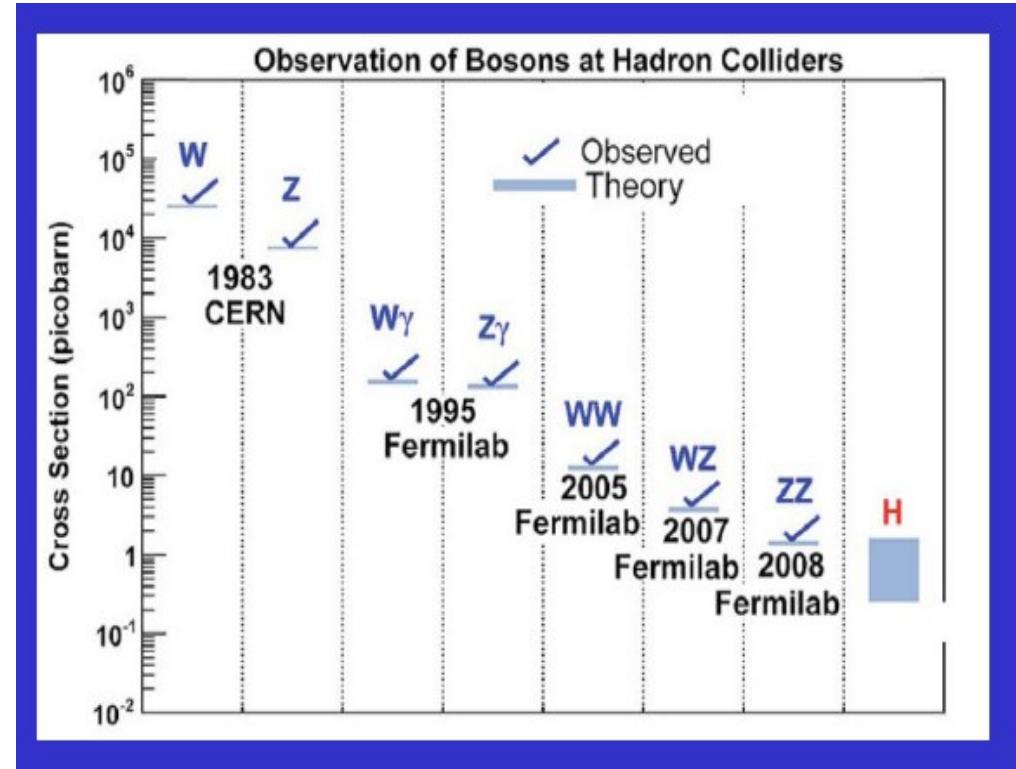
Retracing history of particle physics

- With up to 1pb^{-1} (public results) we made it up to 80's
- Results at summer conferences 2010
- Onia(J/Psi, Psi, Y,...)
+ first hundreds of W,Z in the leptonic channels



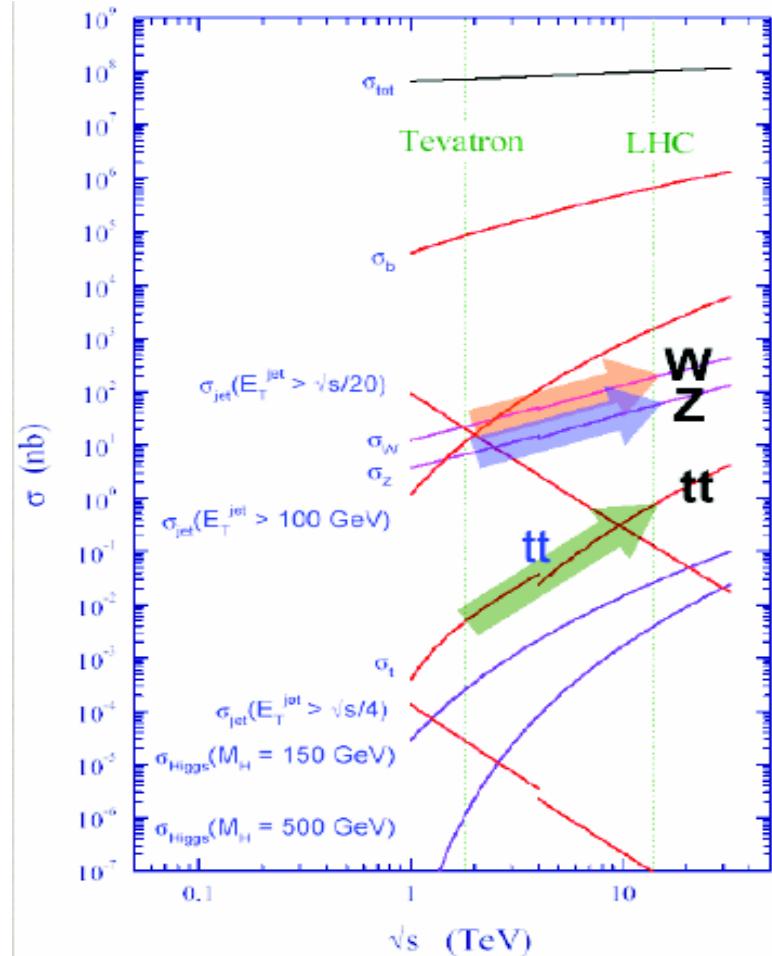
Bosons at hadron colliders

- So far the primary measurement channel is through leptonic decays
 - $\text{BR}(W \rightarrow e \nu) \sim 10\%$
 - $\text{BR}(Z \rightarrow ee) \sim 3\%$
- It means that we are probing $\sigma \times \text{BR}$ values orders of magnitude smaller
- At LHC cross-section 5-10 x higher than at Tevatron at Fermilab.



Bosons at LHC

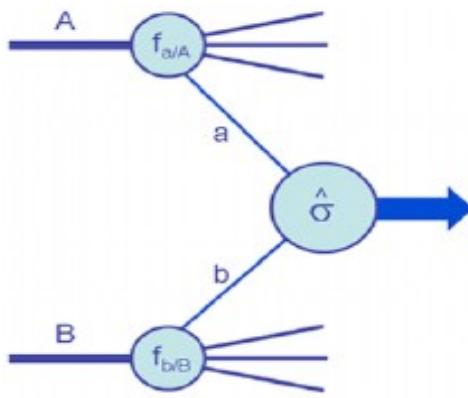
- Well measured by previous experiments
 - Inclusive cross sections, $R(W^+/W^-)$, $R(W/Z)$
 - Differential distributions, associated jet multiplicity, A_{FB} , etc.
- Yet still educational at the LHC
 - Cross sections at $\sqrt{s} = 7\text{TeV}$
 - New pdf constraints possible
- “Standard candles” for high- p_T analyses
 - Calibration, alignment
 - Independent luminosity measurements



Just departure point for high- p_T
Beyond Standard Model analyses

Drell-Yan cross-section

■ Keywords:



- factorisation μ_F and renormalisation μ_R scales
- universal parton distribution functions
- LO, NLO, NNLO matrix elements and DGLAP kernels

also depends on μ_R and μ_F , so as to cancel scale dependence in PDF's and α_s , to this order

$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a, Q^2) f_{b/B}(x_b, Q^2) \hat{\sigma}_{ab \rightarrow X}$$

$$\sigma_{AB} = \int dx_a dx_b f_{a/A}(x_a, \mu_F^2) f_{b/B}(x_b, \mu_F^2) \times [\hat{\sigma}_0 + \alpha_S(\mu_R^2) \hat{\sigma}_1 + \dots]_{ab \rightarrow X}.$$

- All orders cross section has no dependence on μ_F and μ_R ; a residual dependence remains (to order α_s^{n+1}) for a finite order (α_s^n) calculations.

DGLAP equations

- Parton distributions used in hard scattering calculations are solutions of DGLAP equations

$$\frac{\partial q_i(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dz}{z} \left\{ P_{q_i q_j}(z, \alpha_S) q_j\left(\frac{x}{z}, \mu^2\right) + P_{q_i g}(z, \alpha_S) g\left(\frac{x}{z}, \mu^2\right) \right\},$$
$$\frac{\partial g(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dz}{z} \left\{ P_{g q_j}(z, \alpha_S) q_j\left(\frac{x}{z}, \mu^2\right) + P_{gg}(z, \alpha_S) g\left(\frac{x}{z}, \mu^2\right) \right\},$$

- Splitting functions have perturbative expansions

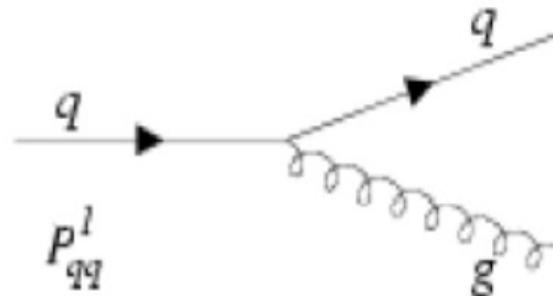
$$P_{ab}(x, \alpha_S) = P_{ab}^{(0)}(x) + \frac{\alpha_S}{2\pi} P_{ab}^{(1)}(x) + \dots$$

Thus, a full NLO calculation will contain both $\hat{\sigma}_1$ (previous slide) and $P_{ab}^{(1)}$

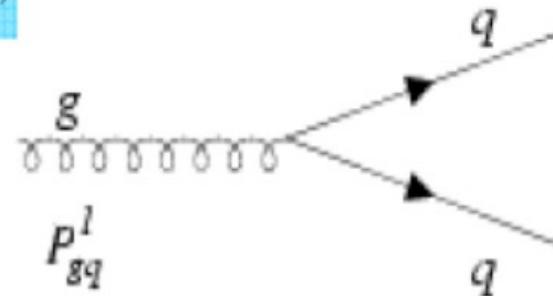
Altarelli-Parisi splitting functions

Altarelli-Parisi splitting functions:

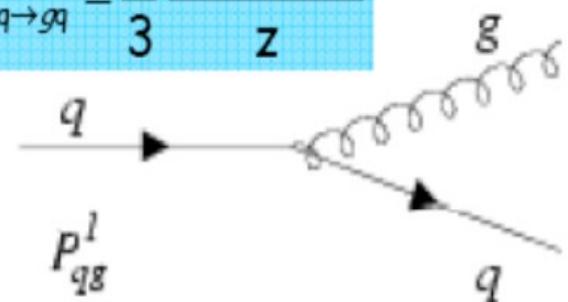
$$P_{q \rightarrow qg} = \frac{4}{3} \left(\frac{1+z^2}{1-z} \right)$$



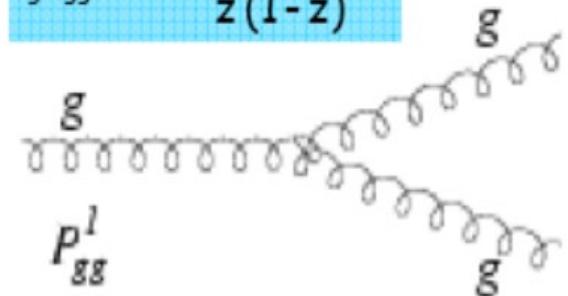
$$P_{g \rightarrow qq} = \frac{n_f^2}{2} (z^2 + (1-z)^2)$$



$$P_{q \rightarrow gq} = \frac{4}{3} \frac{1+(1-z)^2}{z}$$



$$P_{g \rightarrow gg} = 3 \frac{(1-z)(1-z)^2}{z(1-z)}$$



Kinematics

- Double differential cross section for production of Drell-Yan pair of mass M and at rapidity y is given by

$$\frac{d\sigma}{dM^2 dy} = \frac{\hat{\sigma}_0}{Ns} \left[\sum_k Q_k^2 (q_k(x_1, M^2) \bar{q}_k(x_2, M^2) + [1 \leftrightarrow 2]) \right]$$

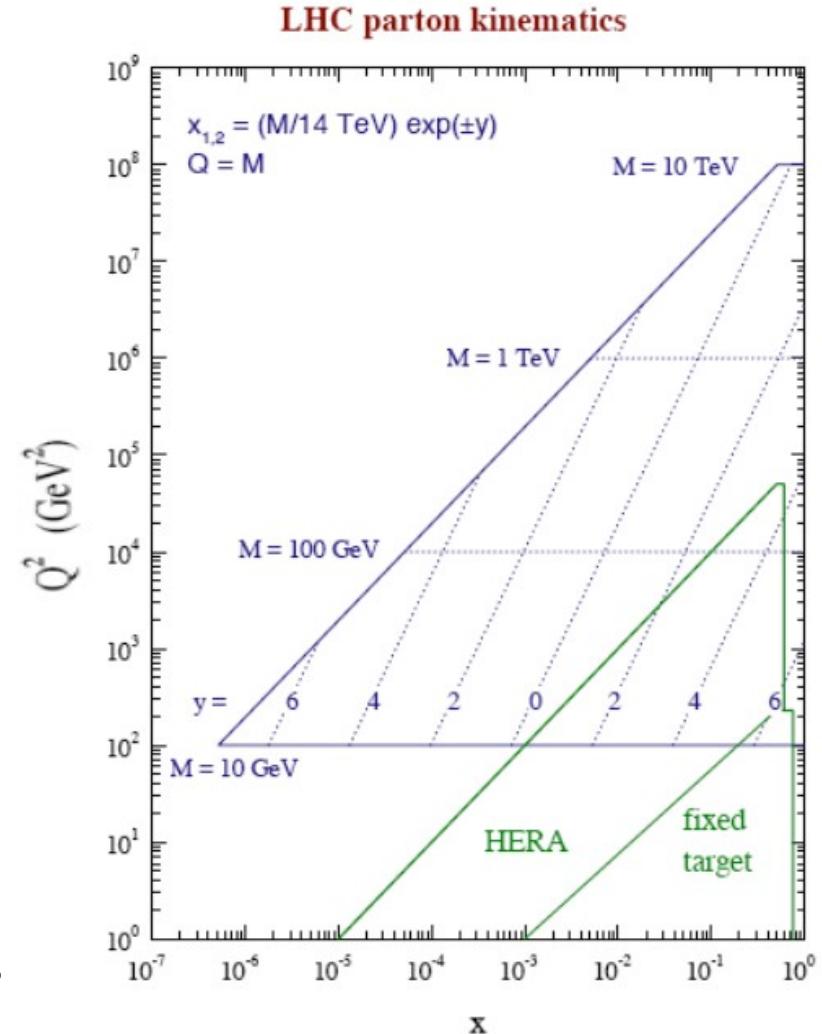
◆ where

$$\hat{\sigma}_0 = \frac{4\pi\alpha^2}{3M^2}$$

◆ and

$$x_1 = \frac{M}{\sqrt{s}} e^y, \quad x_2 = \frac{M}{\sqrt{s}} e^{-y}.$$

- Different values of M and y probes different values of x and Q^2



W/Z production

- Cross sections for on-shell W and Z production (in narrow width limit) given by

$$\hat{\sigma}^{q\bar{q}' \rightarrow W} = \frac{\pi}{3} \sqrt{2} G_F M_W^2 |V_{qq'}|^2 \delta(\hat{s} - M_W^2),$$

$$\hat{\sigma}^{q\bar{q} \rightarrow Z} = \frac{\pi}{3} \sqrt{2} G_F M_Z^2 (v_q^2 + a_q^2) \delta(\hat{s} - M_Z^2),$$

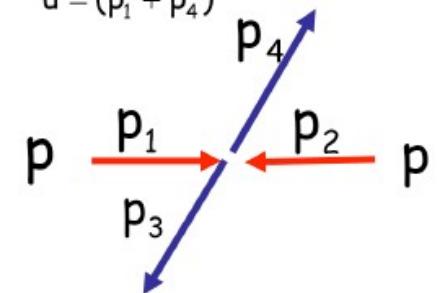
- Where $V_{qq'}$ is appropriate CKM matrix element and v_q and a_q are the vector and axial couplings of the Z to quarks
- At LO there is no α_s dependence; EW vertex only
- NLO contribution to the cross section is proportional to α_s ; NNLO to α_s^2 ; ...

Mandelstamm variables :

$$\hat{s} = (p_1 + p_1')^2$$

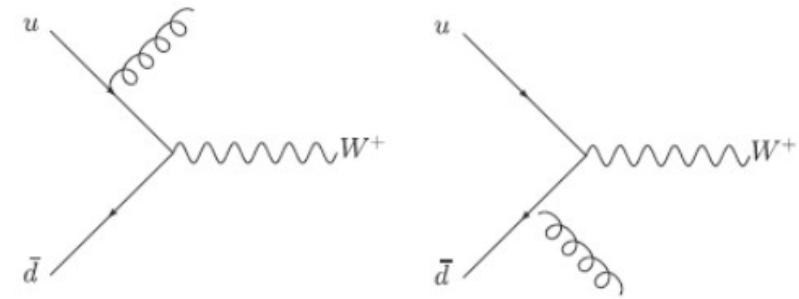
$$\hat{t} = (p_1 + p_3)^2$$

$$\hat{u} = (p_1 + p_4)^2$$



W/Z p_T distributions

- Most of W/Z produced at low p_T but can be produced at non-zero p_T due to the diagrams with emitted gluon



$$\sum |\mathcal{M}^{q\bar{q}' \rightarrow Wg}|^2 = \pi \alpha_S \sqrt{2} G_F M_W^2 |V_{qq'}|^2 \frac{8}{9} \frac{\hat{t}^2 + \hat{u}^2 + 2M_W^2 \hat{s}}{\hat{t}\hat{u}},$$

$$\sum |\mathcal{M}^{gq \rightarrow Wq'}|^2 = \pi \alpha_S \sqrt{2} G_F M_W^2 |V_{qq'}|^2 \frac{1}{3} \frac{\hat{s}^2 + \hat{u}^2 + 2\hat{t}M_W^2}{-\hat{s}\hat{u}},$$

- Sum over colors and spins in initial states and average over same in final states
- Transverse momentum distribution obtained by convoluting these matrix elements with pdf's in usual way

W/Z p_T distributions

- Back to 2->2 subprocess, where Q2 is virtuality of the W

$$|\mathcal{M}^{u\bar{d} \rightarrow W^+ g}|^2 \sim \left(\frac{\hat{t}^2 + \hat{u}^2 + 2Q^2\hat{s}}{\hat{t}\hat{u}} \right)$$

- Convolute with pdf's

$$\sigma = \int dx_1 dx_2 f_u(x_1, Q^2) f_{\bar{d}}(x_2, Q^2) \frac{|\mathcal{M}|^2}{32\pi^2\hat{s}} \frac{d^3 p_W}{E_W} \frac{d^3 p_g}{E_g} \delta(p_u + p_{\bar{d}} - p_g - p_W)$$

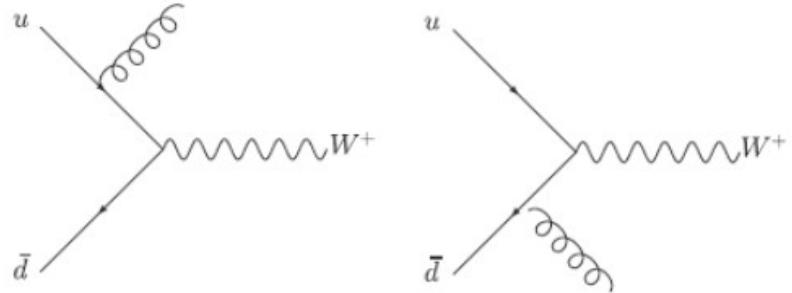
- Transform into differential cross-section

$$\frac{d\sigma}{dQ^2 dy dp_T^2} \sim \frac{1}{s} \int dy_g f_u(x_1, Q^2) f_{\bar{d}}(x_2, Q^2) \frac{|\mathcal{M}|^2}{\hat{s}}$$

W/Z p_T distributions

- In the limit of leading divergence we can write

$$\frac{d\sigma}{dQ^2 dy dp_T^2} \sim \frac{2}{s} \frac{1}{p_T^2} \int dy_g f_u(x_1, Q^2) f_{\bar{d}}(x_2, Q^2) + (\text{sub-leading in } p_T^2)$$



- As p_T of W becomes small, limits on y_g integration are given by $\pm \log(s^{1/2}/p_T)$
- The results is then

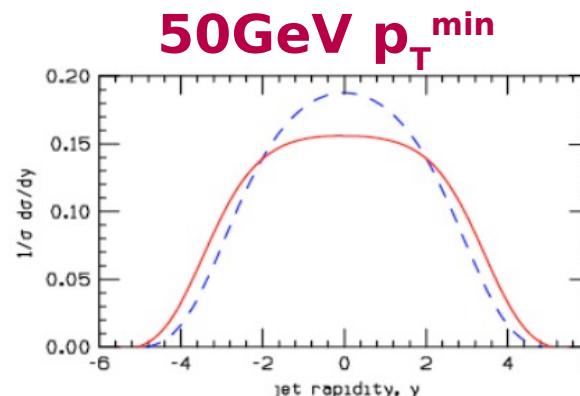
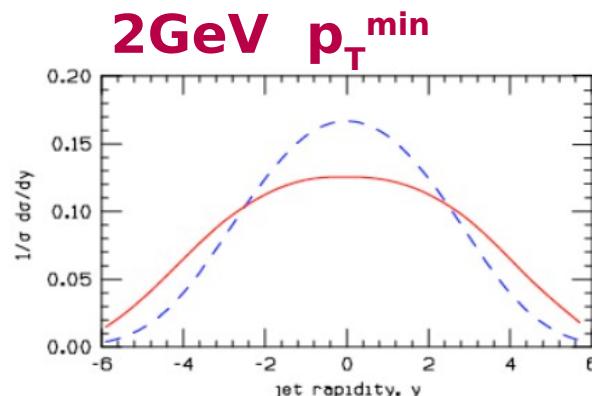
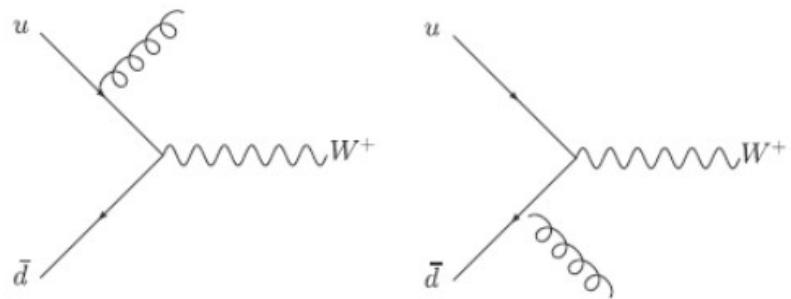
$$\frac{d\sigma}{dQ^2 dy dp_T^2} \sim \frac{\log(s/p_T^2)}{p_T^2}$$

- It diverges unless we apply a p_T^{\min} cut; final distribution depends on α_s times log

W/Z rapidity distributions

- Rapidity distribution for 2 different choices of p_T^{\min}
- Final state parton is not in the forward region, but central due to the requirement on p_T^{\min}

the p_T requirement of the gluon serves as the cutoff

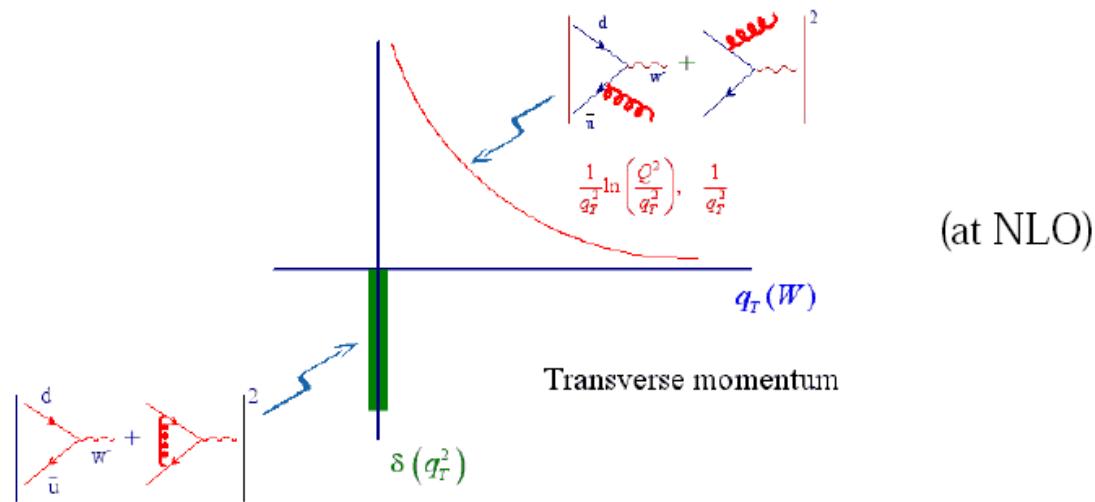


**Blue: $q\bar{q}$ process
Red: $q\bar{q}$ bar process**

Figure 9. The rapidity distribution of the final-state parton found in a lowest-order calculation of the $W + 1$ jet cross section at the LHC. The parton is required to have a p_T larger than 2 GeV (left) or 50 GeV (right). Contributions from $q\bar{q}$ annihilation (solid red line) and the qg process (dashed blue line) are shown separately.

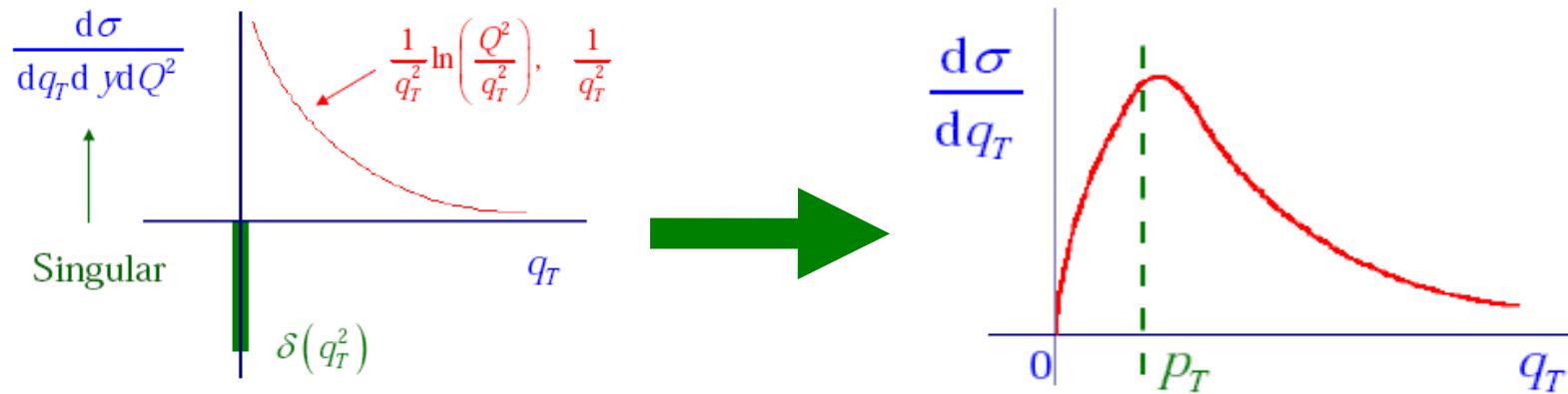
Shortcomings of fixed order calculations

- Divergent, without cut on p_T^{\min} , cannot describe the data

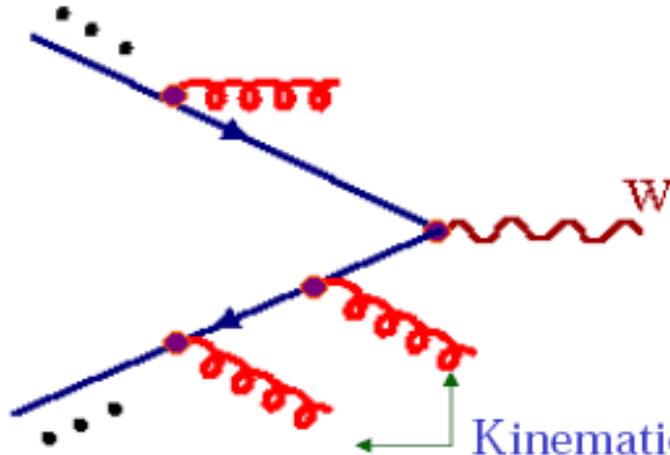


QCD resummation

- Resummation: reorganise calculations in terms of large Logs $L(Q^2/p_T^2)$; regularised at low p_T range;
- Different schemes: CSS which includes also non-perturbative effects; Sudakov form factors; exponentiation;



Monte Carlo approach example: Parton Shower



Backward Radiation
(Initial State Radiation)

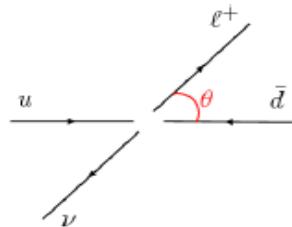
Kinematics of the radiated gluon, controlled by Sudakov form factor with some arbitrary cut-off.
(In contrast to perform integration in impact parameter space, i.e., **b** space.)

The shape of $q_T(w)$ is generated. But, the integrated rate remains the same as at Born level (finite virtual correction is not included).

Recently, there are efforts to include part of higher order effect in the event generator.

Transverse momenta of charged lepton

- In (ud) c.m. system,

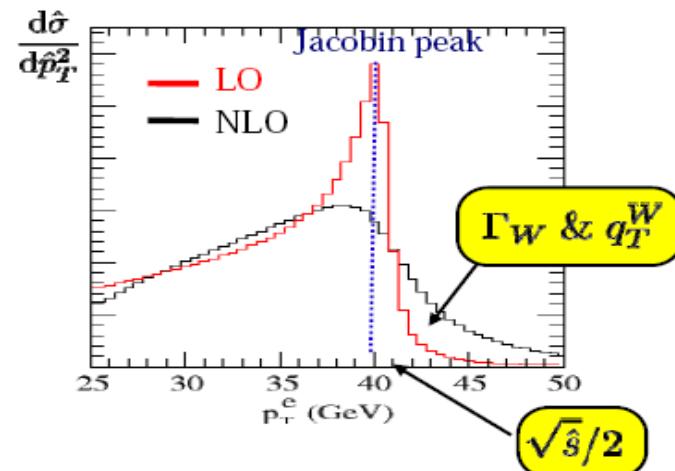


$$\hat{p}_T^2 = \frac{1}{4} \hat{s} \sin^2 \theta$$

Jacobian factor

$$\frac{d \cos \theta}{d \hat{p}_T^2} = -\frac{2}{\hat{s}} \frac{1}{\sqrt{1 - \frac{4 \hat{p}_T^2}{\hat{s}}}}$$

$$\Rightarrow \frac{d\hat{\sigma}}{d\hat{p}_T^2} \sim \frac{d\hat{\sigma}}{d \cos \theta} \times \frac{1}{\sqrt{1 - 4\hat{p}_T^2/\hat{s}}}$$

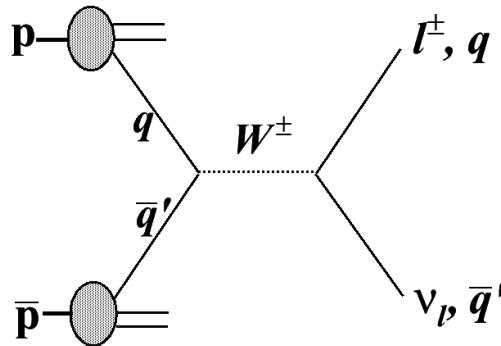


sensitive region for measuring

M_W : $p_T^e \sim 30 - 45$ GeV

Γ_W : not a good observable

Cross-section at LHC (7TeV)



$$\sigma_{W^+ \rightarrow \ell\nu}^{NNLO} = 6.15 \text{ nb}$$

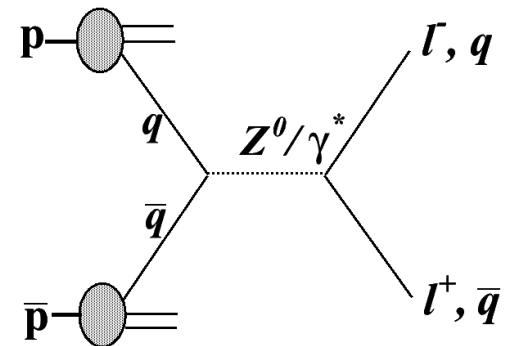
$$\sigma_{W^- \rightarrow \ell\nu}^{NNLO} = 4.3 \text{ nb}$$

$$\sigma(W^+) \neq \sigma(W^-)$$

W^+ production: $u\bar{d} + c\bar{s}$

W^- production: $d\bar{u} + s\bar{c}$

Z production: $u\bar{u} + d\bar{d} + s\bar{s} + c\bar{c} + b\bar{b}$

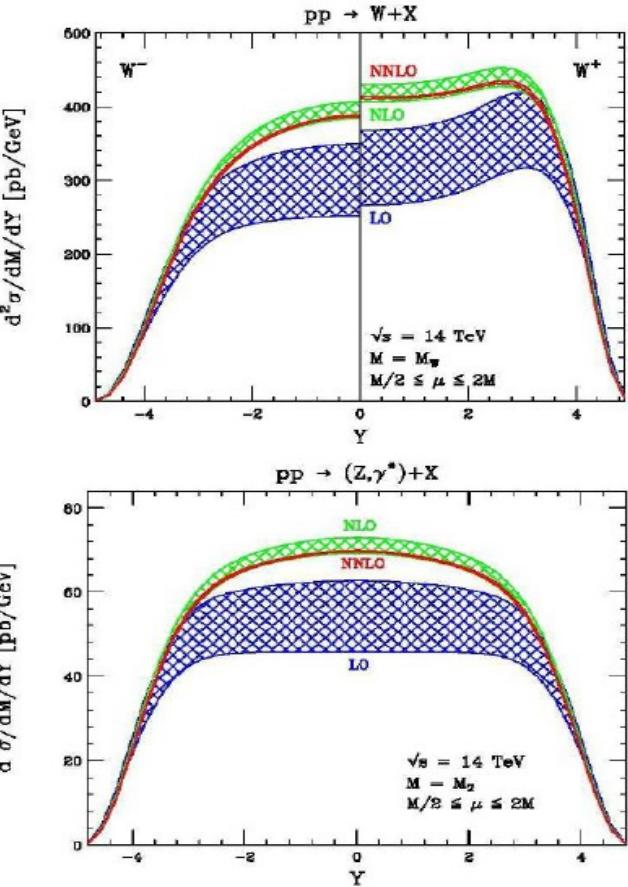


$$\sigma_{Z/\gamma^* \rightarrow \ell\ell}^{NNLO} = 0.989 \text{ nb}$$

- Test QCD (up to NNLO) in production
 - Hard and soft gluon emission
- Sensitive to parton distribution functions
- Extract electroweak parameters
 - $\sin\Theta_W$, m_W , quark-boson couplings

Monte Carlo simulations

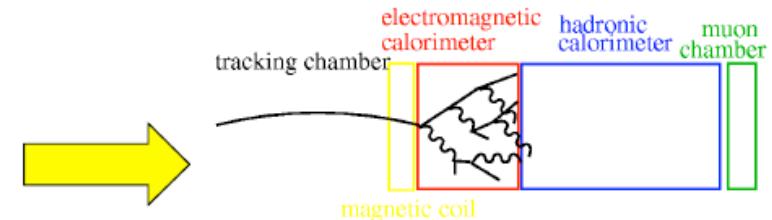
- Base-line generators:
 - Pythia, Herwig (LO),
 - MCatNLO (NLO)
 - POWHEG (NLO)
- Used as components of for cross-checks
 - FEWZ: complete NLO, NNLL
 - ResBos: NNLL resummation
 - Horace: full 1-loop electroweak
 - PHOTOS: final state QED (exponentiated)



Lepton identification

■ Electron:

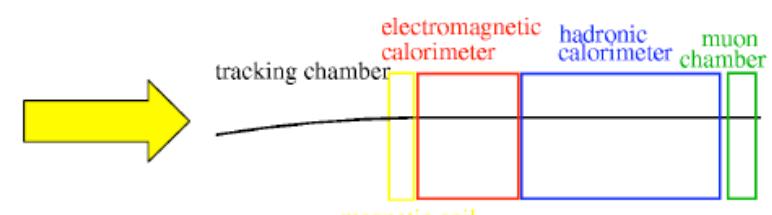
- Compact electromagnetic cluster in calorimeter



- Matched to track

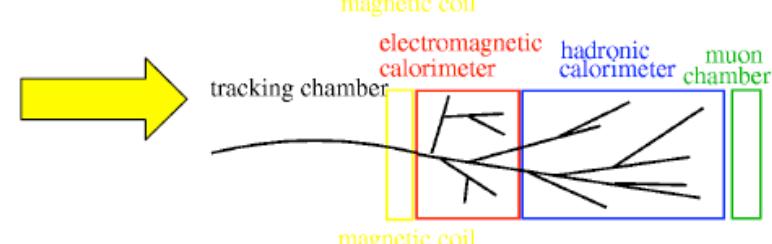
■ Muons:

- Track in the muon chambers
- Matched to track



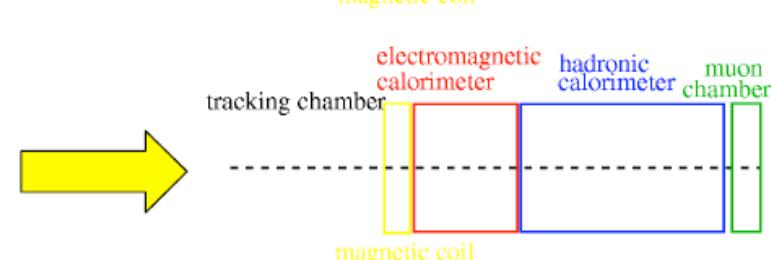
■ Taus:

- Narrow jet
- Matched to one or three tracks



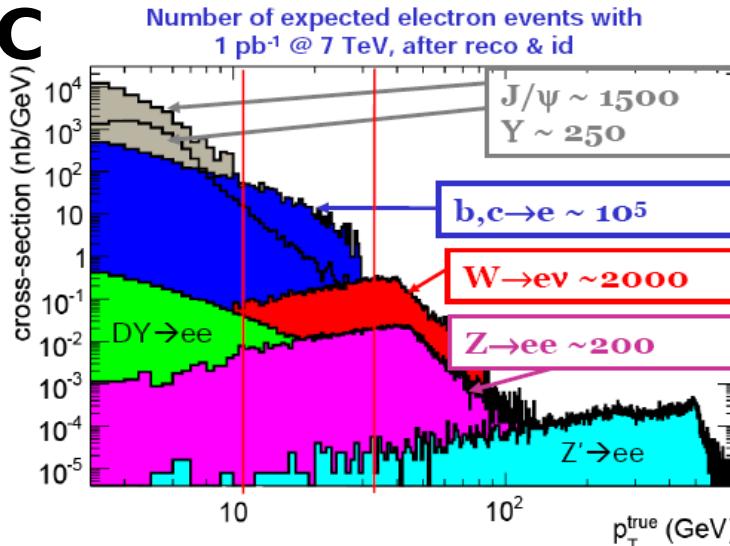
■ Neutrinos

- Imbalance in transverse momentum
- Inferred from total transverse energy in detector



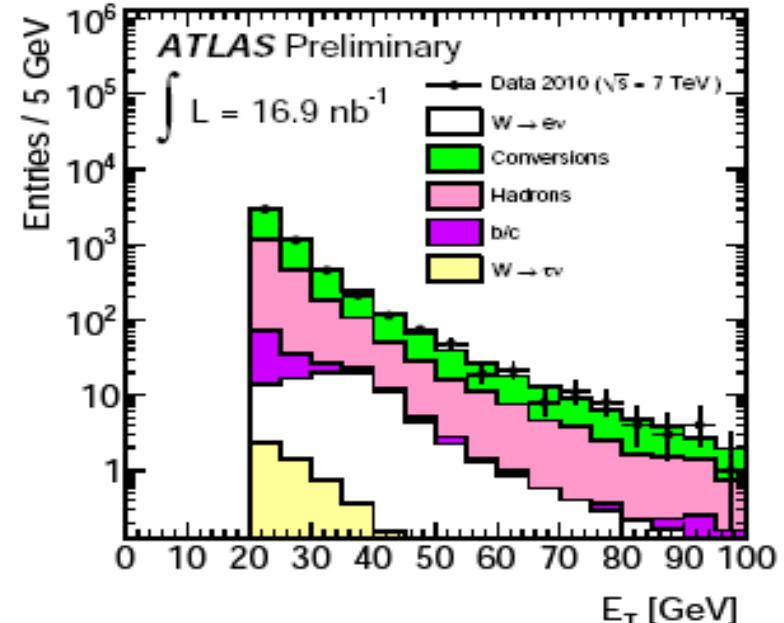
Electrons and jets

MC



- There is also lot of true electrons from semileptonic decays inside jets

DATA: loose electron ID

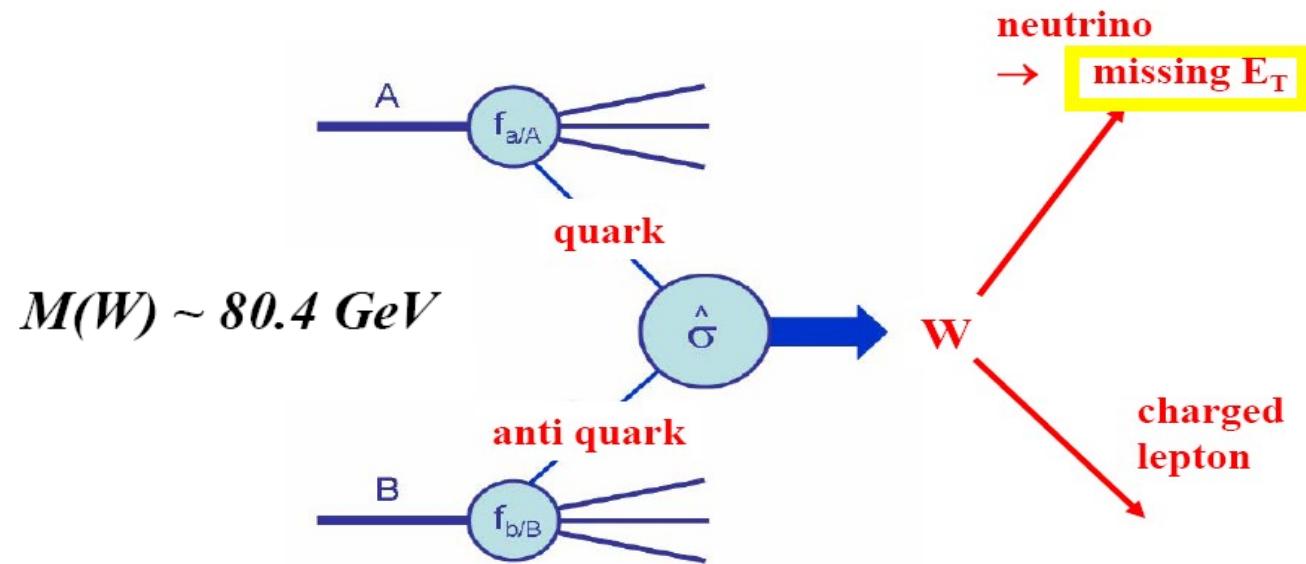


- Jets can look like electrons
 - Photon conversion from π^0 's
 - Early showering charged pions
- And there is lot of jets
- Difficult to model in Monte Carlo
 - Detailed simulation in tracking and calorimeter volume

Measurement: $W \rightarrow l \nu$

■ Signature:

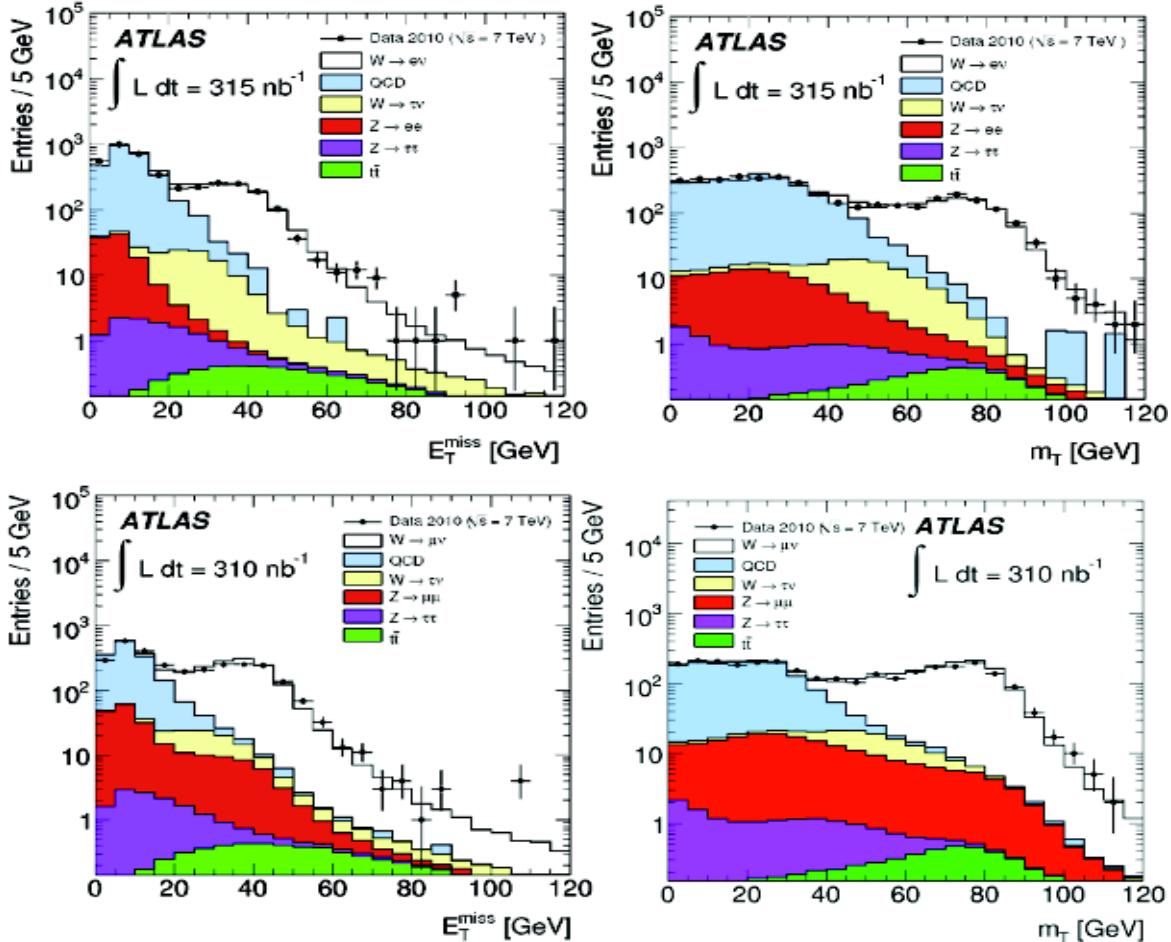
- Single charged lepton and missing transverse energy (MET)
- Leptons are high p_T and isolated
- MET from neutrino
- Peaking at transverse invariant mass



W selection

Electrons:

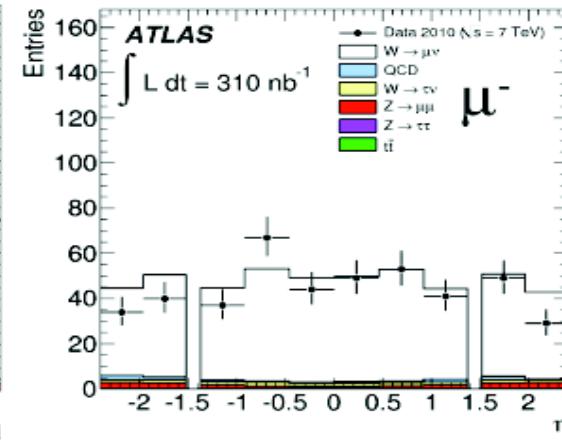
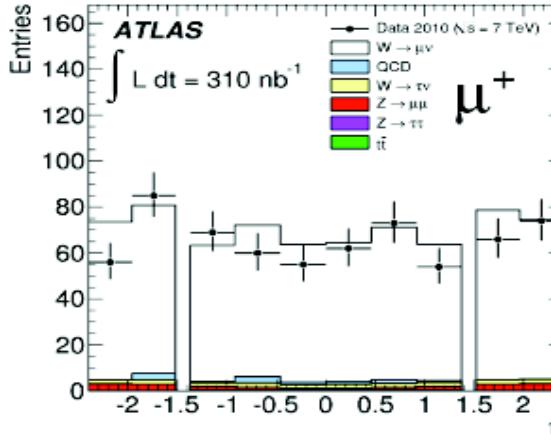
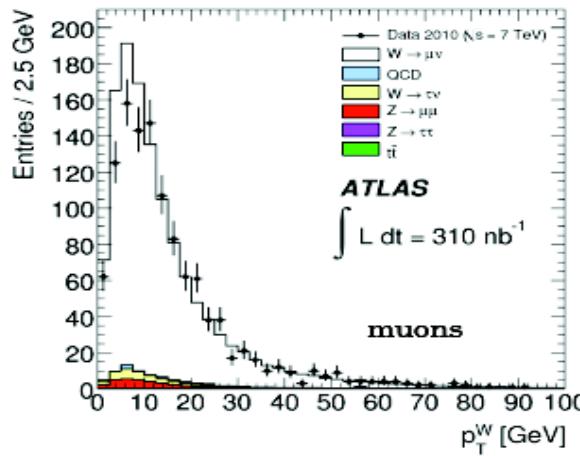
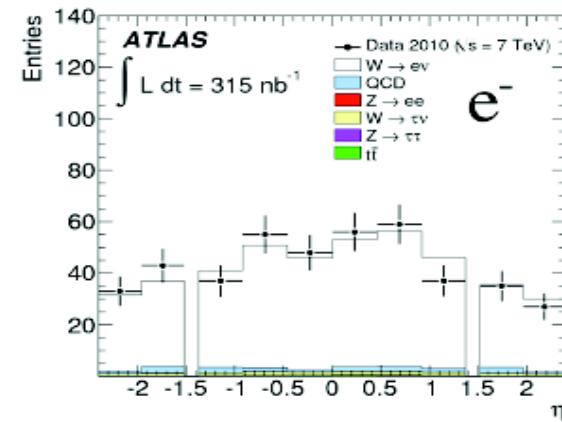
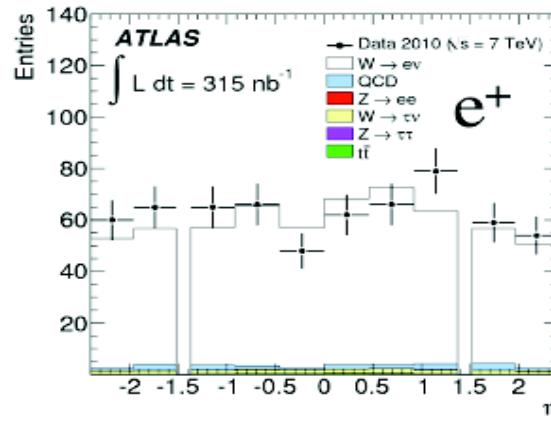
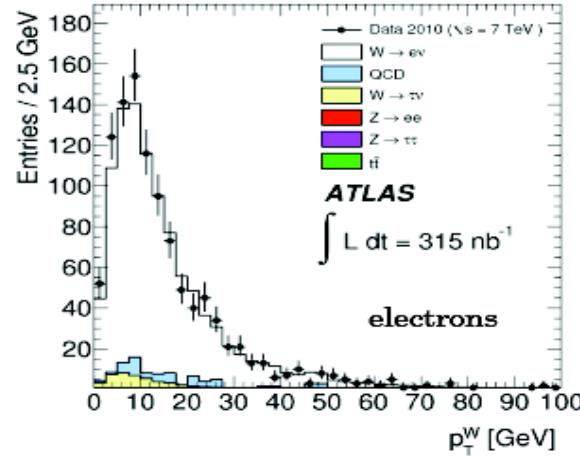
- $E_T > 20 \text{ GeV}$
- *Tight ID*
- $\text{Missing } E_T > 25 \text{ GeV}$
- $m_T > 40 \text{ GeV}$
- **1069 Candidates**



Muons:

- $p_T > 20 \text{ GeV}$
- *Track isolation*
- $\text{Missing } E_T > 25 \text{ GeV}$
- $m_T > 40 \text{ GeV}$
- **1181 Candidates**

W candidate kinematic distribution



W backgrounds

Electrons:

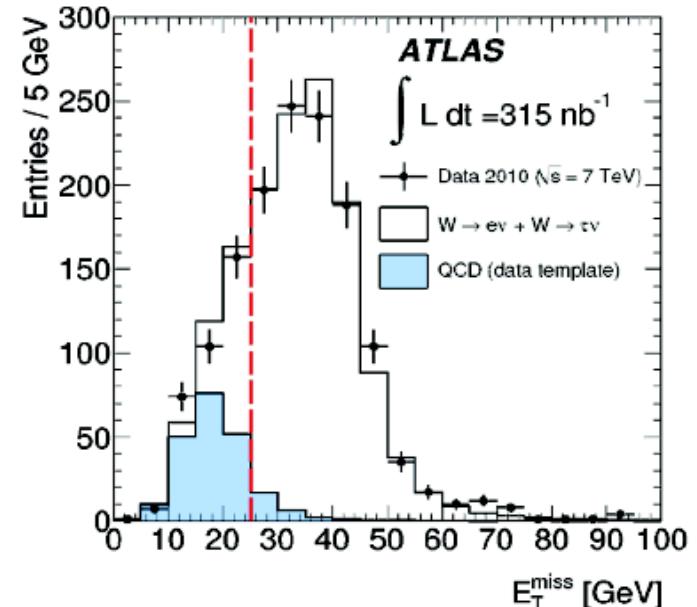
- EW + top background: $W \rightarrow \tau \nu + Z \rightarrow e^+ e^- + t\bar{t}$
 $N_{EW+TOP} = 33.5 \pm 0.2(\text{stat}) \pm 3.0(\text{syst})$
- QCD background is estimated with the template method using the missing energy distribution.
 $N_{QCD} = 28.0 \pm 3.0(\text{stat}) \pm 10.0(\text{syst})$

Muons:

- EW + top background: $Z \rightarrow \mu^+ \mu^- + W \rightarrow \tau \nu + t\bar{t}$
 $N_{EW+TOP} = 77.6 \pm 0.3(\text{stat}) \pm 5.4(\text{syst})$
- QCD background estimated from comparison of events seen in data after the full selection to number of events observed if the isolation is not applied.
 $N_{QCD} = 22.8 \pm 4.6(\text{stat}) \pm 8.7(\text{syst})$

$$N_{loose} = N_{nonQCD} + N_{QCD}$$

$$N_{iso} = \epsilon_{nonQCD}^{iso} N_{nonQCD} + \epsilon_{QCD}^{iso} N_{QCD}$$



W cross-section measurements

The total cross section for each lepton channel can be obtained by:

$$\sigma_W \times BR(W \rightarrow l\nu) = \frac{N_W^{obs} - N^{bkg}}{A_W C_W L_{int}}$$

A_W is the geometrical acceptance calculated at generator level:

$$A_W = \left(\frac{N^{acc}}{N^{all}} \right)_{gen}$$

MC	A_W $W^+ \rightarrow e^+\nu$	A_W $W^- \rightarrow e^-\nu$	A_W $W \rightarrow e\nu$	A_W $W^+ \rightarrow \mu^+\nu$	A_W $W^- \rightarrow \mu^-\nu$	A_W $W \rightarrow \mu\nu$
PYTHIA MRST LO*	0.466	0.457	0.462	0.484	0.475	0.480
PYTHIA CTEQ6.6	0.479	0.458	0.471	0.499	0.477	0.490
PYTHIA HERAPDF1.0	0.477	0.461	0.470	0.496	0.479	0.489
MC@NLO HERAPDF1.0	0.475	0.454	0.465	0.494	0.472	0.483
MC@NLO CTEQ6.6	0.478	0.452	0.465	0.496	0.470	0.483

C_W components and uncertainties

$$\sigma_W \times BR(W \rightarrow l\nu) = \frac{N_W^{obs} - N^{bkg}}{A_W C_W L_{int}}$$

- C_W is a factor correcting for reconstruction, identification and trigger efficiencies of the lepton.

	$W \rightarrow e\nu$	$W \rightarrow \mu\nu$
C_W	0.66	0.76

- Components to systematic uncertainties, are summarized below:

Parameter	$\delta C_W / C_W (\%)$	Parameter	$\delta C_W / C_W (\%)$
Trigger efficiency	<0.2	Trigger efficiency	1.9
Material effects, reconstruction and identification	5.6	Reconstruction efficiency	2.5
Energy scale and resolution	3.3	Momentum scale	1.2
E_T^{miss} scale and resolution	2.0	Momentum resolution	0.2
Problematic regions in the calorimeter	1.4	E_T^{miss} scale and resolution	2.0
Pile-up	0.5	Isolation efficiency	1.0
Charge misidentification	0.5	Theoretical uncertainty (PDFs)	0.3
FSR modelling	0.3	Total uncertainty	4.0
Theoretical uncertainty (PDFs)	0.3		
Total uncertainty	7.0		

Electrons

Muons

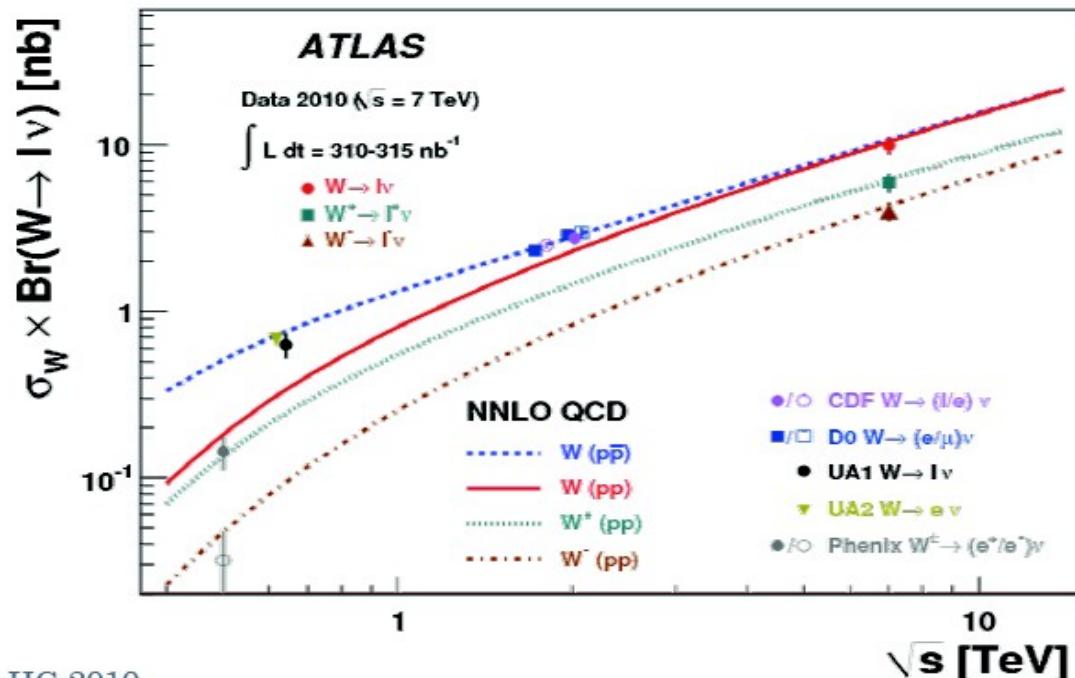
W cross-section results

$L \approx 310 - 315 \text{ nb}^{-1}$

Theory prediction : $10.46 \pm 0.42 \text{ nb}$

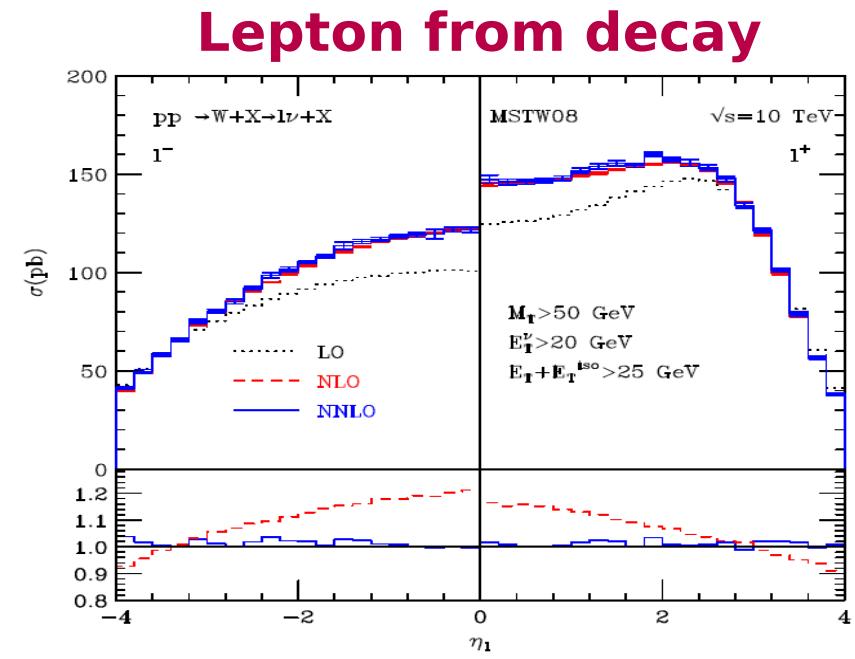
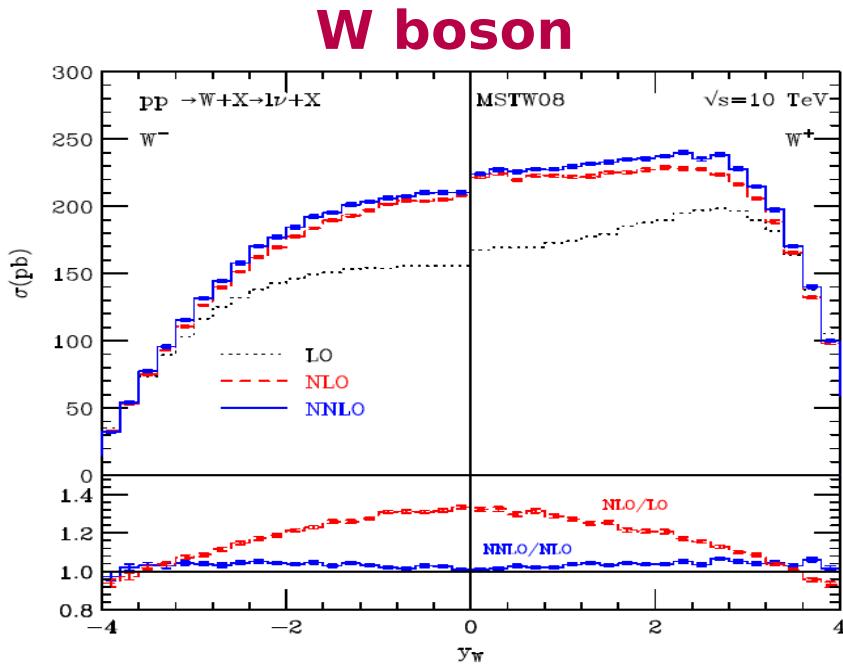
$$\sigma_W \times BR(W \rightarrow e\nu) = [10.51 \pm 0.34(\text{stat}) \pm 0.81(\text{sys}) \pm 1.16(\text{lumi})] \text{ nb}$$

$$\sigma_W \times BR(W \rightarrow \mu\nu) = [9.58 \pm 0.30(\text{stat}) \pm 0.50(\text{sys}) \pm 1.05(\text{lumi})] \text{ nb}$$



W rapidity distribution in pp collision (7TeV LHC)

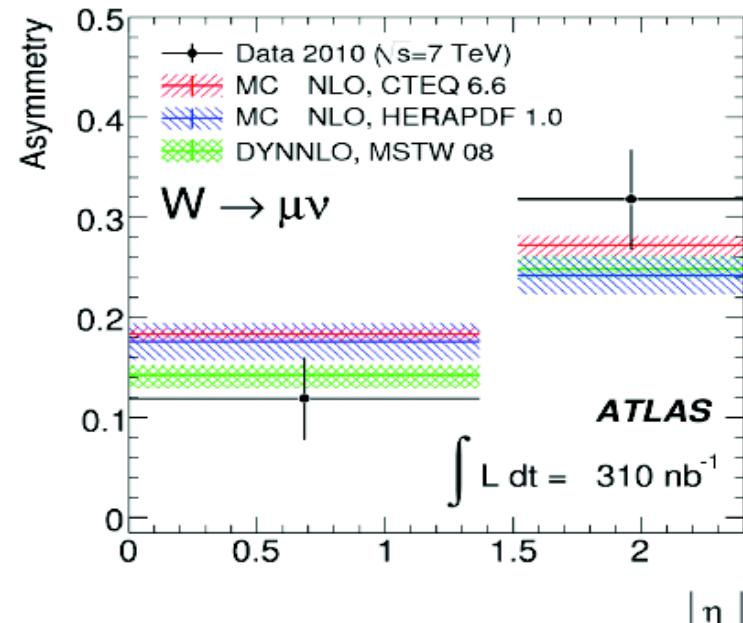
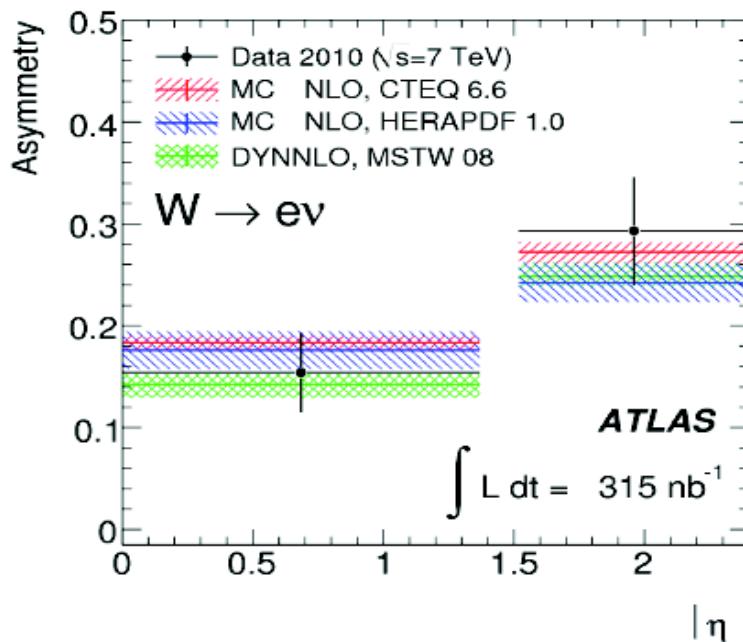
- In pp collision production asymmetry between positive and negative charge; effective asymmetry in rapidity distribution follow



W charge asymmetry

- W^+ and W^- are produced at different rates, which can be measured via the lepton charge asymmetry. This measurement is important to constraint PDFs.
- Many uncertainties cancel fully or partially
- Asymmetry is expected to increase with rapidity

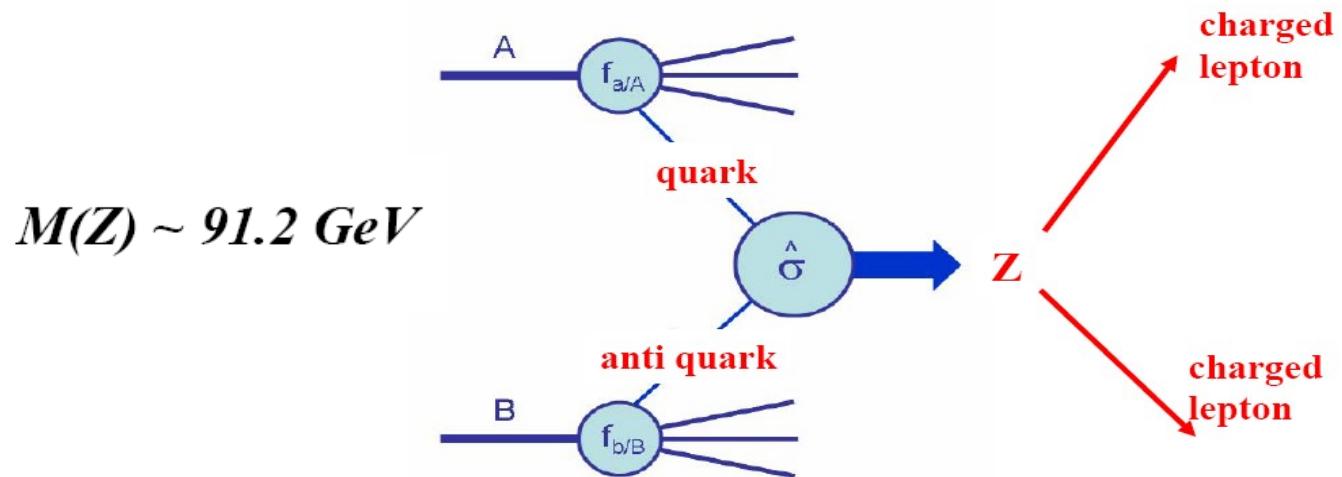
$$A_\ell = \frac{\sigma_{W^+} - \sigma_{W^-}}{\sigma_{W^+} + \sigma_{W^-}}$$



Z cross-section measurement

■ Signature:

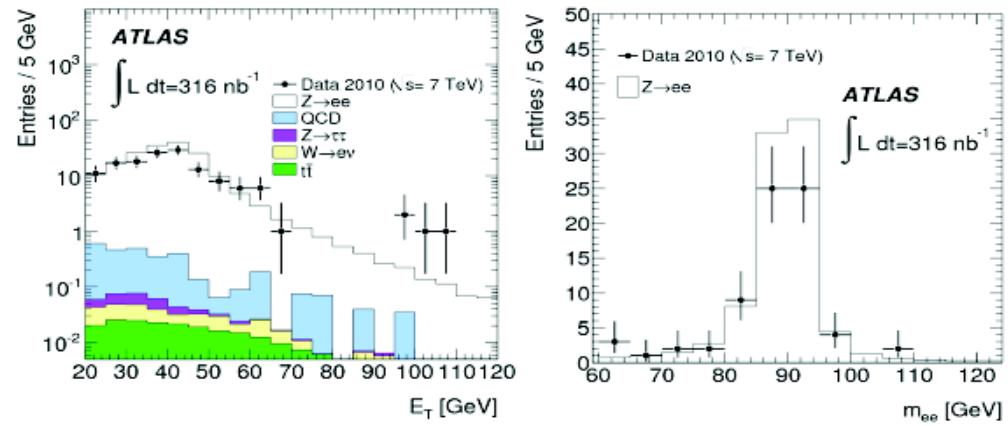
- Pair of charged leptons with opposite-charge
 - Leptons are high pT and isolated
 - Peak in l^+l^- invariant mass



Z events selection

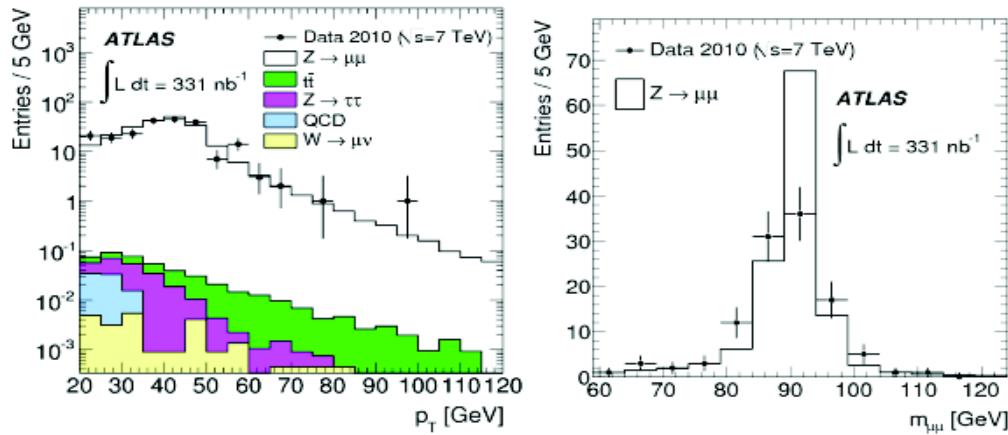
2 Electrons :

- $E_T > 20 \text{ GeV}$
- *Opposite charge*
- *Medium ID*
- $66 < m_{ee} < 116 \text{ GeV}$
- **70 Candidates**



2 Muons :

- $p_T > 20 \text{ GeV}$
- *Track isolation*
- *Opposite charge*
- $66 < m_{\mu\mu} < 116 \text{ GeV}$
- **109 Candidates**



Z backgrounds and cross-section within $66 \text{ GeV} < m_{ll} < 116 \text{ GeV}$

Electron background:

- EW + top background: $N_{\text{EW+TOP}} = 0.27 \pm 0.00(\text{stat}) \pm 0.03(\text{syst})$
- QCD background estimate: $N_{\text{QCD}} = 0.91 \pm 0.11(\text{stat}) \pm 0.41(\text{syst})$

Muon background:

- EW + top background: $N_{\text{EW+TOP}} = 0.21 \pm 0.01(\text{stat}) \pm 0.01(\text{syst})$
- QCD background estimate: $N_{\text{QCD}} = 0.04 \pm 0.01(\text{stat}) \pm 0.04(\text{syst})$

Cross section measurement

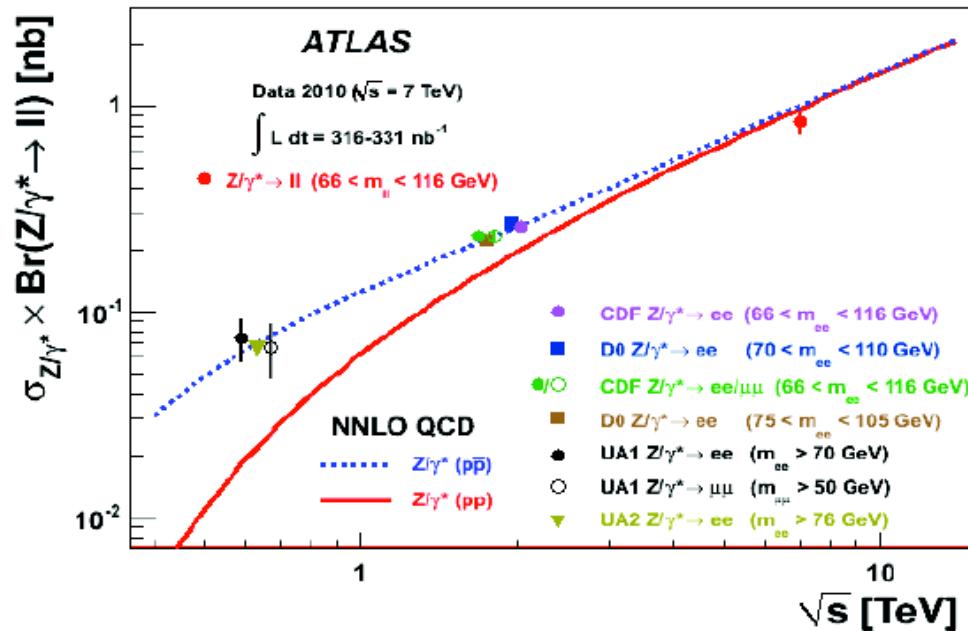
- Similar method as for the W
- The correction factor C_Z
 - Electron: $65.1\% \pm 6.1\%$
 - Muon: $77.3\% \pm 4.3\%$
- A_Z (table)

$$\sigma \times BR(Z \rightarrow ll) = \frac{N_Z^{obs} - N^{bkg}}{A_Z C_Z L_{int}}$$

MC	A_Z $Z \rightarrow e^+e^-$	A_Z $Z \rightarrow \mu^+\mu^-$
PYTHIA MRST LO*	0.446	0.486
PYTHIA CTEQ6.6	0.455	0.496
PYTHIA HERAPDF1.0	0.451	0.492
MC@NLO HERAPDF1.0	0.440	0.479
MC@NLO CTEQ6.6	0.445	0.485

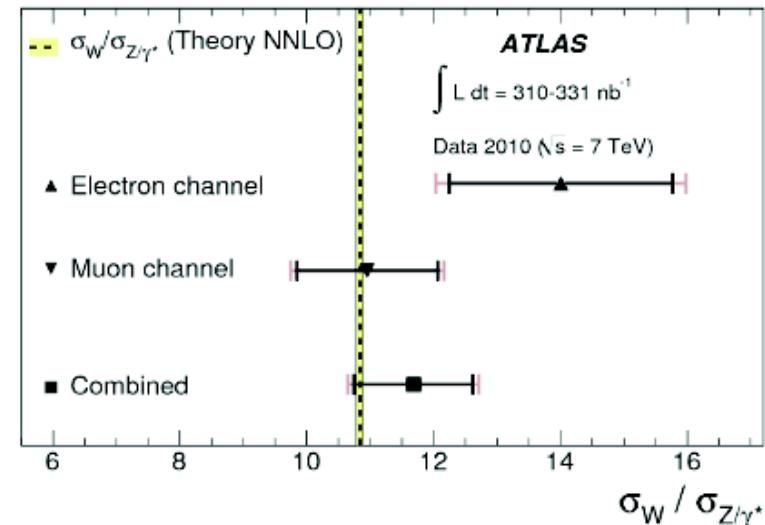
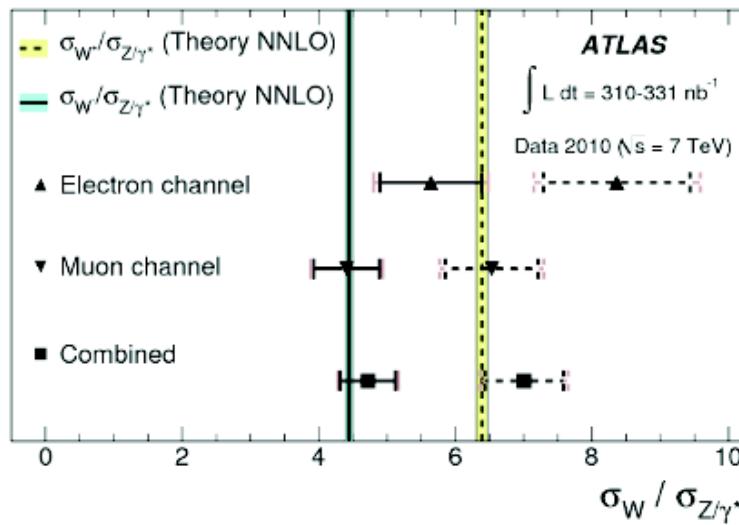
Z/γ^* cross-section results

Theory prediction : 0.96 ± 0.04 nb for [66 – 116] GeV mass window
 $\sigma_Z \times BR(Z \rightarrow e^+e^-) = [0.75 \pm 0.09(stat) \pm 0.08(sys) \pm 0.08(lumi)]$ nb
 $\sigma_Z \times BR(Z \rightarrow \mu^+\mu^-) = [0.87 \pm 0.08(stat) \pm 0.06(sys) \pm 0.10(lumi)]$ nb



W/Z ratio measurement

- The measured ratios between the W+ and W- and the Z cross section in the electron and muon decay channels compared to the theoretical predictions based on NNLO QCD calculations.



The calculations are based on the FEWZ program with the MSTW2008 NNLO PDFs

ATLAS results

- W and Z cross sections have been extracted with $310 - 315 \text{ nb}^{-1}$ with the ATLAS Detector
- W cross-section measurement included observed 1069 $W \rightarrow e\nu$ and 1081 $W \rightarrow \mu\nu$
- Z cross-section measurement included observed 70 $Z \rightarrow e\nu$ and 109 $Z \rightarrow \mu\mu$
- The W asymmetry and Z/W ratio have been extracted
- Results agree well with Standard Model predictions

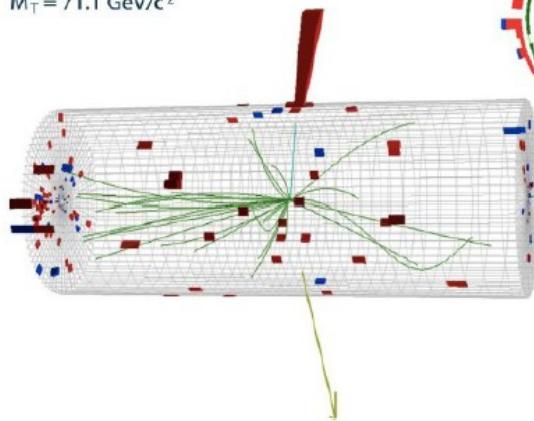
Paper with results has been submitted for publication to JHEP
<http://arxiv.org/abs/1010.2130>

Electron channel W and Z events

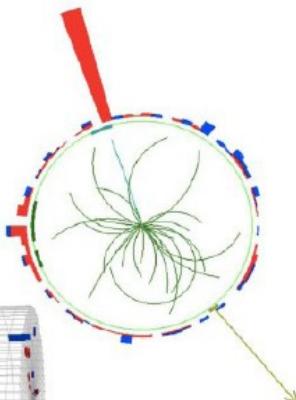


CMS Experiment at LHC, CERN
Run 133874, Event 21466935
Lumi section: 301
Sat Apr 24 2010, 05:19:21 CEST

Electron $p_T = 35.6 \text{ GeV}/c$
 $M_{ET} = 36.9 \text{ GeV}$
 $M_T = 71.1 \text{ GeV}/c^2$



$W \rightarrow e\nu$

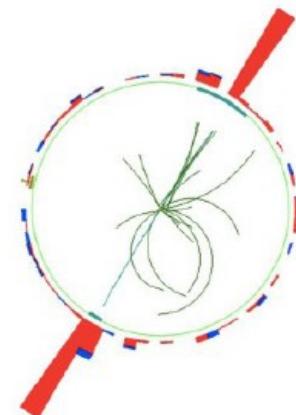
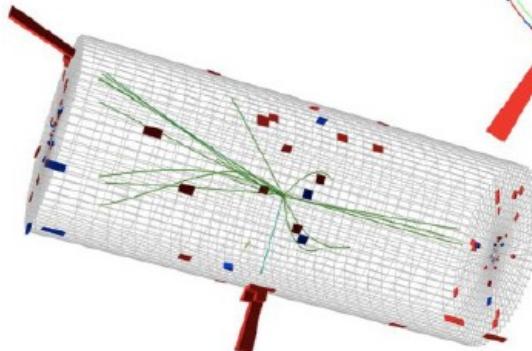


$Z \rightarrow ee$

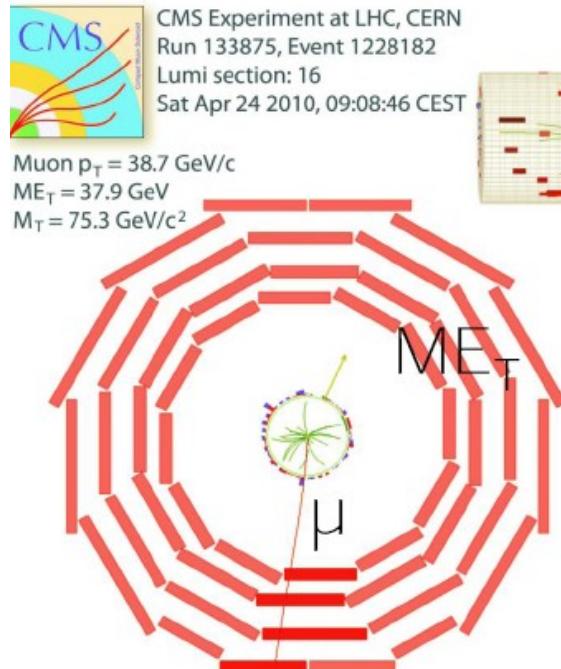


CMS Experiment at LHC, CERN
Run 133877, Event 28405693
Lumi section: 387
Sat Apr 24 2010, 14:00:54 CEST

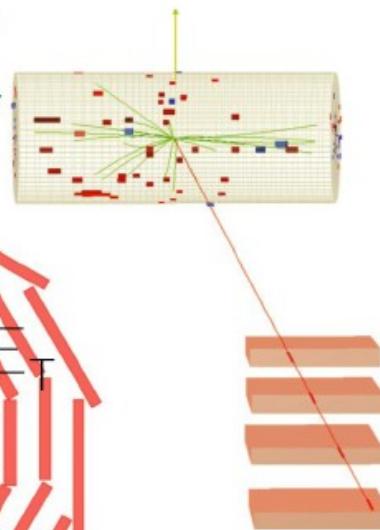
Electrons $p_T = 34.0, 31.9 \text{ GeV}/c$
Inv. mass = $91.2 \text{ GeV}/c^2$



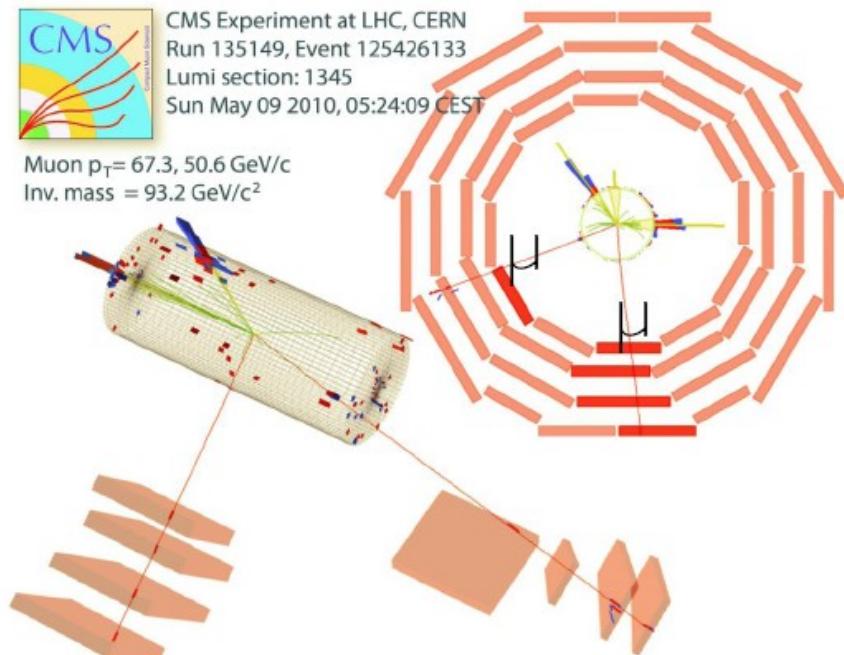
Muon channel W and Z events



W Candidate



Z Candidate

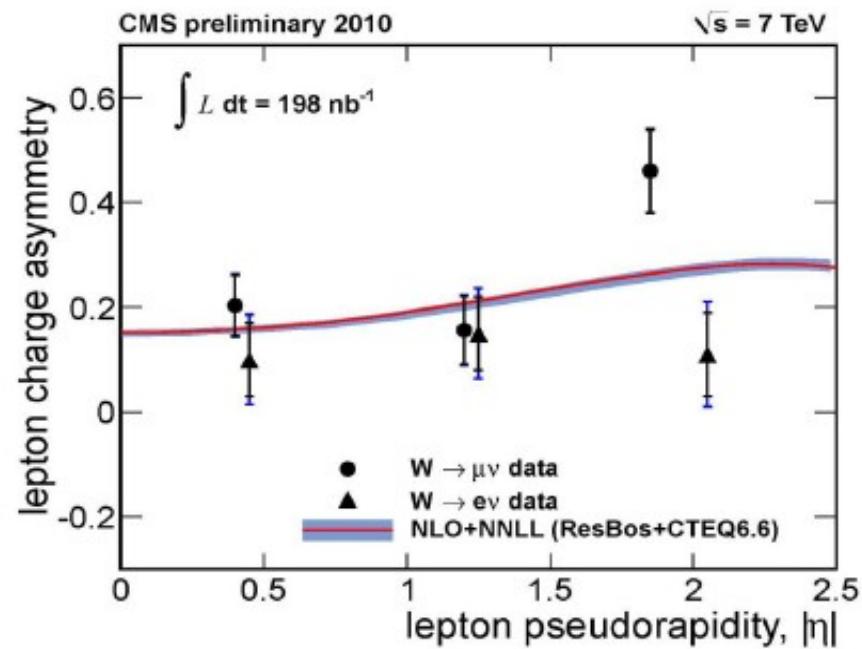


CMS results

- Presented at conferences with 198 pb^{-1}
- Here shown asymmetry only

$$A(\eta) = \frac{d\sigma^{(+)} / d\eta_\ell - d\sigma^{(-)} / d\eta_\ell}{d\sigma^{(+)} / d\eta_\ell + d\sigma^{(-)} / d\eta_\ell}$$

- First measurement in three rapidity bins
In agreement with SM predictions



Next topics

- 10.11 - W,Z bosons
 - Precise measurements at Tevatron
 - Phenix, Hera
 - LHC prospects
- 17.11 -
 - W + jets
 - Tops: xsection, mass
- 24.11 - Hot topics: new exclusion limits
- 1.12, 8.12, 15.12 - Higgs