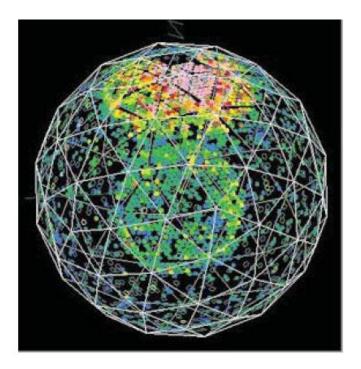
Elementary Particle Physics: theory and experiments

The Weak Interaction and V-A



Follow the course/slides from M. A. Thomson lectures at Cambridge University

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Parity

* The parity operator performs spatial inversion through the origin: $\psi'(\vec{x},t) = \hat{P}\psi(\vec{x},t) = \psi(-\vec{x},t)$ • applying \hat{P} twice: $\hat{P}\hat{P}\psi(\vec{x},t) = \hat{P}\psi(-\vec{x},t) = \psi(\vec{x},t)$ so $\hat{P}\hat{P} = I \longrightarrow \hat{P}^{-1} = \hat{P}$

To preserve the normalisation of the wave-function

$$\begin{split} \langle \psi | \psi \rangle &= \langle \psi' | \psi' \rangle = \langle \psi | \hat{P}^{\dagger} \hat{P} | \psi \rangle \\ \hat{P}^{\dagger} \hat{P} &= I & \rightarrow \hat{P} & \text{Unitary} \\ \text{But since } \hat{P} \hat{P} &= I & \hat{P} & \neq \hat{P} & \text{Hermitian} \end{split}$$

which implies Parity is an observable quantity. If the interaction Hamiltonian commutes with \hat{P} , parity is an observable conserved quantity

- If $\psi(\vec{x},t)$ is an eigenfunction of the parity operator with eigenvalue P $\hat{P}\psi(\vec{x},t) = P\psi(\vec{x},t) \longrightarrow \hat{P}\hat{P}\psi(\vec{x},t) = P\hat{P}\psi(\vec{x},t) = P^2\psi(\vec{x},t)$ since $\hat{P}\hat{P} = I$ $P^2 = 1$ $P^2 = 1$ $P^2 = 1$
- **★ QED** and QCD are invariant under parity

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* Experimentally observe that Weak Interactions do not conserve parity

Intrinsic Parities of fundamental particles:

Spin-1 Bosons

•From Gauge Field Theory can show that the gauge bosons have P = -1

$$P_{\gamma} = P_g = P_{W^+} = P_{W^-} = P_Z = -1$$

Spin-¹/₂ Fermions

• From the Dirac equation showed :

Spin $\frac{1}{2}$ particles have opposite parity to spin $\frac{1}{2}$ anti-particles • Conventional choice: spin $\frac{1}{2}$ particles have P = +1

$$P_{e^-} = P_{\mu^-} = P_{\tau^-} = P_{\nu} = P_q = +1$$

and anti-particles have opposite parity, i.e.

$$P_{e^+} = P_{\mu^+} = P_{\tau^+} = P_{\overline{\nu}} = P_{\overline{q}} = -1$$

★ For Dirac spinors it was shown that the parity operator is:

$$\hat{P} = \gamma^0 = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

Parity Conservation in QED and QCD

•Consider the QED process $e^-q \rightarrow e^-q$

• The Feynman rules for QED give:

$$-iM = [\overline{u}_e(p_3)ie\gamma^{\mu}u_e(p_1)]\frac{-ig_{\mu\nu}}{q^2}[\overline{u}_q(p_4)ie\gamma^{\nu}u_q(p_2)]$$

•Which can be expressed in terms of the electron and quark 4-vector currents:

$$M = -\frac{e^{-}}{q^{2}}g_{\mu\nu}j_{e}^{\mu}j_{q}^{\nu} = -\frac{e^{-}}{q^{2}}j_{e}.j_{q}$$

with $j_{e} = \overline{u}_{e}(p_{3})\gamma^{\mu}u_{e}(p_{1})$ and $j_{q} = \overline{u}_{q}(p_{4})\gamma^{\mu}u_{q}(p_{2})$

$$e^{-p_1}$$
 μ p_3 e^{-p_2} p_4 p_4 q

★Consider the what happen to the matrix element under the parity transformation

Spinors transform as

$$u \stackrel{\hat{P}}{\to} \hat{P}u = \gamma^0 u$$

Adjoint spinors transform as

$$\begin{split} \overline{u} &= u^{\dagger} \gamma^{0} \xrightarrow{P} (\hat{P}u)^{\dagger} \gamma^{0} = u^{\dagger} \gamma^{0\dagger} \gamma^{0} = u^{\dagger} \gamma^{0} \gamma^{0} = \overline{u} \gamma^{0} \\ \overline{u} \xrightarrow{\hat{P}} \overline{u} \gamma^{0} \end{split}$$

$$\bullet \text{ Hence } j_{e} &= \overline{u}_{e}(p_{3}) \gamma^{\mu} u_{e}(p_{1}) \xrightarrow{\hat{P}} \overline{u}_{e}(p_{3}) \gamma^{0} \gamma^{\mu} \gamma^{0} u_{e}(p_{1})$$

Consider the components of the four-vector current

- The time-like component remains unchanged and the space-like components change sign
- •Similarly $j_q^0 \xrightarrow{\hat{P}} j_q^0 \qquad j_q^k \xrightarrow{\hat{P}} -j_q^k \quad k=1,2,3$

★ Consequently the four-vector scalar product

$$j_e \cdot j_q = j_e^0 j_q^0 - j_e^k j_q^k \xrightarrow{P} j_e^0 j_q^0 - (-j_e^k)(-j_q^k) = j_e \cdot j_q \quad k = 1,3$$

or
$$j^{\mu} \xrightarrow{\hat{P}} j_{\mu}$$

 $j^{\mu}.j^{\nu} \xrightarrow{\hat{P}} j_{\mu}.j_{\nu}$
 $\xrightarrow{\hat{P}} j^{\mu}.j^{\nu}$

QED Matrix Elements are Parity Invariant

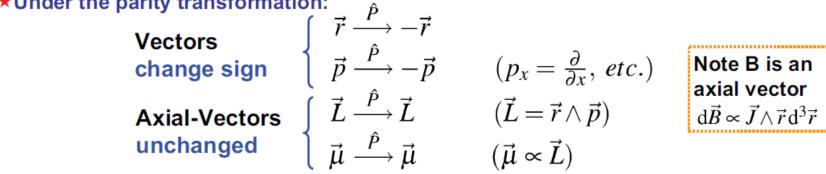
Parity Conserved in QED

★ The QCD vertex has the same form and, thus,

Parity Conserved in QCD

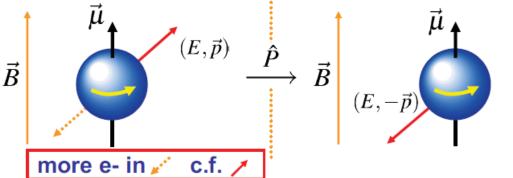
Parity Violation in β-Decay

★The parity operator \hat{P} corresponds to a discrete transformation $x \rightarrow -x$, *etc*. **★**Under the parity transformation:



1957: C.S.Wu et al. studied beta decay of polarized cobalt-60 nuclei: ${}^{60}\text{Co} \rightarrow {}^{60}Ni^ + e^- + \overline{v}_e$

* Observed electrons emitted preferentially in direction opposite to applied field



If parity were conserved: expect equal rate for producing e⁻ in directions along and opposite to the nuclear spin.

*Conclude parity is violated in WEAK INTERACTION \rightarrow that the WEAK interaction vertex is NOT of the form $\overline{u}_e \gamma^\mu u_\nu$

Bilinear Covariants

* The requirement of Lorentz invariance of the matrix element severely restricts the form of the interaction vertex. QED and QCD are "VECTOR" interactions:

$$j^{\mu} = \overline{\psi} \gamma^{\mu} \phi$$

* This combination transforms as a 4-vector (Handout 2 appendix V)

In general, there are only 5 possible combinations of two spinors and the gamma matrices that form Lorentz invariant currents, called "bilinear covariants":

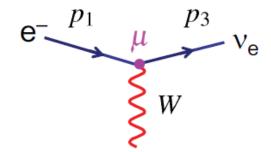
Туре	Form	Components	"Boson Spin"
SCALAR	$\overline{\psi}\phi$	1	0
PSEUDOSCALAR	$\overline{\psi}\gamma^5\phi$	1	0
VECTOR	$\overline{\psi}\gamma^{\mu}\phi$	4	1
AXIAL VECTOR	$\overline{\psi}\gamma^{\mu}\gamma^{5}\phi$	4	1
TENSOR	$\overline{\psi}(\gamma^{\mu}\gamma^{ u}-\gamma^{ u}\gamma^{\mu}$	²) φ 6	2

Note that in total the sixteen components correspond to the 16 elements of a general 4x4 matrix: "decomposition into Lorentz invariant combinations"

- * In QED the factor $g_{\mu\nu}$ arose from the sum over polarization states of the virtual photon (2 transverse + 1 longitudinal, 1 scalar) = (2J+1) + 1
- Associate SCALAR and PSEUDOSCALAR interactions with the exchange of a SPIN-0 boson, etc. – no spin degrees of freedom

V-A Structure of the Weak Interaction

- *The most general form for the interaction between a fermion and a boson is a linear combination of bilinear covariants
- For an interaction corresponding to the exchange of a spin-1 particle the most general form is a linear combination of VECTOR and AXIAL-VECTOR
- * The form for WEAK interaction is <u>determined from experiment</u> to be VECTOR - AXIAL-VECTOR (V - A)



$$j^{\mu} \propto \overline{u}_{\nu_e} (\gamma^{\mu} - \gamma^{\mu} \gamma^5) u_e$$

V – A

- ★ Can this account for parity violation?
- ★ First consider parity transformation of a pure AXIAL-VECTOR current

$$j_{A} = \overline{\psi} \gamma^{\mu} \gamma^{5} \phi \qquad \text{with} \qquad \gamma^{5} = i \gamma^{0} \gamma^{1} \gamma^{2} \gamma^{3}; \qquad \gamma^{5} \gamma^{0} = -\gamma^{0} \gamma^{5}$$

$$j_{A} = \overline{\psi} \gamma^{\mu} \gamma^{5} \phi \qquad \stackrel{\hat{P}}{\longrightarrow} \overline{\psi} \gamma^{0} \gamma^{\mu} \gamma^{5} \gamma^{0} \phi = -\overline{\psi} \gamma^{0} \gamma^{\mu} \gamma^{0} \gamma^{5} \phi$$

$$j_{A}^{0} = \stackrel{\hat{P}}{\longrightarrow} -\overline{\psi} \gamma^{0} \gamma^{0} \gamma^{0} \gamma^{5} \phi = -\overline{\psi} \gamma^{0} \gamma^{5} \phi = -j_{A}^{0}$$

$$j_{A}^{k} = \stackrel{\hat{P}}{\longrightarrow} -\overline{\psi} \gamma^{0} \gamma^{k} \gamma^{0} \gamma^{5} \phi = +\overline{\psi} \gamma^{k} \gamma^{5} \phi = +j_{A}^{k} \qquad k = 1, 2, 3 \qquad \text{or} \qquad j_{A}^{\mu} \stackrel{\hat{P}}{\longrightarrow} -j_{A\mu}$$

 The space-like components remain unchanged and the time-like components change sign (the opposite to the parity properties of a vector-current)

$$j_A^0 \xrightarrow{\hat{P}} -j_A^0; \quad j_A^k \xrightarrow{\hat{P}} +j_A^k; \qquad j_V^0 \xrightarrow{\hat{P}} +j_V^0; \quad j_V^k \xrightarrow{\hat{P}} -j_V^k$$

Now consider the matrix elements

$$M \propto g_{\mu\nu} j_1^{\mu} j_2^{\nu} = j_1^0 j_2^0 - \sum_{k=1,3} j_1^k j_2^k$$

For the combination of a two axial-vector currents

$$j_{A1}.j_{A2} \xrightarrow{P} (-j_1^0)(-j_2^0) - \sum_{k=1,3} (j_1^k)(j_2^k) = j_{A1}.j_{A2}$$

- Consequently parity is conserved for both a pure vector and pure axial-vector interactions
- However the combination of a vector current and an axial vector current

$$j_{V1}, j_{A2} \xrightarrow{P} (j_1^0)(-j_2^0) - \sum_{k=1,3} (-j_1^k)(j_2^k) = -j_{V1}, j_{A2}$$

changes sign under parity – can give parity violation !

Now consider a general linear combination of VECTOR and AXIAL-VECTOR (note this is relevant for the Z-boson vertex)

$$\psi_{1} \qquad \psi_{1} \qquad \psi_{1} \qquad \int_{V_{1}} \frac{1}{q} = \overline{\phi}_{1} (g_{V} \gamma^{\mu} + g_{A} \gamma^{\mu} \gamma^{5}) \psi_{1} = g_{V} j_{1}^{V} + g_{A} j_{1}^{A} \qquad \frac{g_{\mu\nu}}{q^{2} - m^{2}} \qquad \psi_{2} \qquad \phi_{2} \qquad \int_{J_{2}} \frac{g_{\mu\nu}}{q^{2} - m^{2}} \\ \frac{g_{\mu\nu}}{q^{2} - m^{2}} \\ \qquad \int_{J_{2}} \frac{g_{\mu\nu}}{q^{2} - m^{2}} \\ \frac{g_{\mu\nu}}{q^{$$

Consider the parity transformation of this scalar product

$$j_1.j_2 \xrightarrow{P} g_V^2 j_1^V.j_2^V + g_A^2 j_1^A.j_2^A - g_V g_A(j_1^V.j_2^A + j_1^A.j_2^V)$$

• If either g_A or g_V is zero, Parity is conserved, i.e. parity conserved in a pure VECTOR or pure AXIAL-VECTOR interaction

• Relative strength of parity violating part $\,\propto\,$

$$\frac{g_V g_A}{g_V^2 + g_A^2}$$

Maximal Parity Violation for V-A (or V+A)

Chiral Structure of QED (Reminder)

★ Recall introduced CHIRAL projections operators

$$P_R = \frac{1}{2}(1+\gamma^5); \quad P_L = \frac{1}{2}(1-\gamma^5)$$

project out chiral right- and left- handed states

- * In the ultra-relativistic limit, chiral states correspond to helicity states
- ★ Any spinor can be expressed as:

$$\boldsymbol{\psi} = \frac{1}{2}(1+\gamma^5)\boldsymbol{\psi} + \frac{1}{2}(1-\gamma^5)\boldsymbol{\psi} = P_R\boldsymbol{\psi} + P_L\boldsymbol{\psi} = \boldsymbol{\psi}_R + \boldsymbol{\psi}_L$$

• The QED vertex $\overline{\psi}\gamma^{\mu}\phi$ in terms of chiral states:

 $\overline{\psi}\gamma^{\mu}\phi = \overline{\psi}_{R}\gamma^{\mu}\phi_{R} + \overline{\psi}_{R}\gamma^{\mu}\phi_{L} + \overline{\psi}_{L}\gamma^{\mu}\phi_{R} + \overline{\psi}_{L}\gamma^{\mu}\phi_{L}$

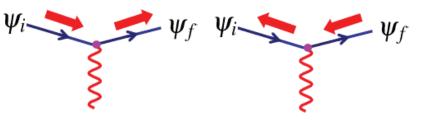
conserves chirality, e.g.

$$\overline{\psi}_{R} \gamma^{\mu} \phi_{L} = \frac{1}{2} \psi^{\dagger} (1 + \gamma^{5}) \gamma^{0} \gamma^{\mu} \frac{1}{2} (1 - \gamma^{5}) \phi$$

$$= \frac{1}{4} \psi^{\dagger} \gamma^{0} (1 - \gamma^{5}) \gamma^{\mu} (1 - \gamma^{5}) \phi$$

$$= \frac{1}{4} \overline{\psi} \gamma^{\mu} (1 + \gamma^{5}) (1 - \gamma^{5}) \phi = 0$$

In the ultra-relativistic limit only two helicity combinations are non-zero



Helicity Structure of the Weak Interactions

The charged current (W[±]) weak vertex is: $\frac{-\iota g_w}{\sqrt{2}} \frac{1}{2} \gamma^{\mu} (1 - \gamma^5)$ **★**Since $\frac{1}{2}(1-\gamma^5)$ projects out left-handed chiral particle states: $\overline{\psi}\frac{1}{2}\gamma^{\mu}(1-\gamma^{5})\phi = \overline{\psi}\gamma^{\mu}\phi_{L}$ **★**Writing $\overline{\Psi} = \overline{\Psi}_R + \overline{\Psi}_L$ and from discussion of QED, $\overline{\Psi}_R \gamma^\mu \phi_L = 0$ gives $\overline{\psi}\frac{1}{2}\gamma^{\mu}(1-\gamma^{5})\phi = \overline{\psi}_{I}\gamma^{\mu}\phi_{L}$ Only the left-handed chiral components of particle spinors and right-handed chiral components of anti-particle spinors participate in charged current weak interactions **\star** At very high energy $(E \gg m)$, the left-handed chiral components are helicity eigenstates :

 $\frac{1}{2}$

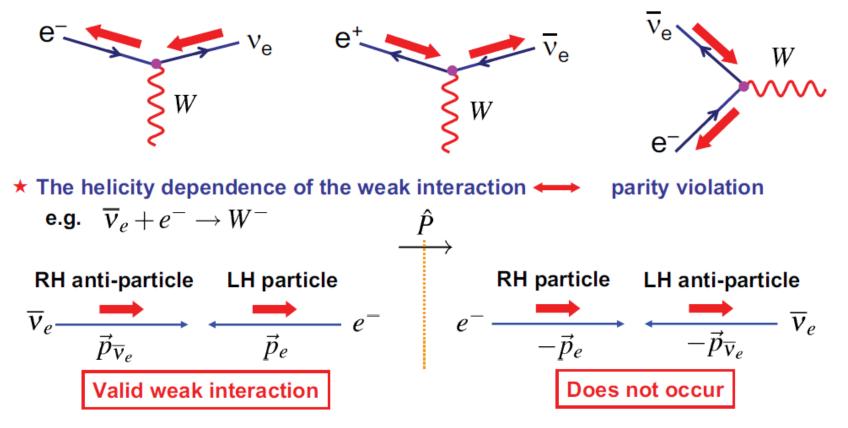
$$(1-\gamma^5)u \implies$$

LEFT-HANDED PARTICLES Helicity = -1

RIGHT-HANDED ANTI-PARTICLES Helicity = +1

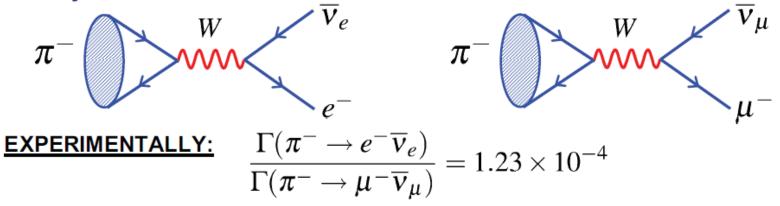
In the ultra-relativistic limit only left-handed particles and right-handed antiparticles participate in charged current weak interactions

e.g. In the relativistic limit, the only possible electron - neutrino interactions are:



Helicity in Pion Decay

The decays of charged pions provide a good demonstration of the role of helicity in the weak interaction



 Might expect the decay to electrons to dominate – due to increased phase space.... The opposite happens, the electron decay is helicity suppressed

★Consider decay in pion rest frame.

- Pion is spin zero: so the spins of the $\overline{\nu}$ and μ are opposite
- Weak interaction only couples to RH chiral anti-particle states. Since neutrinos are (almost) massless, must be in RH Helicity state
- Therefore, to conserve angular mom. muon is emitted in a RH HELICITY state



But only left-handed CHIRAL particle states participate in weak interaction

*****The general right-handed helicity solution to the Dirac equation is

$$u_{\uparrow} = N \begin{pmatrix} c \\ e^{i\phi}s \\ \frac{|\vec{p}|}{E+m}c \\ \frac{|\vec{p}|}{E+m}e^{i\phi}s \end{pmatrix}$$

with
$$c = \cos \frac{\theta}{2}$$
 and $s = \sin \frac{\theta}{2}$

 project out the left-handed <u>chiral</u> part of the wave-function using

$$P_L = \frac{1}{2}(1 - \gamma^5) = \frac{1}{2} \begin{pmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & -1 \\ -1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{pmatrix}$$

1

Ω

-1

 Ω

giving
$$P_L u_{\uparrow} = \frac{1}{2} N \left(1 - \frac{|\vec{p}|}{E+m} \right) \begin{pmatrix} c \\ e^{i\phi}s \\ -c \\ -e^{i\phi}s \end{pmatrix} = \frac{1}{2} N \left(1 - \frac{|\vec{p}|}{E+m} \right) u_L$$

In the limit $m \ll E$ this tends to zero

similarly

$$P_{R}u_{\uparrow} = \frac{1}{2}N\left(1 + \frac{|\vec{p}|}{E+m}\right)\begin{pmatrix} c\\e^{i\phi}s\\c\\e^{i\phi}s \end{pmatrix} = \frac{1}{2}N\left(1 + \frac{|\vec{p}|}{E+m}\right)u_{R}$$

In the limit $m \ll E$, $P_{R}u_{\uparrow} \rightarrow u_{R}$

* Hence
$$u_{\uparrow} = P_R u_{\uparrow} + P_L u_{\uparrow} = \frac{1}{2} \left(1 + \frac{|\vec{p}|}{E+m} \right) u_R + \frac{1}{2} \left(1 - \frac{|\vec{p}|}{E+m} \right) u_L$$

RH Helicity RH Chiral LH Chiral

- In the limit $E \gg m$, as expected, the RH chiral and helicity states are identical
- Although only LH chiral particles participate in the weak interaction the contribution from RH Helicity states is not necessarily zero !

$$\overline{v}_{\mu} \quad \longleftarrow \quad \mu^{-}$$

$$m_{\nu} \approx 0: \text{ RH Helicity } \equiv \text{ RH Chiral} \qquad \qquad m_{\mu} \neq 0: \text{ RH Helicity has}$$

$$LH \text{ Chiral Component}$$

 Expect matrix element to be proportional to LH chiral component of RH Helicity electron/muon spinor

$$M_{fi} \propto \frac{1}{2} \left(1 - \frac{|\vec{p}|}{E+m} \right) = \frac{m_{\mu}}{m_{\pi} + m_{\mu}}$$
 from the kinematics of pion decay at rest

★ Hence because the electron mass is much smaller than the pion mass the decay $\pi^- \rightarrow e^- \overline{v}_e$ is heavily suppressed.

Evidence for V-A

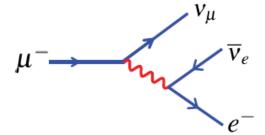
***** The V-A nature of the charged current weak interaction vertex fits with experiment

EXAMPLE charged pion decay

- Experimentally measure: $\frac{\Gamma(\pi^- \rightarrow e^- \overline{\nu}_e)}{\Gamma(\pi^- \rightarrow \mu^- \overline{\nu}_\mu)} = (1.230 \pm 0.004) \times 10^{-4}$
- Theoretical predictions (depend on Lorentz Structure of the interaction)

V-A
$$(\overline{\psi}\gamma^{\mu}(1-\gamma^{5})\phi)$$
 or V+A $(\overline{\psi}\gamma^{\mu}(1+\gamma^{5})\phi) \implies \frac{\Gamma(\pi^{-} \to e^{-}\overline{\nu}_{e})}{\Gamma(\pi^{-} \to \mu^{-}\overline{\nu}_{\mu})} \approx 1.3 \times 10^{-4}$
Scalar $(\overline{\psi}\phi)$ or Pseudo-Scalar $(\overline{\psi}\gamma^{5}\phi) \implies \frac{\Gamma(\pi^{-} \to e^{-}\overline{\nu}_{e})}{\Gamma(\pi^{-} \to \mu^{-}\overline{\nu}_{\mu})} = 5.5$

EXAMPLE muon decay



e.g. TWIST expt: <mark>6x10⁹ μ decays</mark> Phys. Rev. Lett. 95 (2005) 101805 Measure electron energy and angular distributions relative to muon spin direction. Results expressed in terms of general S+P+V+A+T form in "Michel Parameters"

 $\rho = 0.75080 \pm 0.00105$

V-A Prediction: $\rho = 0.75$

Weak Charged Current Propagator

* The charged-current Weak interaction is different from QED and QCD in that it is mediated by massive W-bosons (80.3 GeV)

This results in a more complicated form for the propagator:
showed that for the exchange of a massive particle:

 $\frac{1}{q^2} \xrightarrow{\text{massive}} \frac{1}{q^2 - m^2}$

In addition the sum over W boson polarization states modifies the numerator

W-boson propagator

spin 1 W[±]
$$\frac{-i\left[g_{\mu\nu} - q_{\mu}q_{\nu}/m_W^2\right]}{q^2 - m_W^2} \qquad \overset{\mu}{\checkmark} \overset{q}{\checkmark} \overset{\nu}{\checkmark} \overset{\nu}{\checkmark}$$

★ However in the limit where q^2 is small compared with $m_W = 80.3 \,\text{GeV}$ the interaction takes a simpler form.

Normalized W-boson propagator (
$$q^2 \ll m_W^2$$
) $rac{ig_{\mu
u}}{m_W^2}$ $\mu_{ullet} v$

• The interaction appears point-like (i.e no q² dependence)

Connection to Fermi Theory

*In 1934, before the discovery of parity violation, Fermi proposed, in analogy with QED, that the invariant matrix element for β-decay was of the form: $\$

$$M_{fi} = G_{\rm F} g_{\mu\nu} [\overline{\psi} \gamma^{\mu} \psi] [\overline{\psi} \gamma^{\nu} \psi]$$

where $G_{\rm F} = 1.166 \times 10^{-5} \, {\rm GeV^{-2}}$

Note the absence of a propagator : i.e. this represents an interaction at a point
 After the discovery of parity violation in 1957 this was modified to

$$M_{fi} = \frac{G_{\rm F}}{\sqrt{2}} g_{\mu\nu} [\overline{\psi} \gamma^{\mu} (1 - \gamma^5) \psi] [\overline{\psi} \gamma^{\nu} (1 - \gamma^5) \psi]$$

(the factor of $\sqrt{2}$ was included so the numerical value of G_F did not need to be changed) **★ Compare to the prediction for W-boson exchange**

$$M_{fi} = \left[\frac{g_W}{\sqrt{2}}\overline{\psi}\frac{1}{2}\gamma^{\mu}(1-\gamma^5)\psi\right]\frac{g_{\mu\nu} - q_{\mu}q_{\nu}/m_W^2}{q^2 - m_W^2}\left[\frac{g_W}{\sqrt{2}}\overline{\psi}\frac{1}{2}\gamma^{\nu}(1-\gamma^5)\psi\right]$$

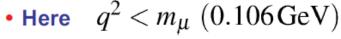
which for $q^2 \ll m_W^2$ becomes:

$$M_{fi} = \frac{g_W^2}{8m_W^2} g_{\mu\nu} [\overline{\psi}\gamma^{\mu}(1-\gamma^5)\psi] [\overline{\psi}\gamma^{\nu}(1-\gamma^5)\psi]$$

Still usually use $G_{\rm F}$ to express strength of weak interaction as the is the quantity that is precisely determined in muon decay

Strength of Weak Interaction

★ Strength of weak interaction most precisely measured in muon decay



 $q^2 \overline{v}_e$ • To a very good approximation the W-boson propagator can be written

$$\frac{-i\left[g_{\mu\nu}-q_{\mu}q_{\nu}/m_{W}^{2}\right]}{q^{2}-m_{W}^{2}}\approx\frac{ig_{\mu\nu}}{m_{W}^{2}}$$

• In muon decay measure g_W^2/m_W^2

• Muon decay \implies $G_{\rm F}=1.16639(1)\times 10^{-5}\,{\rm GeV^{-2}}$

★ To obtain the intrinsic strength of weak interaction need to know mass of W-boson: $m_W = 80.403 \pm 0.029 \,\text{GeV}$

$$\Rightarrow \qquad \alpha_W = \frac{g_W^2}{4\pi} = \frac{8m_W^2 G_F}{4\sqrt{2}\pi} = \frac{1}{30}$$

The intrinsic strength of the weak interaction is similar to, but greater than, the EM interaction ! It is the massive W-boson in the propagator which makes it appear weak. For $q^2 \gg m_W^2$ weak interactions are more likely than EM.

Summary

***** Weak interaction is of form Vector – Axial-vector (V-A)

$$\frac{-ig_w}{\sqrt{2}}\frac{1}{2}\gamma^{\mu}(1-\gamma^5)$$

 Consequently only left-handed chiral particle states and right-handed chiral anti-particle states participate in the weak interaction

MAXIMAL PARITY VIOLATION

- ★ Weak interaction also violates Charge Conjugation symmetry
- * At low q^2 weak interaction is only weak because of the large W-boson mass

$$\frac{G_{\rm F}}{\sqrt{2}} = \frac{g_W^2}{8m_W^2}$$

★ Intrinsic strength of weak interaction is similar to that of QED