

Elementary Particle Physics: theory and experiments

Interactions

Akcelerators for high energy physics

Some slides from M. A. Thomson lectures at Cambridge University

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Preliminaries: Natural Units

- S.I. UNITS: kg m s are a natural choice for “everyday” objects
- not very natural in particle physics
- instead use **Natural Units** based on the language of particle physics
 - From Quantum Mechanics - the unit of action : \hbar
 - From relativity - the speed of light: c
 - From Particle Physics - unit of energy: **GeV** (1 GeV ~ proton rest mass energy)

★ Units become (i.e. with the correct dimensions):

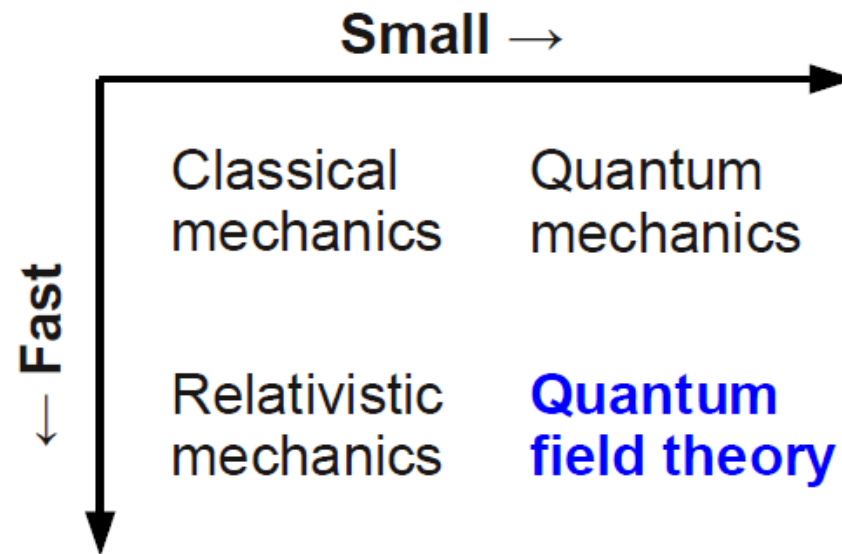
| | | | |
|----------|--------------------|--------|-----------------------------|
| Energy | GeV | Time | $(\text{GeV}/\hbar)^{-1}$ |
| Momentum | GeV/c | Length | $(\text{GeV}/\hbar c)^{-1}$ |
| Mass | GeV/c ² | Area | $(\text{GeV}/\hbar c)^{-2}$ |

★ Simplify algebra by setting: $\hbar = c = 1$

- Now all quantities expressed in powers of **GeV**

| | | | | |
|----------|-----|--------|-------------------|---|
| Energy | GeV | Time | GeV ⁻¹ | } To convert back to S.I. units, need to restore missing factors of \hbar and c |
| Momentum | GeV | Length | GeV ⁻¹ | |
| Mass | GeV | Area | GeV ⁻² | |

Quantum field theory



First major achievement: Dirac's equation for free electrons (and positrons)

$$E^2 - \mathbf{p}^2 c^2 = m^2 c^4$$
$$E = \pm \sqrt{\mathbf{p}^2 c^2 + m^2 c^4}$$

Interpretation of negative energies: sea of electrons → holes in sea act as positively charged electrons → confirmed by Anderson 1932



Paul Dirac
(NP 1933)



Carl Anderson
(NP 1936)

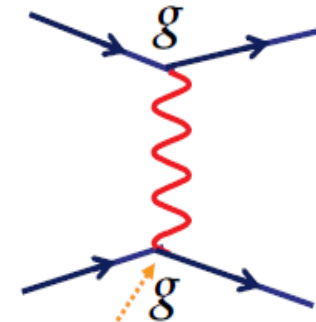
Interactions

- In particle physics high energies are needed to create new particles and to explore the structure of hadrons. Energies must be at least of several hundred MeV.
- **Any theory of elementary particles must combine the requirements of both special relativity and quantum theory.**
- For every charged particle of nature, whether elementary or a hadron, there is an associated particle of the same mass, but opposite charge, called antiparticle. This result is a necessary consequence of combining special relativity with quantum mechanics.
- **This important theoretical prediction was made by Dirac and follows from the solution of the equation he first wrote down to describe relativistic electrons.**

Forces in the Standard Model

★ Forces mediated by the exchange of **spin-1** Gauge Bosons

| Force | Boson(s) | J^P | m/GeV |
|--------------|-----------------|-------|----------------|
| EM (QED) | Photon γ | 1^- | 0 |
| Weak | W^\pm / Z | 1^- | 80 / 91 |
| Strong (QCD) | 8 Gluons g | 1^- | 0 |
| Gravity (?) | Graviton? | 2^+ | 0 |



- Fundamental interaction strength is given by charge g .
- Related to the dimensionless coupling “constant” α

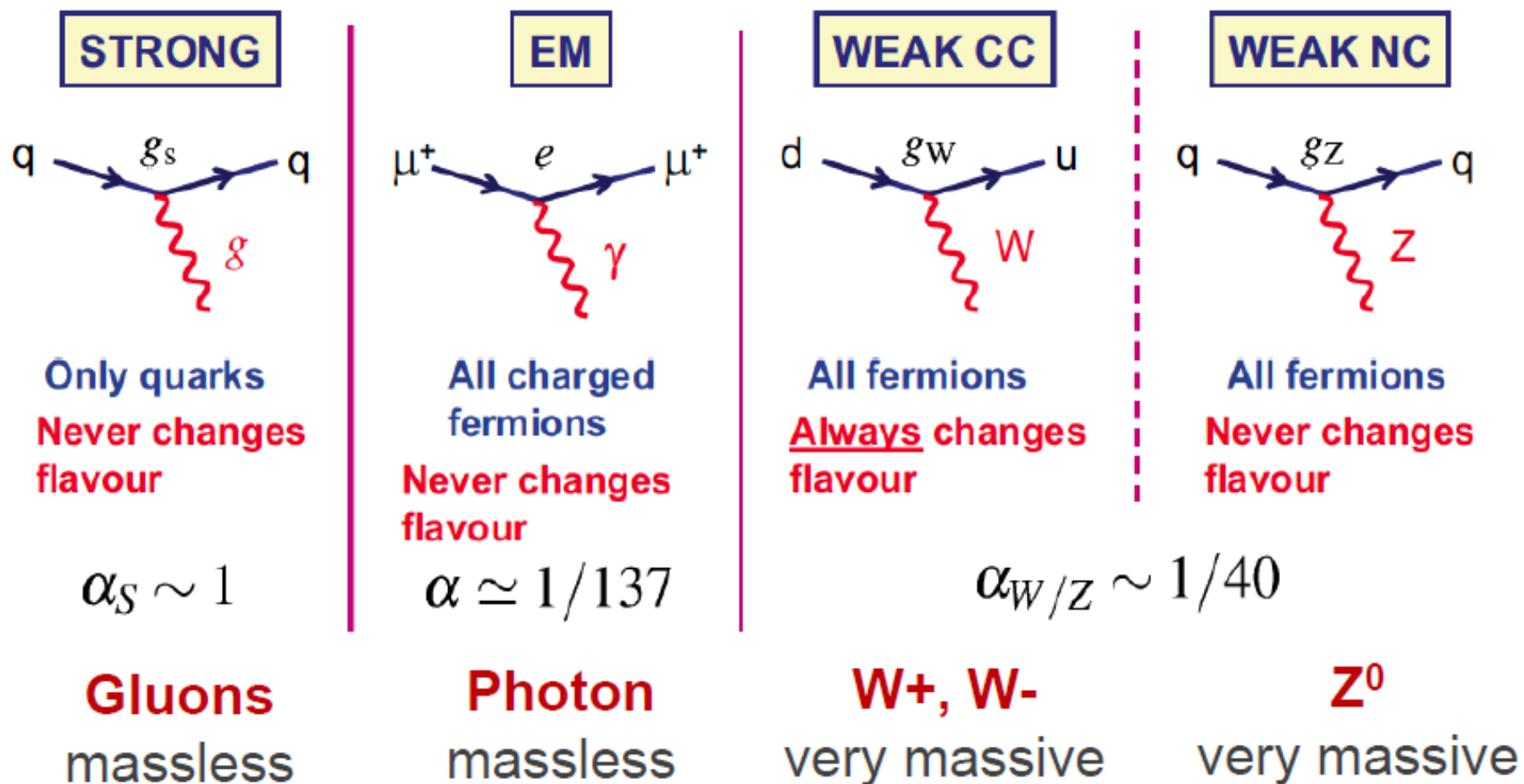
e.g. QED $g_{em} = e = \sqrt{4\pi\alpha\epsilon_0\hbar c}$

- ★ In Natural Units $g = \sqrt{4\pi\alpha}$ (both g and α are dimensionless, but g contains a “hidden” $\hbar c$)

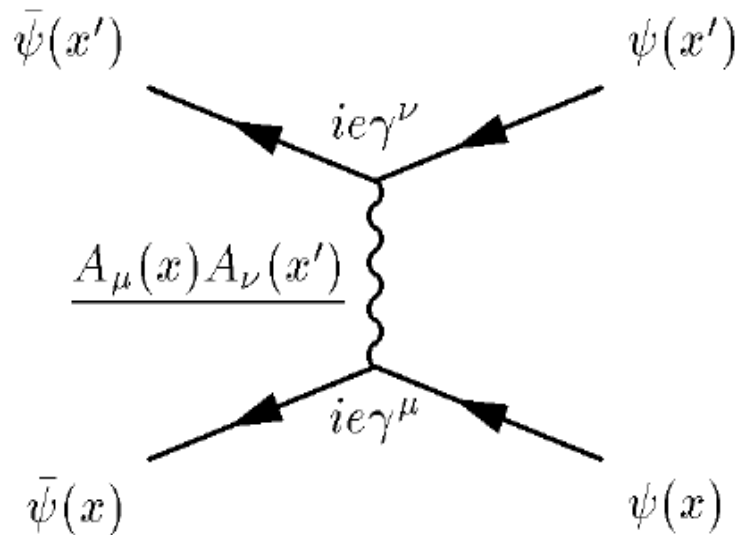
- ★ Convenient to express couplings in terms of α which, being genuinely dimensionless does not depend on the system of units (this is not true for the numerical value for e)

Standard Model vertices

The interaction of gauge bosons with fermions is described by the Standard Model



Feynman diagrams



Feynman diagrams:

Powerful tool to write down scattering amplitudes (also for higher order perturbations)

Feynman rules:

Set of rules to get from a Feynman diagram to the mathematical expression



R. Feynman
(NP 1965)

In QFTs perturbation theory is only **valid for finite energy range** → **divergences in calculation of scattering amplitudes**

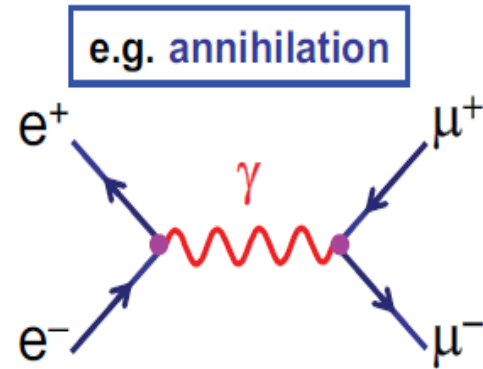
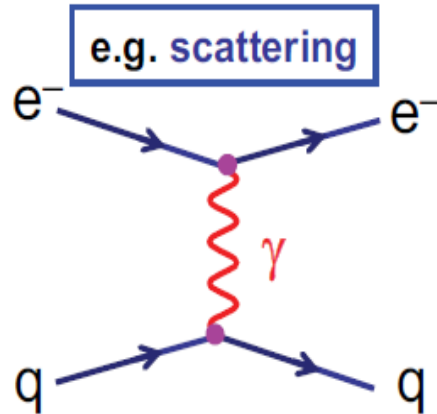
Renormalization is a technique to remove these divergences



M. Veltman and G. 't Hooft
(NP 1999)

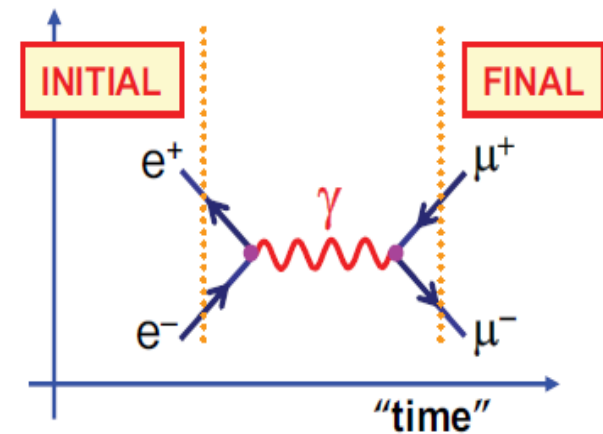
Feynman diagrams

★ Particle interactions described in terms of Feynman diagrams



★ IMPORTANT POINTS TO REMEMBER:

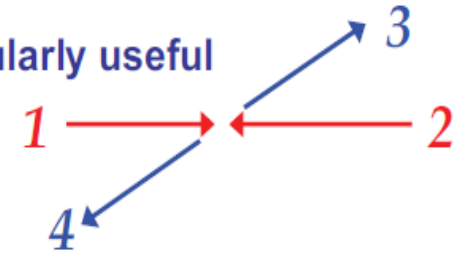
- “time” runs from left - right, **only** in sense that:
 - ♦ LHS of diagram is initial state
 - ♦ RHS of diagram is final state
 - ♦ Middle is “how it happened”
- anti-particle arrows in -ve “time” direction
- Energy, momentum, angular momentum, etc. conserved at **all interaction vertices**
- All intermediate particles are “virtual”
i.e. $E^2 \neq |\vec{p}|^2 + m^2$



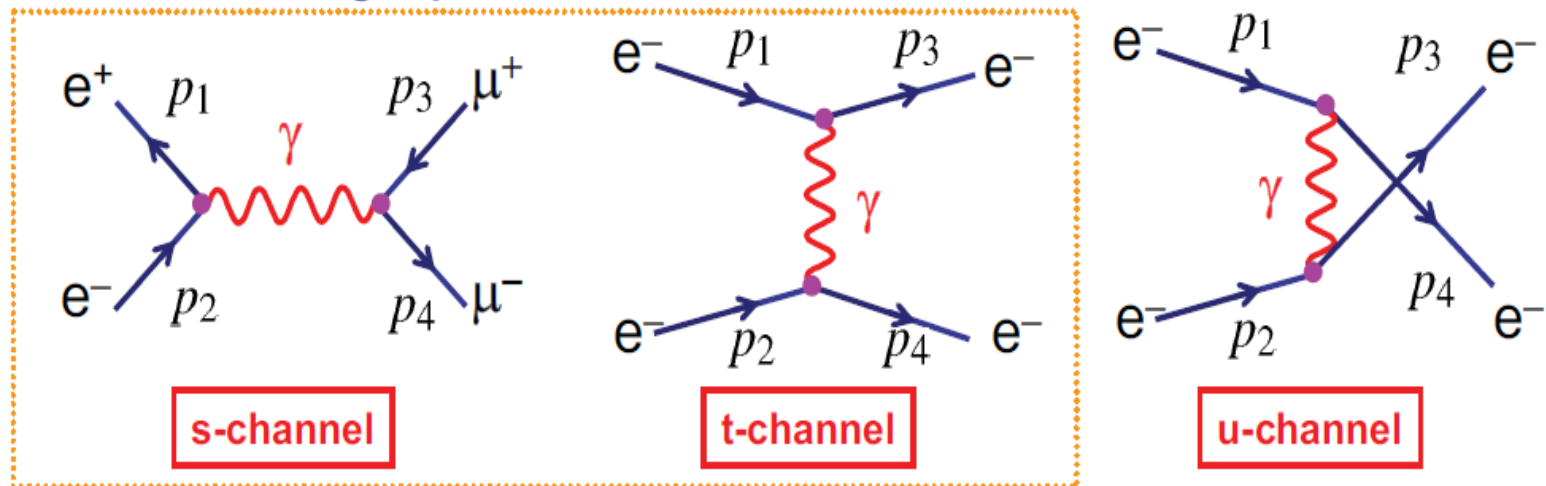
Mandelstam s, t and u

★ In particle scattering/annihilation there are three particularly useful Lorentz Invariant quantities: **s**, **t** and **u**

★ Consider the scattering process $1 + 2 \rightarrow 3 + 4$



★ (Simple) Feynman diagrams can be categorised according to the four-momentum of the exchanged particle

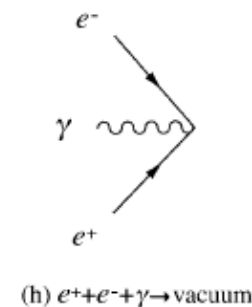
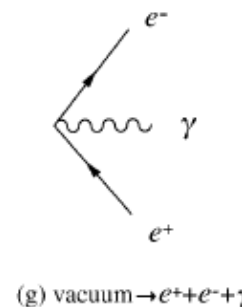
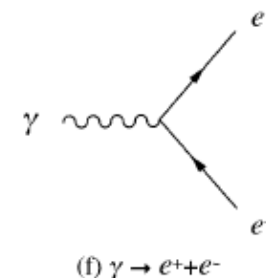
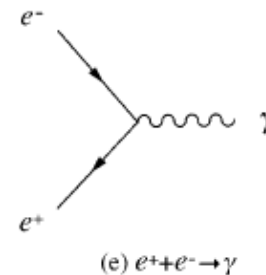
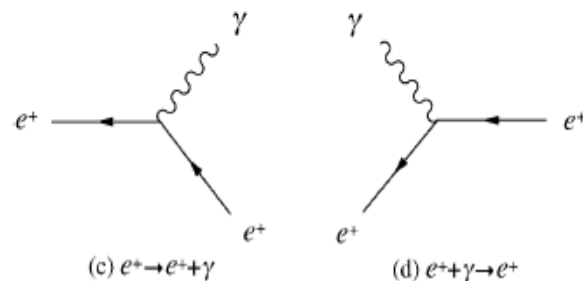
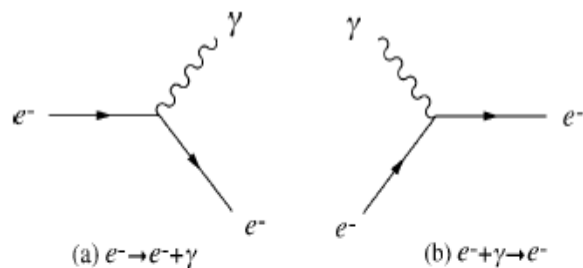


• Can define **three** kinematic variables: **s**, **t** and **u** from the following four vector scalar products (squared four-momentum of exchanged particle)

$$s = (p_1 + p_2)^2, \quad t = (p_1 - p_3)^2, \quad u = (p_1 - p_4)^2$$

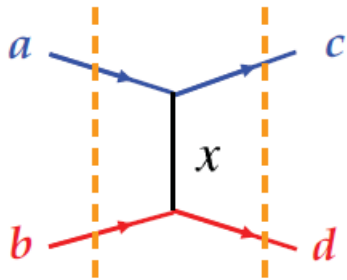
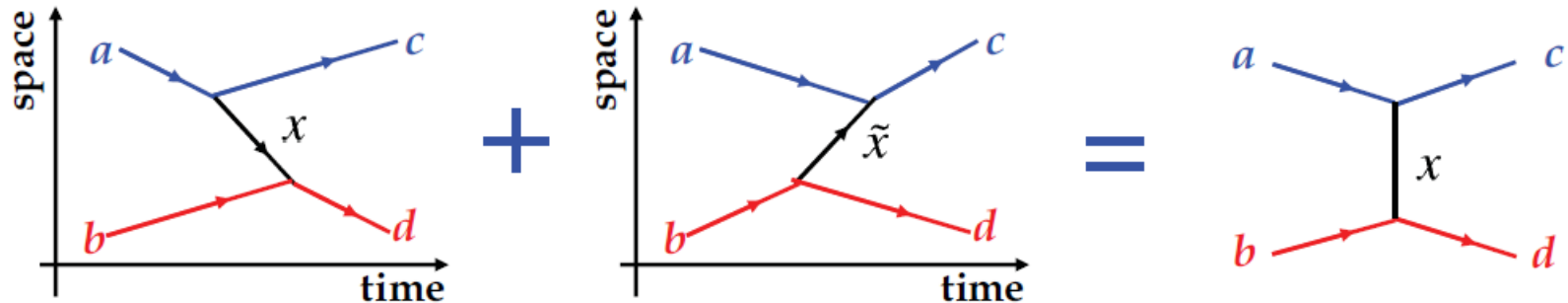
Quantum Electrodynamics (QED)

- The oldest, the simplest and the most successful of the dynamical theories
- All electromagnetic phenomena are ultimately reducible to the following elementary process, where electron either emits or absorbs a photon.



Feynman Rules for QED

- The sum over all possible time-orderings is represented by a **FEYNMAN diagram**



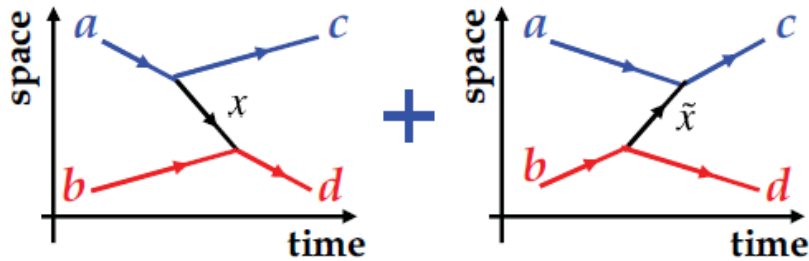
In a Feynman diagram:

- the LHS represents the initial state
- the RHS is the final state
- everything in between is “how the interaction happened”

- It is important to remember that **energy and momentum** are conserved at each interaction vertex in the diagram.
- The factor $1/(q^2 - m_x^2)$ is the propagator; it arises naturally from the above discussion of interaction by particle exchange

Virtual Particles

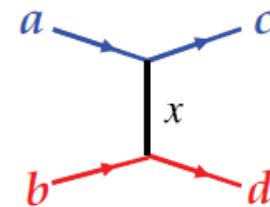
"Time-ordered QM"



- Momentum conserved at vertices
- Energy **not** conserved at vertices
- Exchanged particle **"on mass shell"**

$$E_x^2 - |\vec{p}_x|^2 = m_x^2$$

Feynman diagram



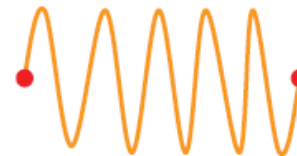
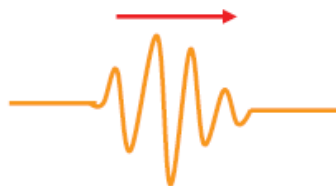
$$M_{fi} = \frac{g_a g_b}{q^2 - m_x^2}$$

- Momentum **AND** energy conserved at interaction vertices
- Exchanged particle **"off mass shell"**

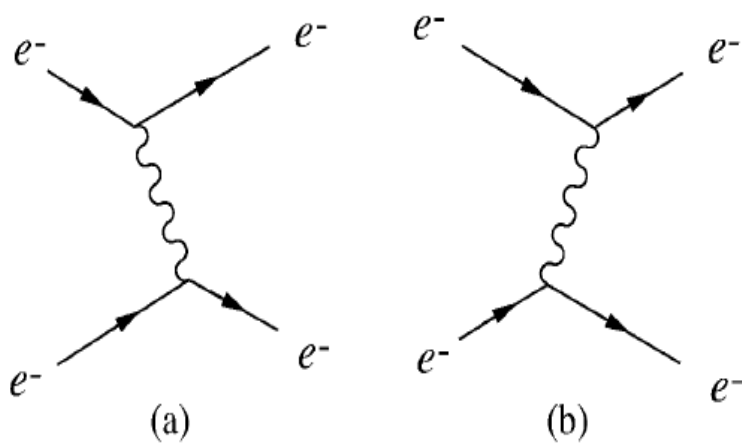
$$E_x^2 - |\vec{p}_x|^2 = q^2 \neq m_x^2$$

VIRTUAL PARTICLE

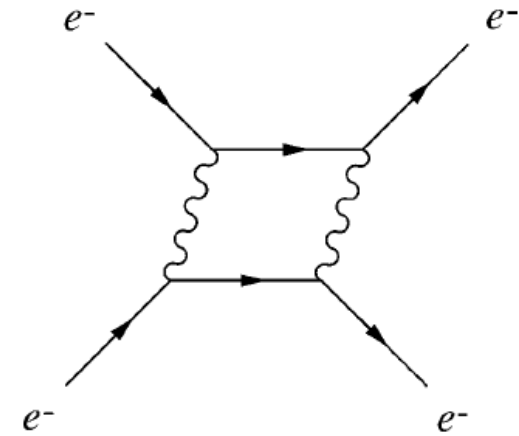
- Can think of observable **"on mass shell"** particles as propagating waves and unobservable virtual particles as normal modes between the source particles:



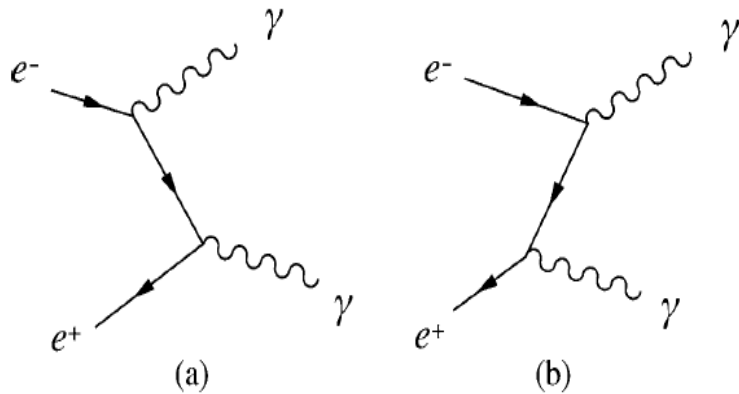
Quantum Electrodynamics (QED)



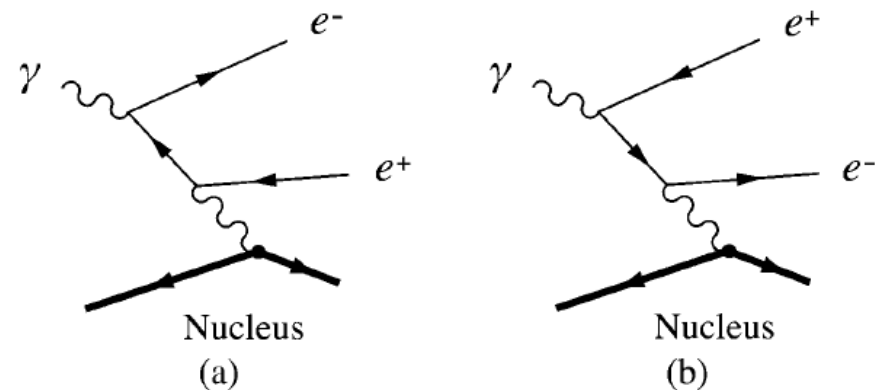
Single photon exchange



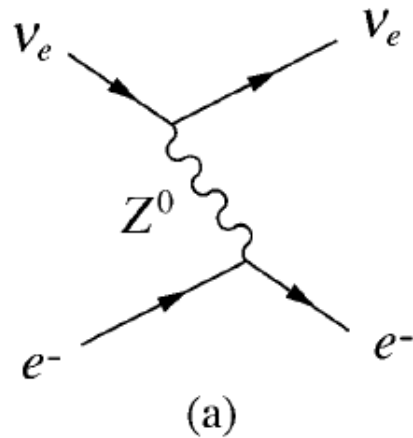
Double photon exchange



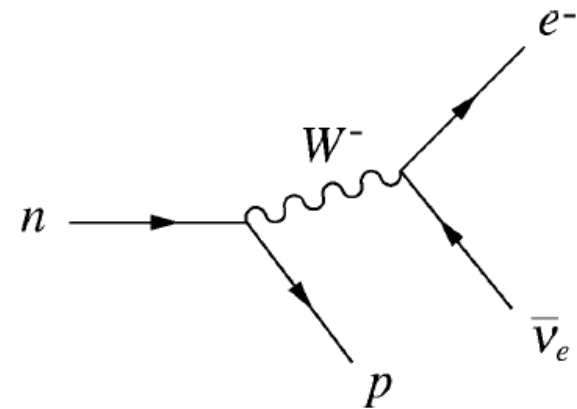
Pair annihilation



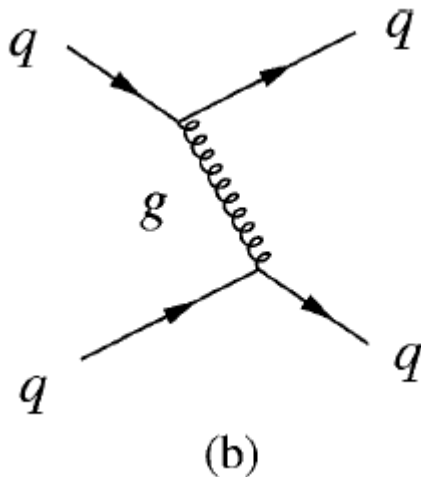
Weak and Strong interactions



Elastic weak scattering



Decay on neutron
via intermediate vector boson



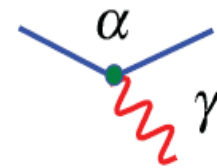
Strong interactions

Colour in QCD

- ★ The theory of the strong interaction, Quantum Chromodynamics (QCD), is very similar to QED but with 3 conserved “colour” charges

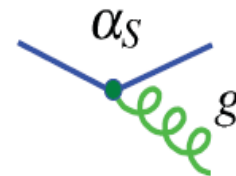
In QED:

- the electron carries one unit of charge $-e$
- the anti-electron carries one unit of anti-charge $+e$
- the force is mediated by a massless “gauge boson” – the photon



In QCD:

- quarks carry colour charge: r, g, b
- anti-quarks carry anti-charge: $\bar{r}, \bar{g}, \bar{b}$
- The force is mediated by massless gluons



- ★ In QCD, the strong interaction is invariant under rotations in colour space

$$r \leftrightarrow b; r \leftrightarrow g; b \leftrightarrow g$$

i.e. the same for all three colours



SU(3) colour symmetry

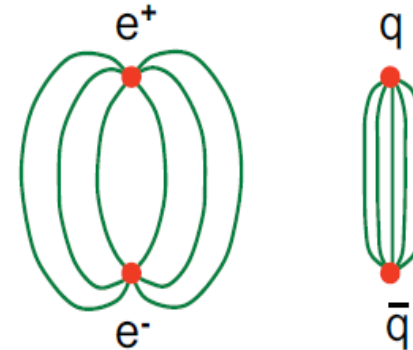
- This is an **exact** symmetry, unlike the approximate uds flavour symmetry discussed previously.

Gluon self-Interactions and confinement

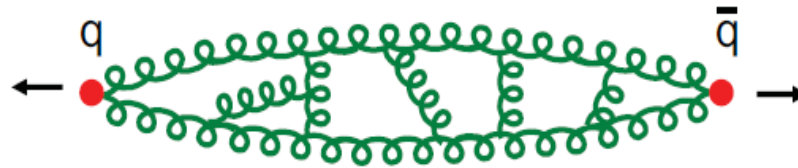
- ★ Gluon self-interactions are believed to give rise to colour confinement

- ★ Qualitative picture:

- Compare QED with QCD
- In QCD “gluon self-interactions squeeze lines of force into a flux tube”



- ★ What happens when try to separate two coloured objects e.g. $q\bar{q}$

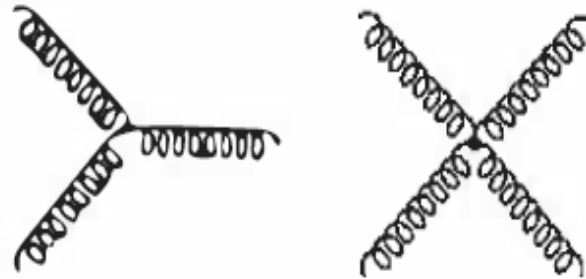


- Form a flux tube of interacting gluons of approximately constant energy density $\sim 1 \text{ GeV/fm}$

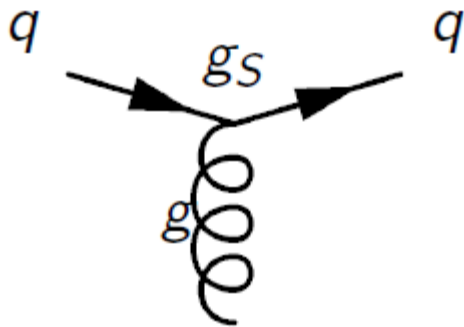
$$\rightarrow V(r) \sim \lambda r$$

- Require infinite energy to separate coloured objects to infinity
- Coloured quarks and gluons are always **confined** within colourless states
- In this way QCD provides a plausible explanation of confinement – but **not yet proven** (although there has been recent progress with Lattice QCD)

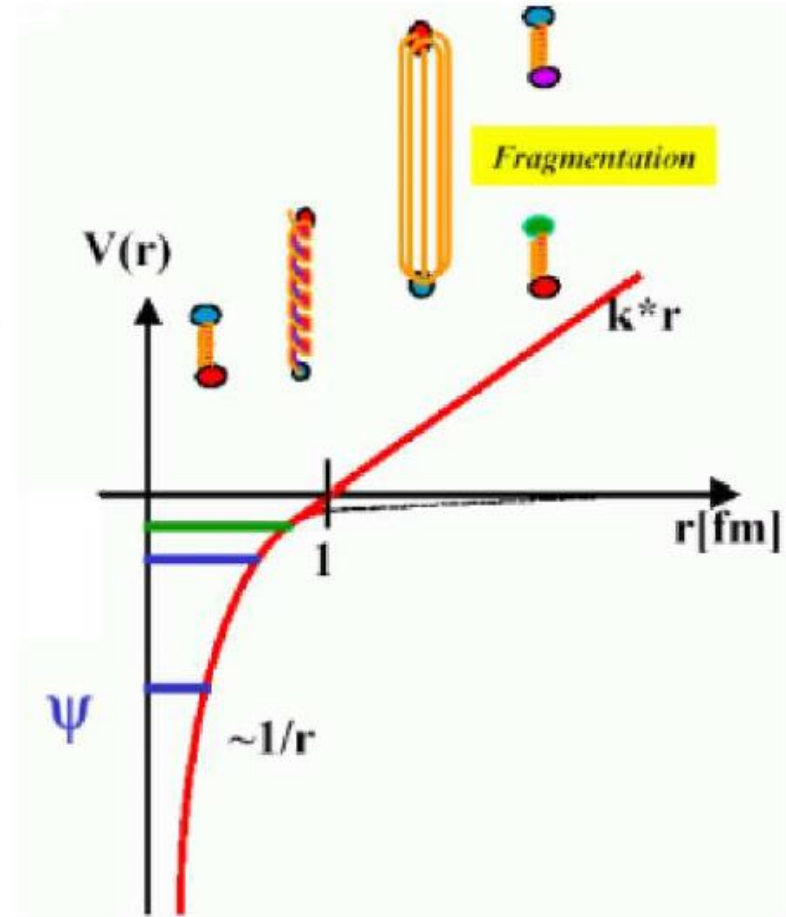
Quantum Chromodynamics



Three-gluon vertices and four-gluon vertices

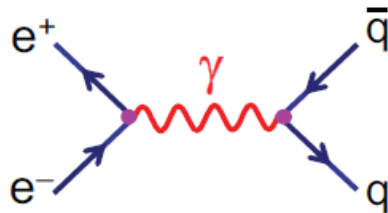


Confinement



QCD and Colour in e^+e^- Collisions

★ e^+e^- colliders are an excellent place to study QCD



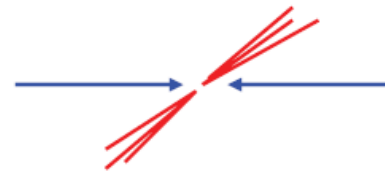
★ Well defined production of quarks

- QED process well-understood
- no need to know parton structure functions
- + experimentally very clean - no proton remnants

★ expressions for the $e^+e^- \rightarrow \mu^+\mu^-$ cross-section

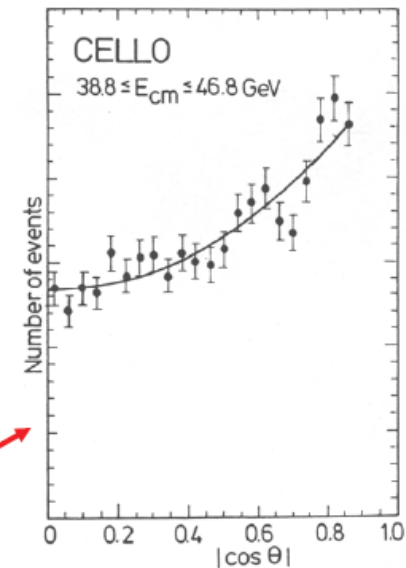
$$\sigma = \frac{4\pi\alpha^2}{3s} \quad \frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4s} (1 + \cos^2 \theta)$$

- In e^+e^- collisions produce all quark flavours for which $\sqrt{s} > 2m_q$
- In general, i.e. unless producing a $q\bar{q}$ bound state, produce jets of hadrons
- Usually can't tell which jet came from the quark and came from anti-quark



★ Angular distribution of jets $\propto (1 + \cos^2 \theta)$

→ Quarks are spin $\frac{1}{2}$



H.J.Behrend et al., Phys Lett 183B (1987) 400

Jet production in e^+e^- collision

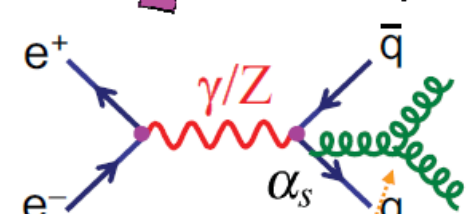
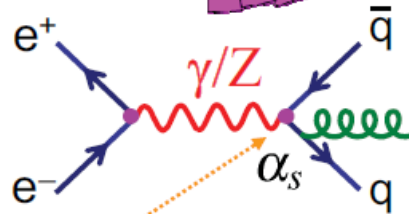
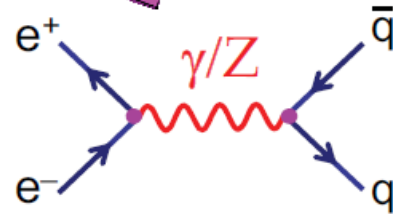
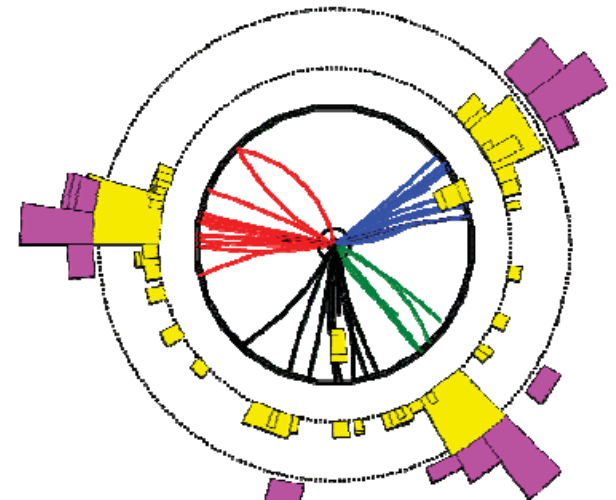
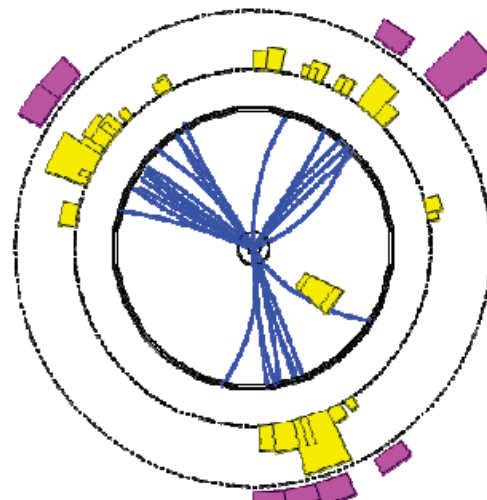
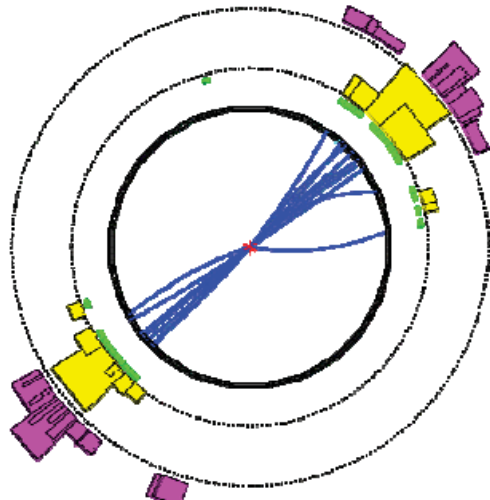
★ e^+e^- colliders are also a good place to study gluons

$$e^+e^- \rightarrow q\bar{q} \rightarrow 2\text{jets}$$

$$e^+e^- \rightarrow q\bar{q}g \rightarrow 3\text{jets}$$

$$e^+e^- \rightarrow q\bar{q}gg \rightarrow 4\text{jets}$$

OPAL at LEP (1989-2000)



Experimentally:

- Three jet rate \rightarrow measurement of α_s
- Angular distributions \rightarrow gluons are spin-1
- Four-jet rate and distributions \rightarrow QCD has an underlying SU(3) symmetry

Weak interaction in quark sector

- ★ Extend ideas to three quark flavours

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

By convention CKM matrix defined as acting on quarks with charge $-\frac{1}{3}e$

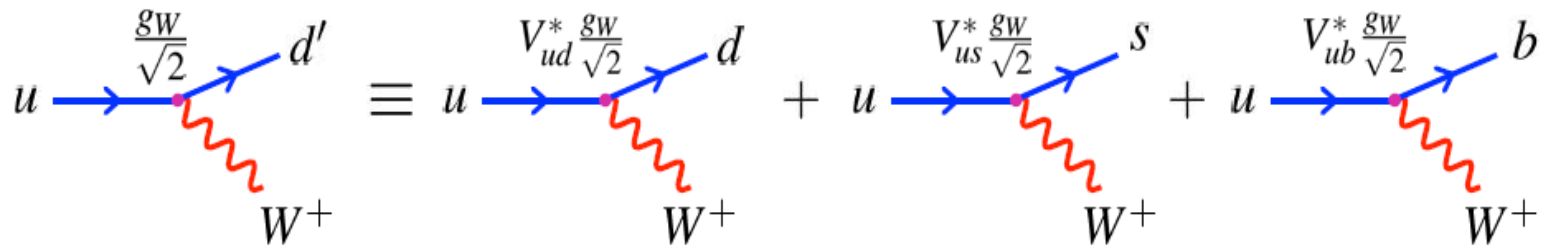
Weak eigenstates

CKM Matrix

Mass Eigenstates

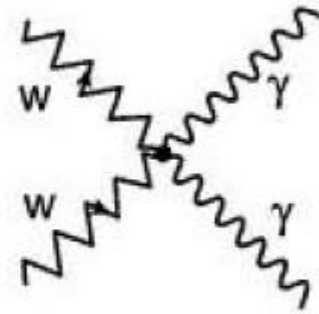
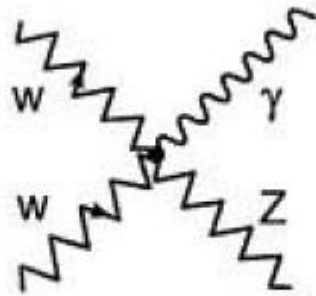
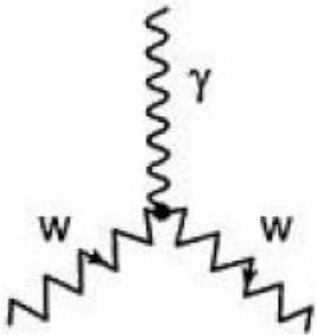
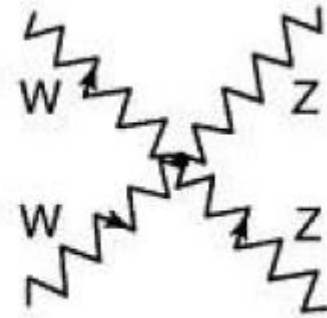
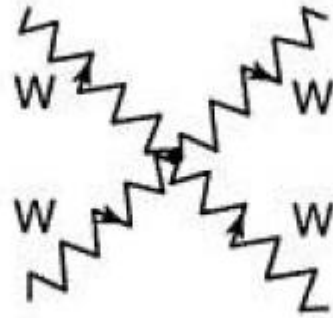
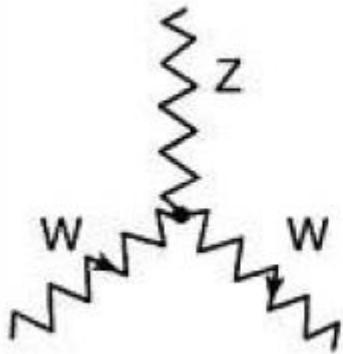
(Cabibbo, Kobayashi, Maskawa)

- ★ e.g. Weak eigenstate d' is produced in weak decay of an up quark:

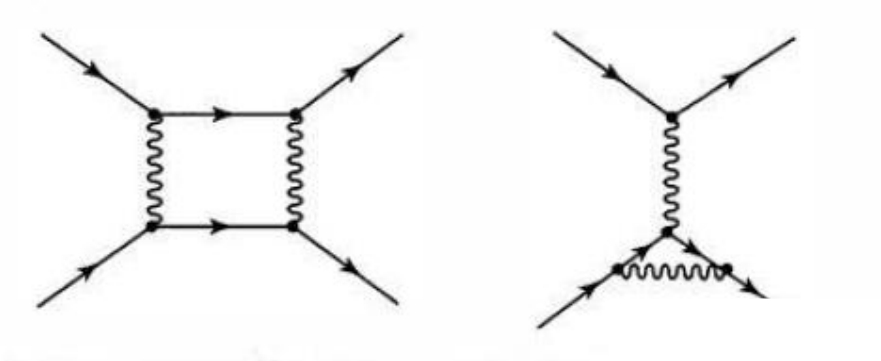


- The CKM matrix elements V_{ij} are **complex constants**
- The CKM matrix is **unitary**
- The V_{ij} are not predicted by the SM – have to **determined from experiment**

Weak and Electromagnetic Couplings

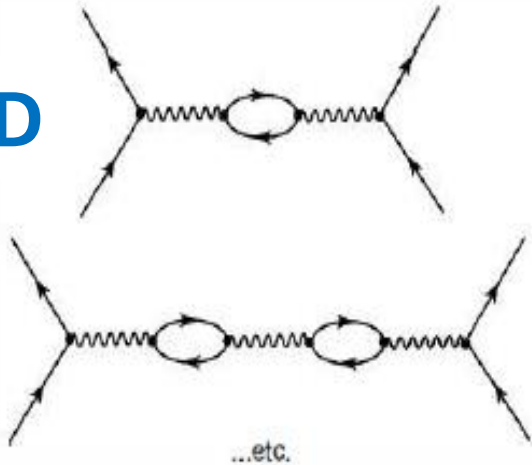


Loops

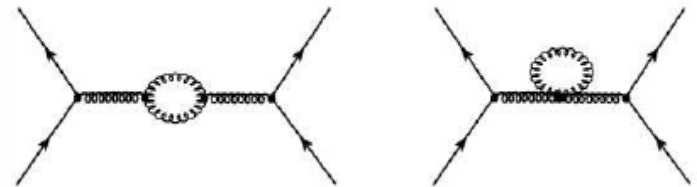


Virtual corrections
and box diagrams

QED

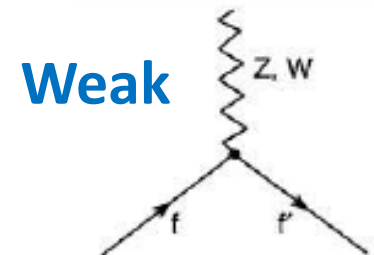
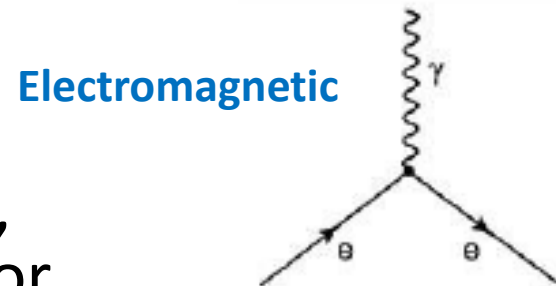
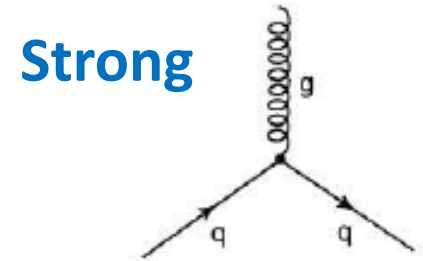


QCD



Conservation laws

- **Charge:** all three interactions conserve electric charge
- **Color:** the electromagnetic and weak interactions do not affect color. At strong vertex color change but difference carried by the gluon.
- **Baryon number:** conserved in all simple vertices
- **Lepton number:** is absolutely conserved, cross-generation mixing in neutrino sector (oscillation)
- **Flavour:** conserved at strong and electromagnetic vertex but not weak vertex



Grand unification

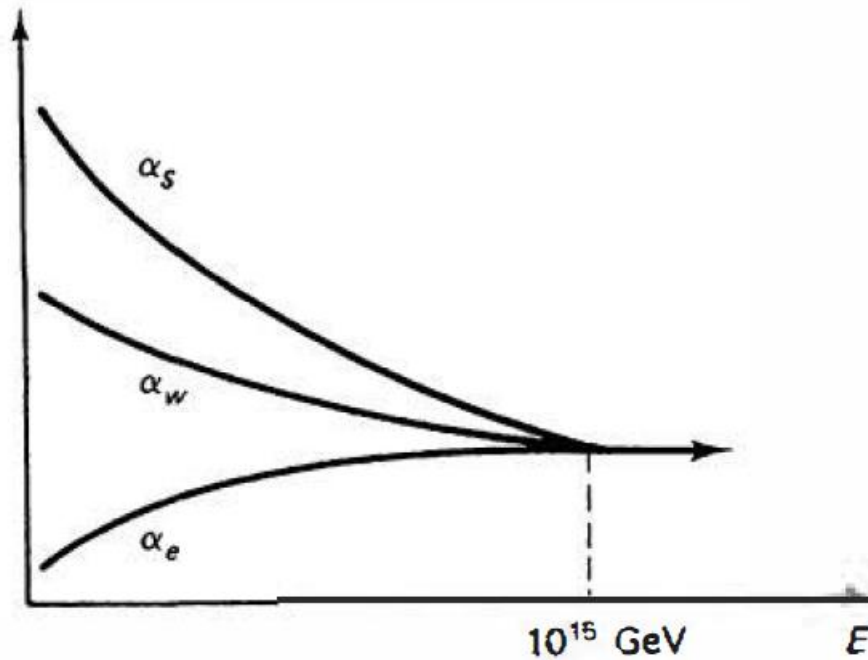
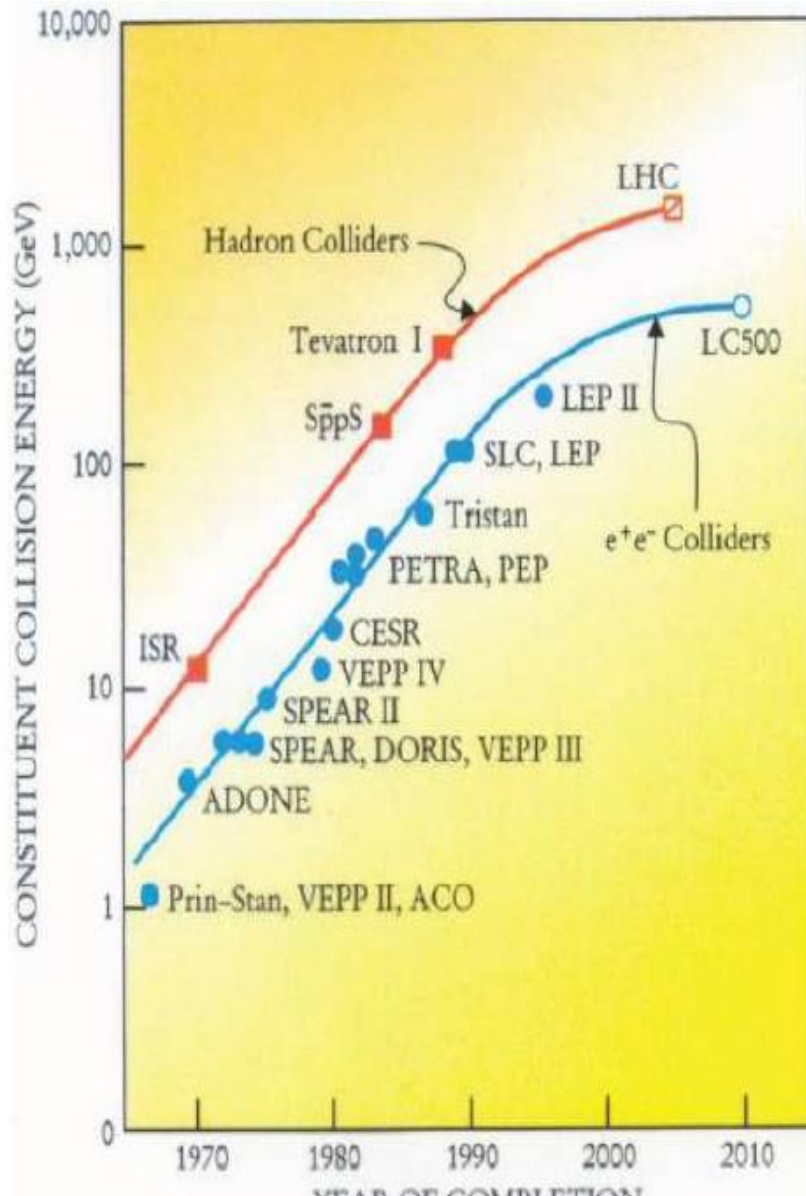


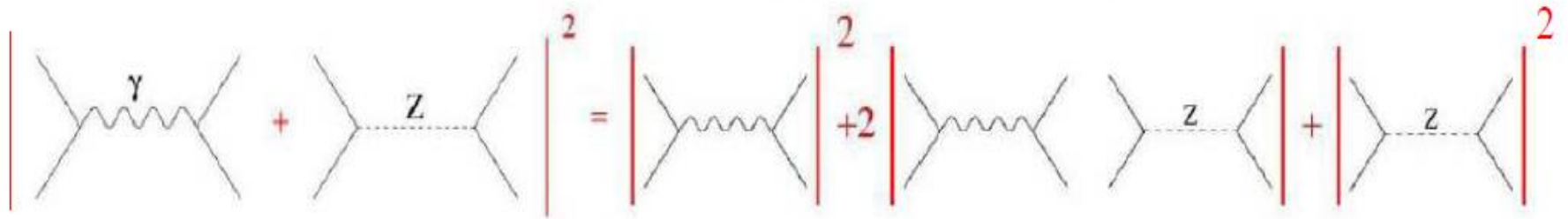
Fig. 2.5 Evolution of the three fundamental coupling constants.

Energy frontier



- The interplay between electron and hadron machines has a long and fruitful tradition
 - J/ψ at SPEAR (e^+e^-) and AGS (proton fixed target)
 - Υ discovery at E288 (p fixed target), precision B studies at the e^+e^- B factories
 - ...
 - top quark at LEP and Tevatron
- To be continued in the form of LHC and ILC

$e^+ e^- \rightarrow Z$ cross-section



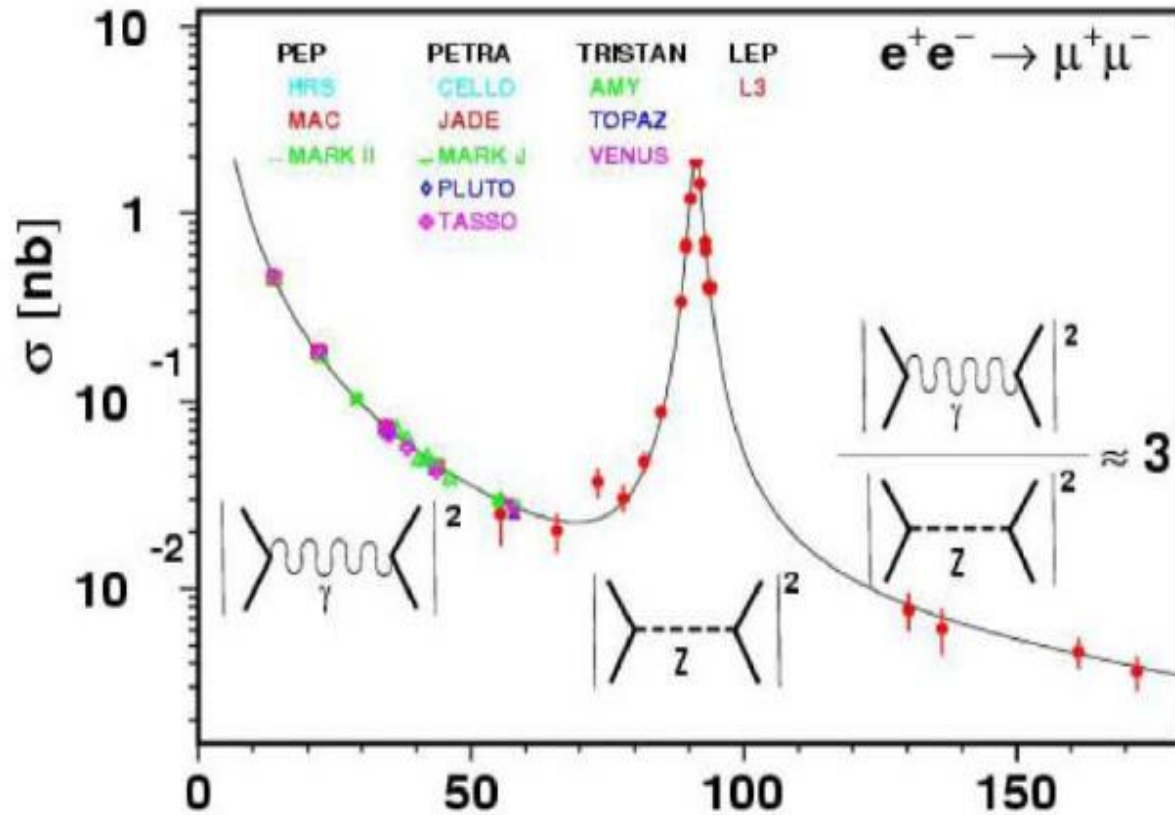
$$\frac{d\sigma}{d\Omega} = N_C \frac{\alpha_{em}^2}{4s} \left\{ (1 + \cos^2 \theta) [Q_f^2 - 2\chi_1 v_e v_f Q_f - \chi_2 (a_e^2 + v_e^2)(a_f^2 + v_f^2)] + 2 \cos \theta [-2\chi_1 a_e a_f Q_f + 4\chi_2 a_e a_f v_e v_f] \right\}$$

$$\chi_1 = \frac{s(s - M_Z^2)}{16 \sin^2 \theta_W \cos^2 \theta_W ((s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2) s^2}$$

$$\chi_2 = \frac{s(s - M_Z^2)}{256 \sin^4 \theta_W \cos^4 \theta_W ((s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2)}$$

$$a_e = -1; \quad v_e = -1 + 4 \sin^2 \theta_W; \quad a_f = 2I_f; \quad v_f = 2I_f - 4Q_f \sin^2 \theta_W$$

$e^+ e^- \rightarrow Z$ cross-section



Complementarity between pp and ee machines



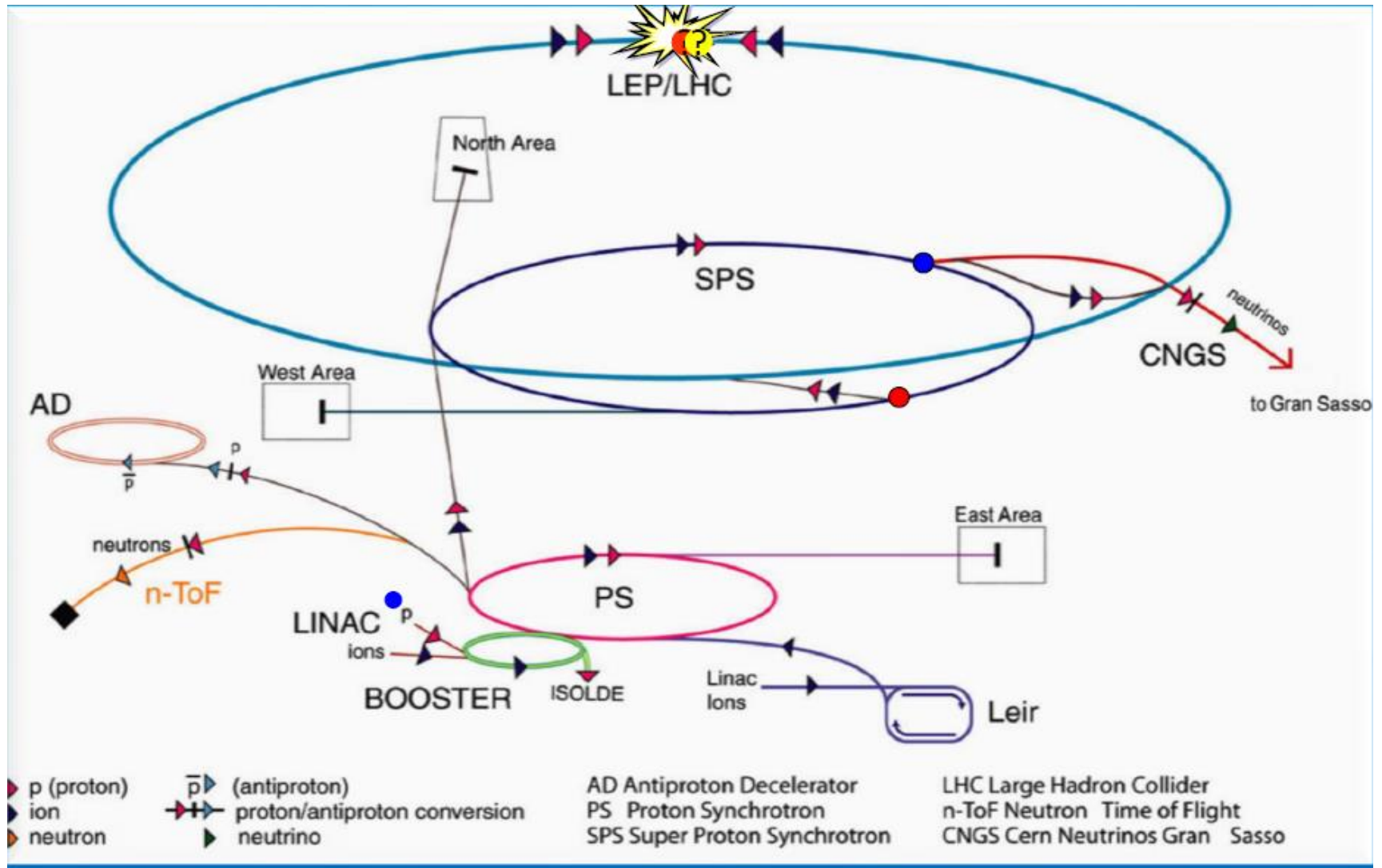
- Proton-(Anti-)Proton Colliders

- Higher energy reach (limited by magnets)
- Composite particles: unknown and different colliding constituents, energies in each collision
- Confusing final states
- Discovery machines (W , Z , t)
- In some cases: precision measurements possible (W mass at the Tevatron)

- Electron-Positron-Colliders

- Energy reach limited by RF
- Point like particles, exactly defined initial system, quantum numbers, energy, spin polarisation possible
- Hadronic final states with clear signatures
- Precision machines
- Discovery potential, but not at the energy frontier

CERN accelerator complex



Luminosity frontier

- Need corresponding rise in luminosity (beam intensity)

$$N = \sigma L = \sigma \int \mathcal{L} dt$$

Number of events
Instantaneous luminosity

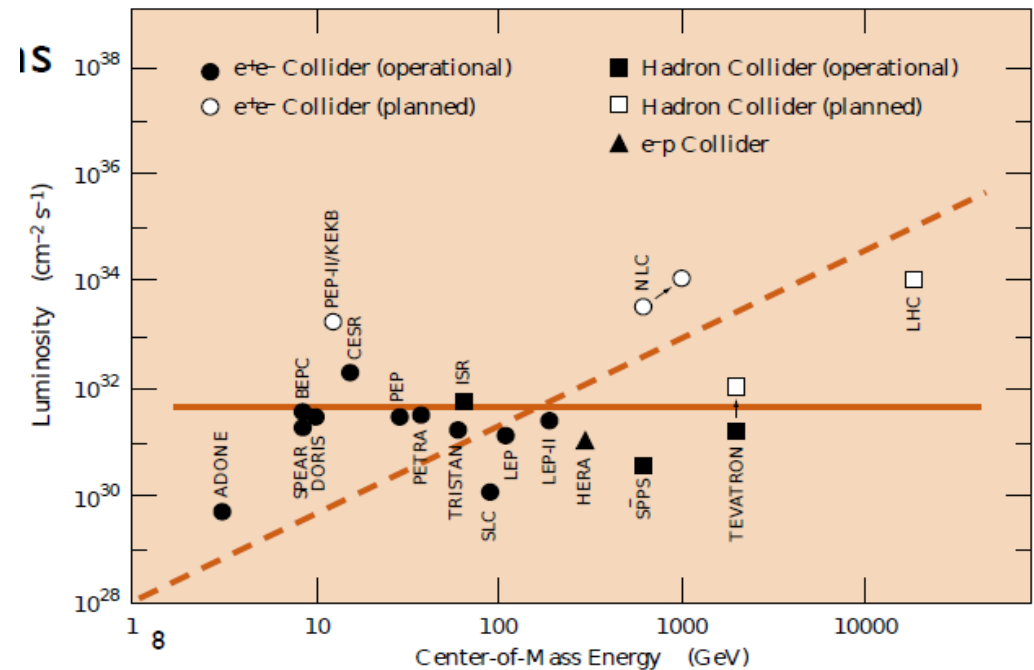
↓
↓

↑
↑

Cross section
Integrated luminosity

- High luminosity brings all the challenges for the detectors:

- High event rates
- Pile up
- Beam –beam interactions
- Beamstrahlung



Designing a machine

- Particle species
 - Electron/positrons
 - Protons/antiprotons
 - Muons/antimuons
- Beam energy
- Spin
- Luminosity
- How do you produce antiparticles?
- Ones produced how ones keep them (muon collider)?
- Ones collided what ones does with spent beams?
- Accelerator and detector protection

Accelerator is much more than just....

- Particle production
- Damping, cooling or preparation
- Injection and extraction
- Acceleration
- Collimation (betatron, energy etc.)
- Diagnostics and controls
- Machine (and detector protection)
- Beam delivery and luminosity production
- Technology spin off
 - Lower energy machines, medical applications, applied physics, materials,

Acceleration

Lorentz force law

$$\mathbf{F} = q (\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

Electric field Velocity Magnetic field

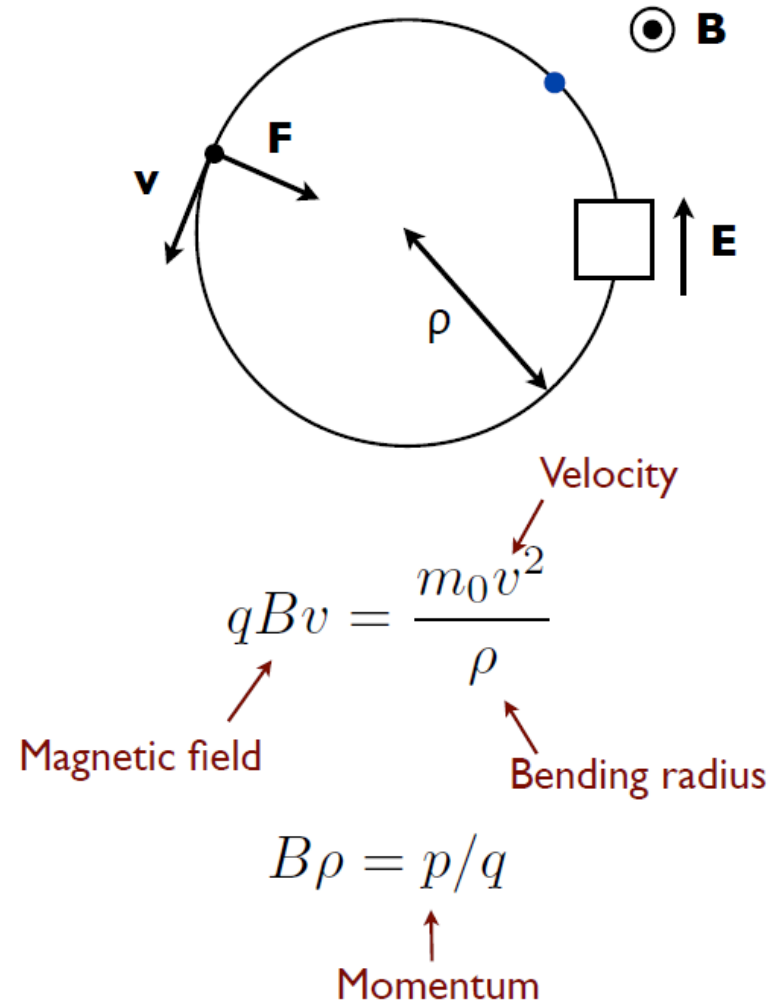
Energy change

$$\Delta E = \int_{\mathbf{r}_1}^{\mathbf{r}_2} \mathbf{F} \cdot d\mathbf{r}$$

- Electric field (either static or more commonly, time varying) to accelerate, or more appropriately, increase energy of beam
- Magnetic part of Lorentz force used to guide and focus
 - Dipole magnets: to bend
 - Quadrupole: to focus or defocus

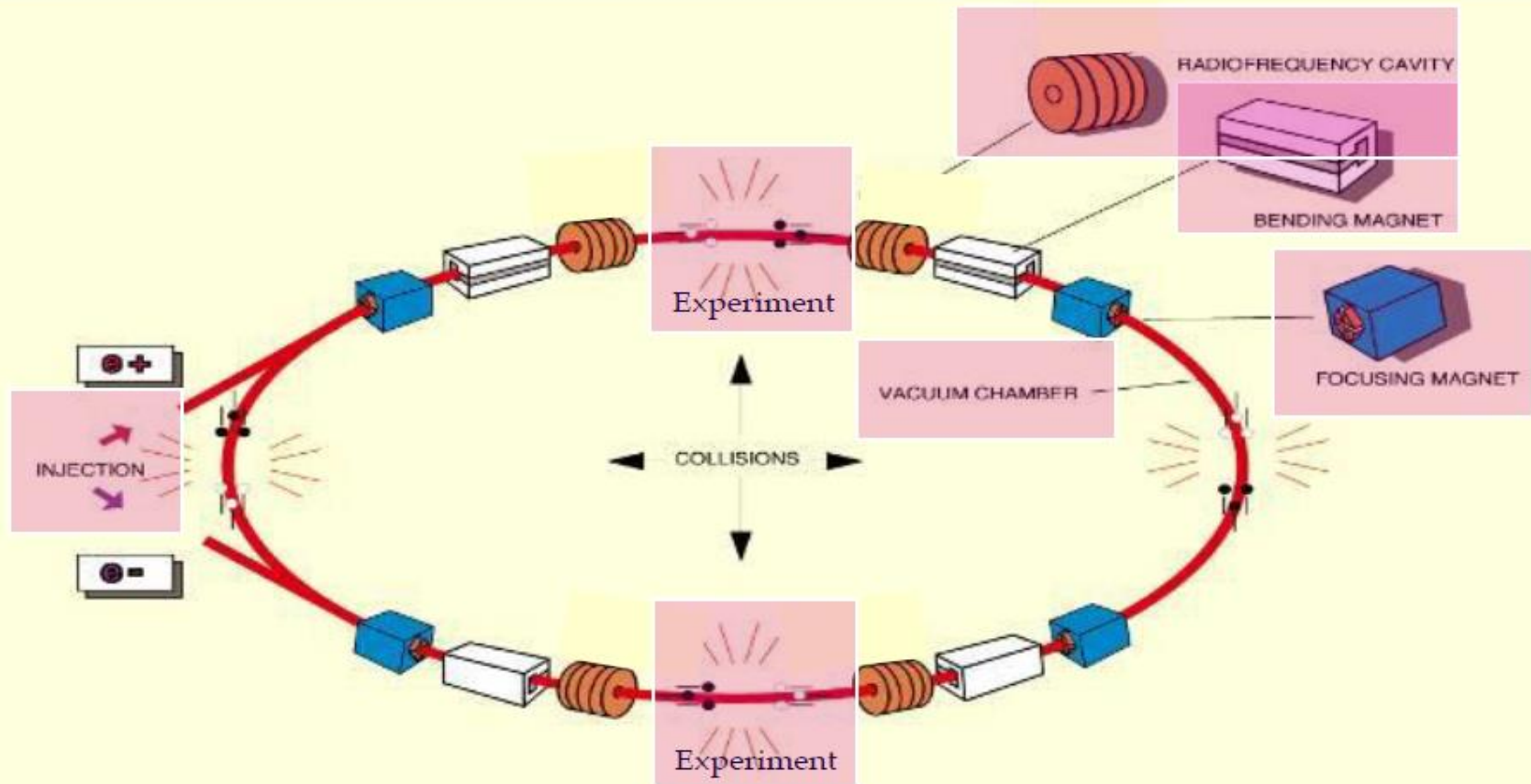
Synchrotron

- Workhorse of modern particle physics
 - Huge legacy of discovery
 - Increase energy whilst synchronously increasing bending magnet strength
 - Stable storage of high beam current/power
- Magnetic field proportional to momentum

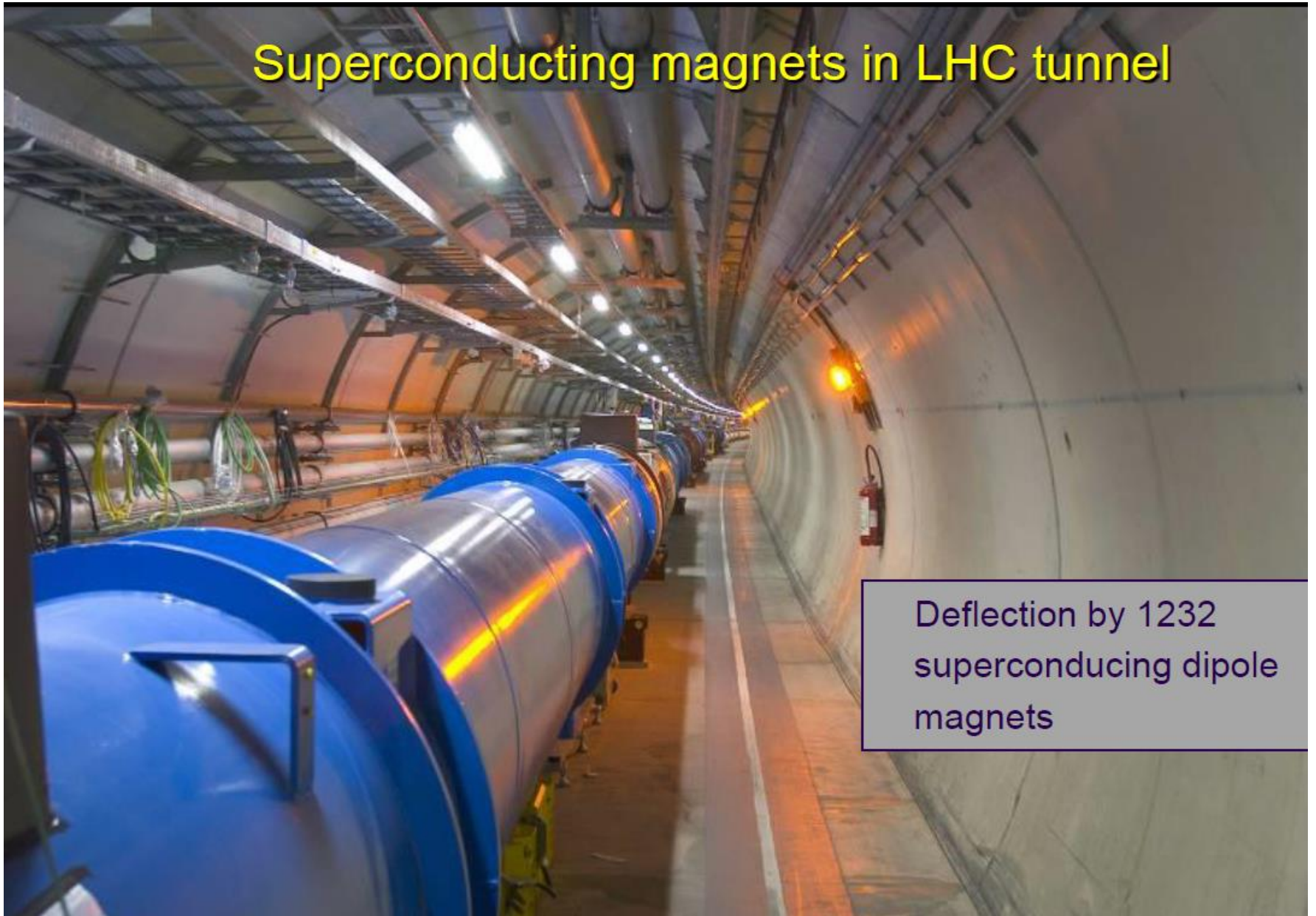


Synchrotron + many passages in RF cavities

LHC **circular machine** with energy gain per turn ~ 0.5 MeV
acceleration from 450 GeV to 7 TeV will take about 20 minutes

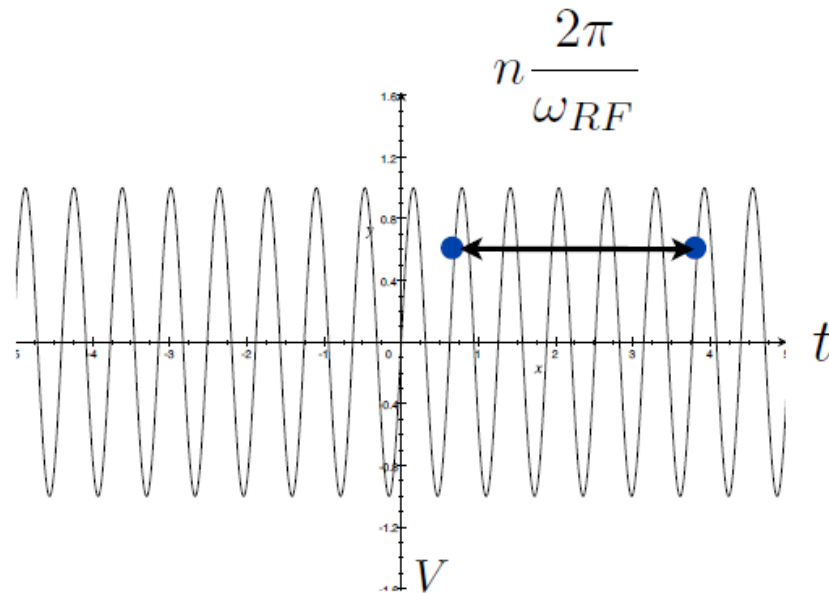
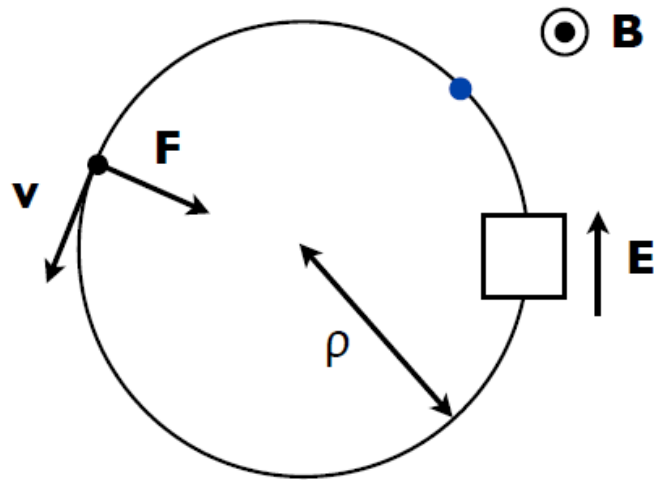


Superconducting magnets in LHC tunnel



Deflection by 1232
superconducting dipole
magnets

Synchrotron



- Time varying electric field:

$$V(t) = V_0 \sin(\omega_{RF}t + \phi)$$

↑
Angular frequency of
accelerating field

- Particle gets a kick every revolution

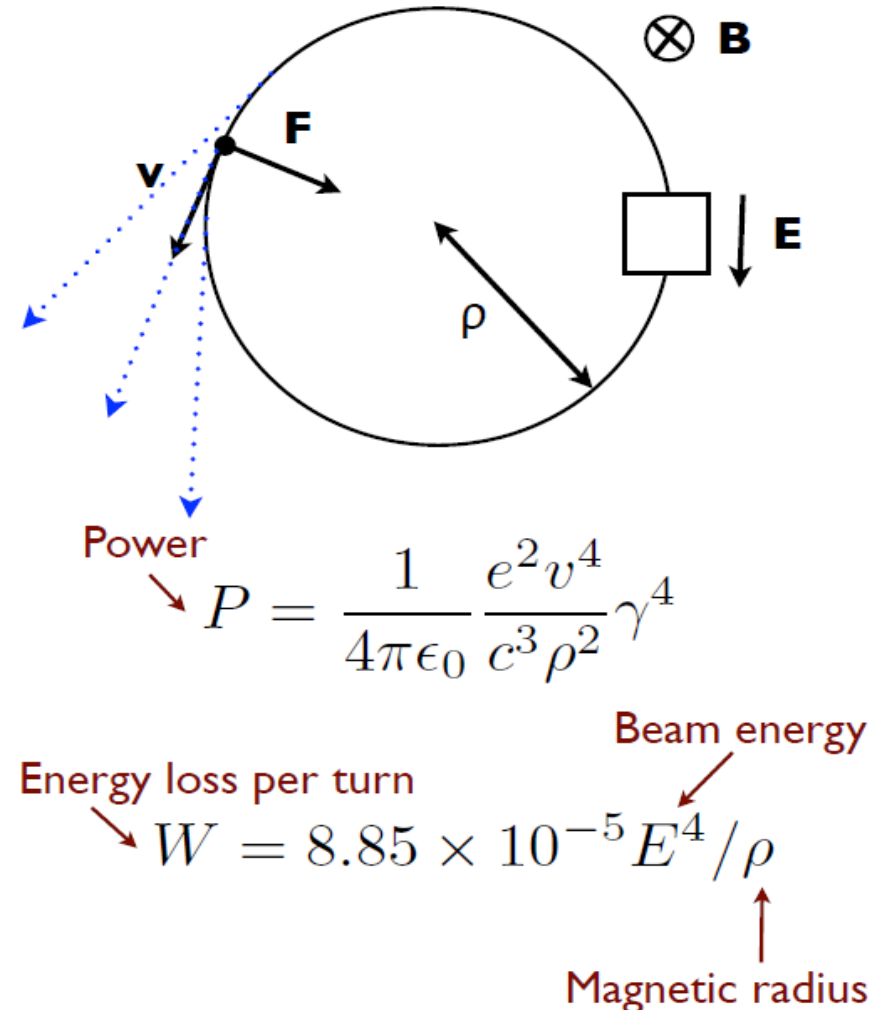
$$\frac{1}{f_{\text{ref}}} = n \frac{2\pi}{\omega_{RF}}$$

↑
Revolution
frequency

↑
Integer

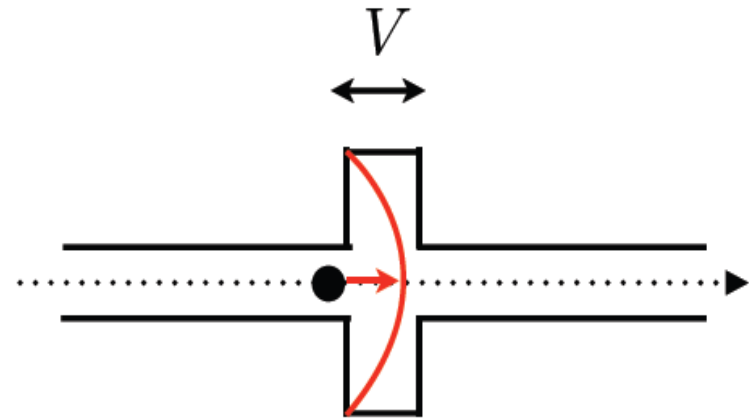
Synchrotron Radiation Limits

- Why not just build bigger LEP?
- Reuse accelerating section every revolution of particle bunch
- Power loss due to synchrotron radiation
- LEP2 was practical limit for electron-positron synchrotron



Absolute Limits on Acceleration

- Need to create large on axis electric fields
- Accelerating structures:
 - Superconducting (~35 MV/m)
 - Normal conducting (~100 MV/m)
- Beyond these values there is high voltage breakdown

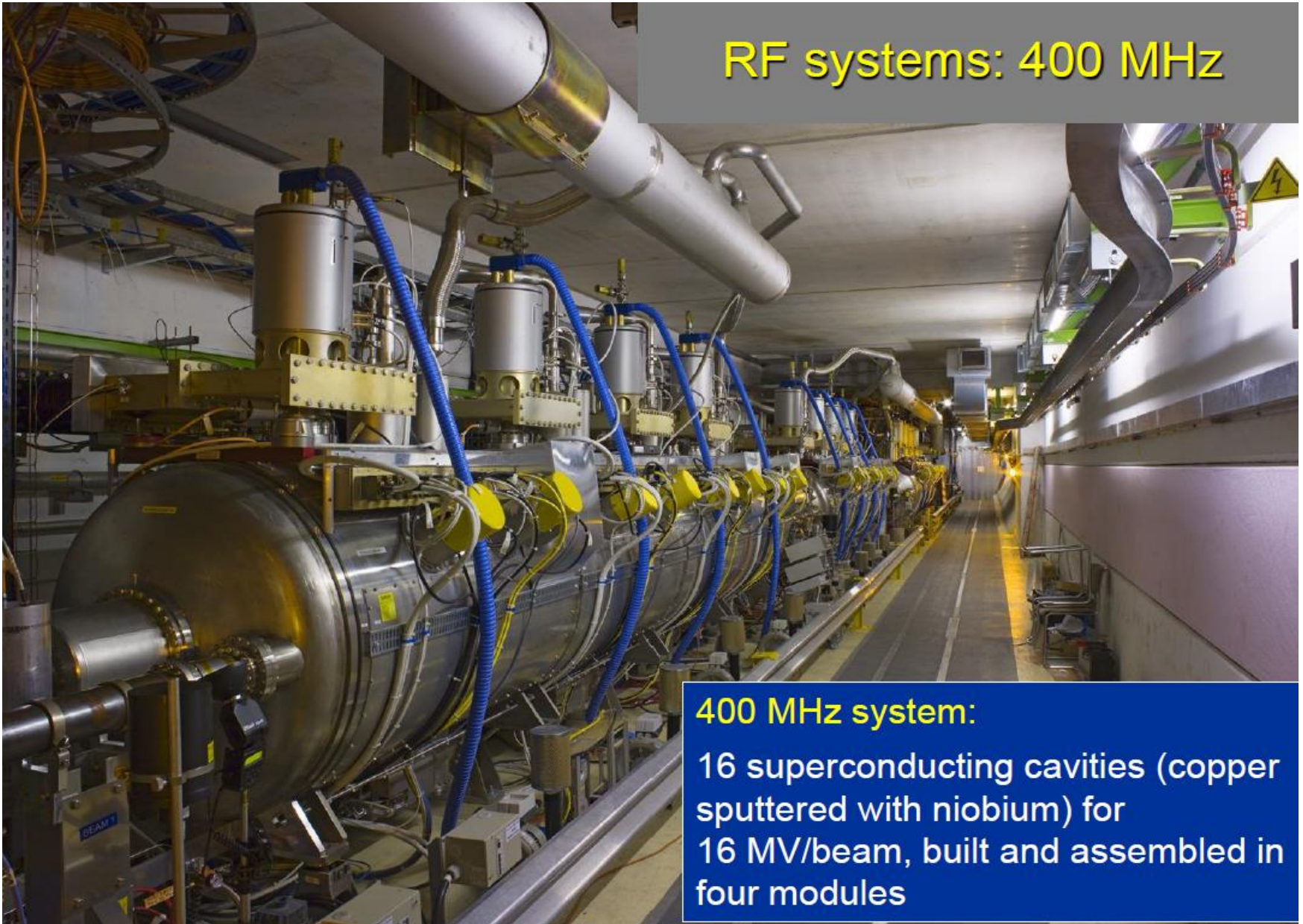


$$S = \frac{E}{q \frac{dV}{ds}}$$

Machine length [m] Beam energy [MeV]

↑
Accelerating gradient [MV/m]

RF systems: 400 MHz

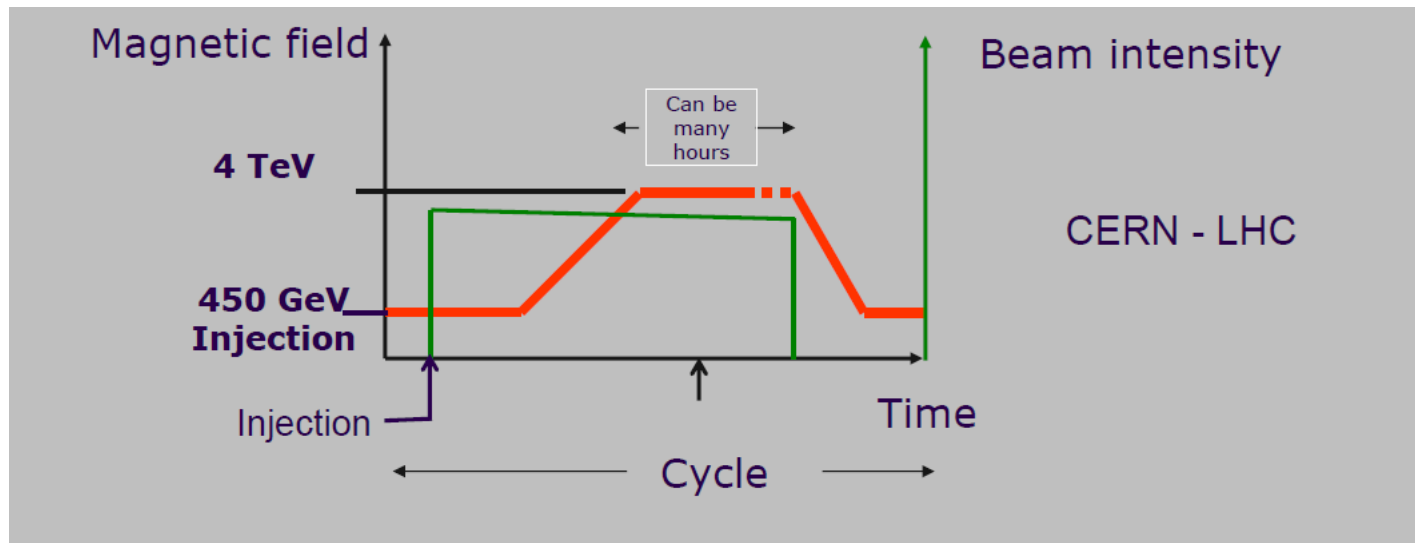


400 MHz system:

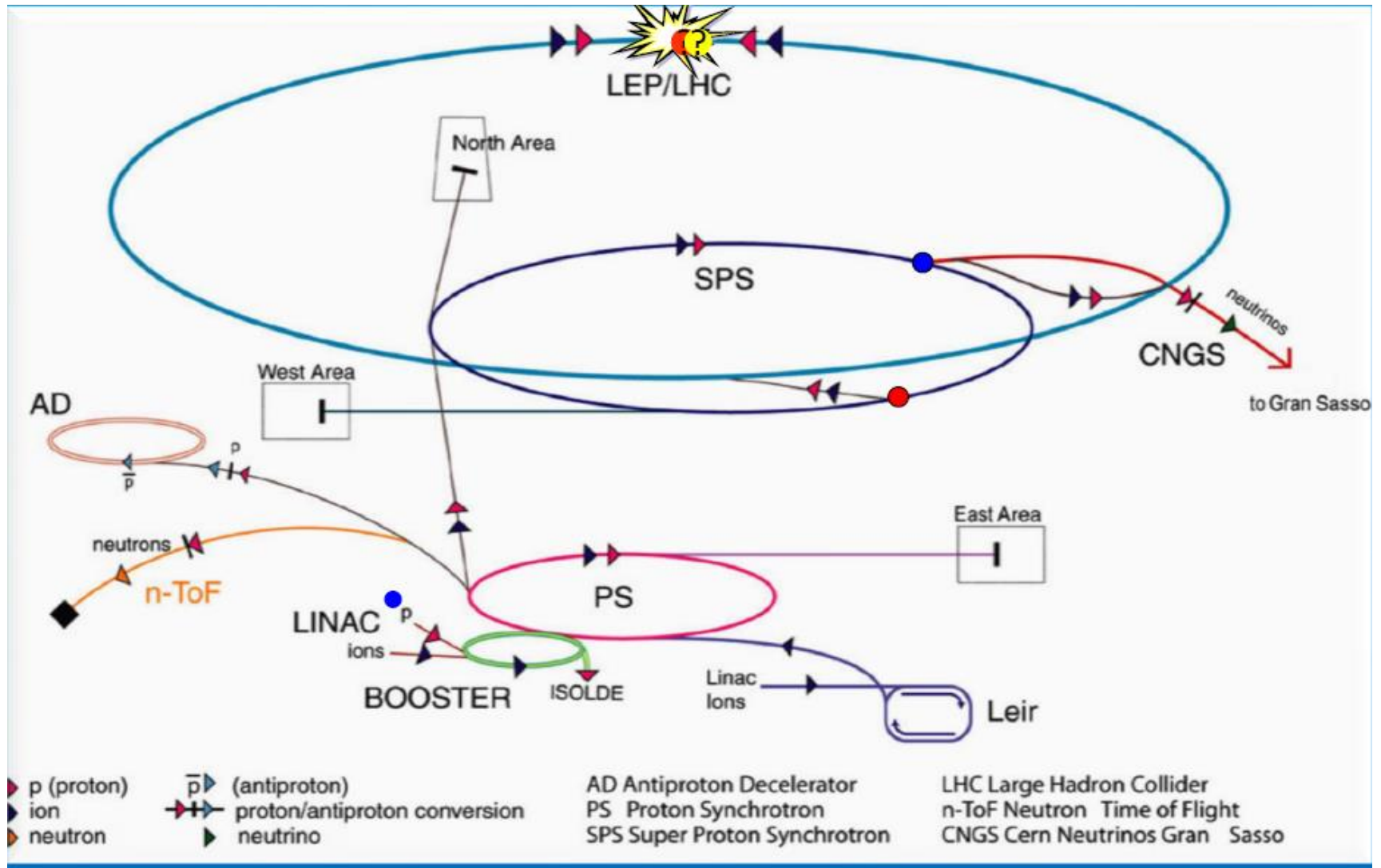
16 superconducting cavities (copper sputtered with niobium) for 16 MV/beam, built and assembled in four modules

Principle of a synchrotron

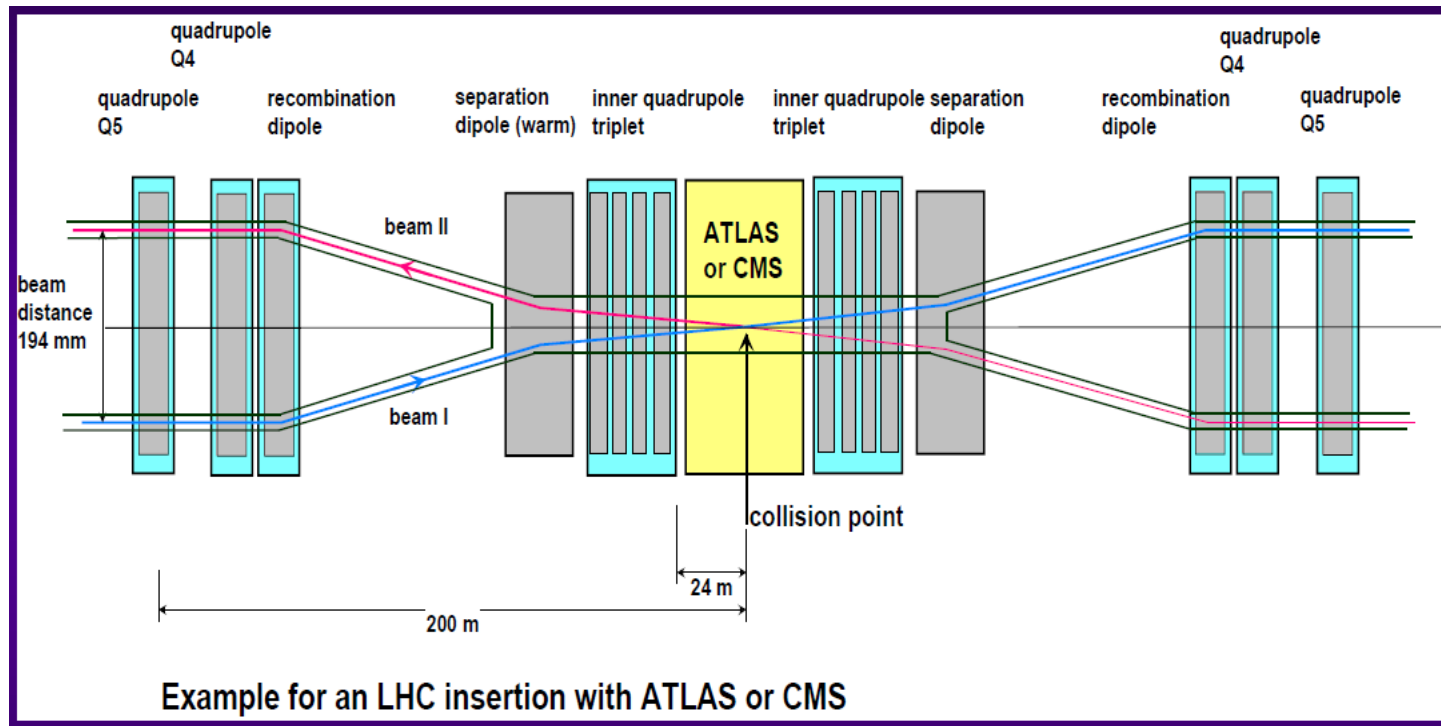
- Injection at low energy
- Ramping of magnetic field and acceleration by RF field. Beams are accelerated in bunches
- Operation (collisions) at top energy



CERN accelerator complex



Experimental long straight section



The 2 LHC beams are brought together to collide in common region. Over $\sim 260\text{m}$ the beams circulate in one vacuum chamber with „parasitic” encounters.

The crossing angle of about $300\mu\text{rad}$

Luminosity

- What luminosity is required for measurement?
- Need some knowledge of x-section
- Simple relationship between number of particles, frequency of collision and beam sizes

Diagram illustrating the relationship between Luminosity, Bunch populations, Frequency of collisions, and Beam r.m.s. sizes:

$$\mathcal{L} = f \frac{N_1 N_2}{4\pi\sigma_x\sigma_y}$$

Labels and arrows:

- Luminosity [$s^{-1} m^{-2}$] points to \mathcal{L}
- Bunch populations points to $N_1 N_2$
- Frequency of collisions [Hz] points to f
- Beam r.m.s. sizes [m] points to $\sigma_x \sigma_y$

$$\sigma = \sqrt{\epsilon\beta}$$

Labels and arrows:

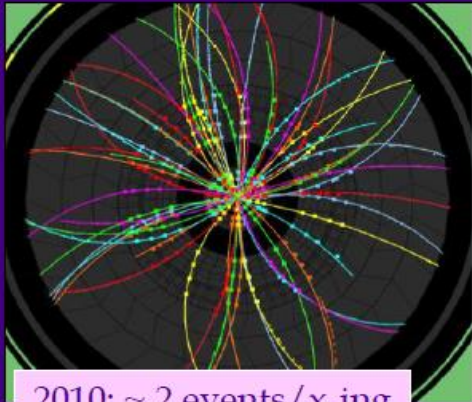
- Emittance [m] points to ϵ
- Beta function [m] points to β

$$\mathcal{L} = f \frac{N_1 N_2}{4\pi \sqrt{\epsilon_x \beta_x^* \epsilon_y \beta_y^*}}$$

CMS

E
CMS Experiment at LHC, CERN
Data recorded: Mon May 28 01:16:20 2012 CERN
Run/Event: 195099 / 35488125
Lumi Section: 65
Orbit/Crossing: 16992111 / 2295

- ⇒ With the parameters of 2012 for each bunch crossing there are up to ~35 interactions (lower luminosity, less number of bunches)
- ⇒ 'Hats off' to ATLAS & CMS for handling this pile-up !!



2010: ~ 2 events/x-ing

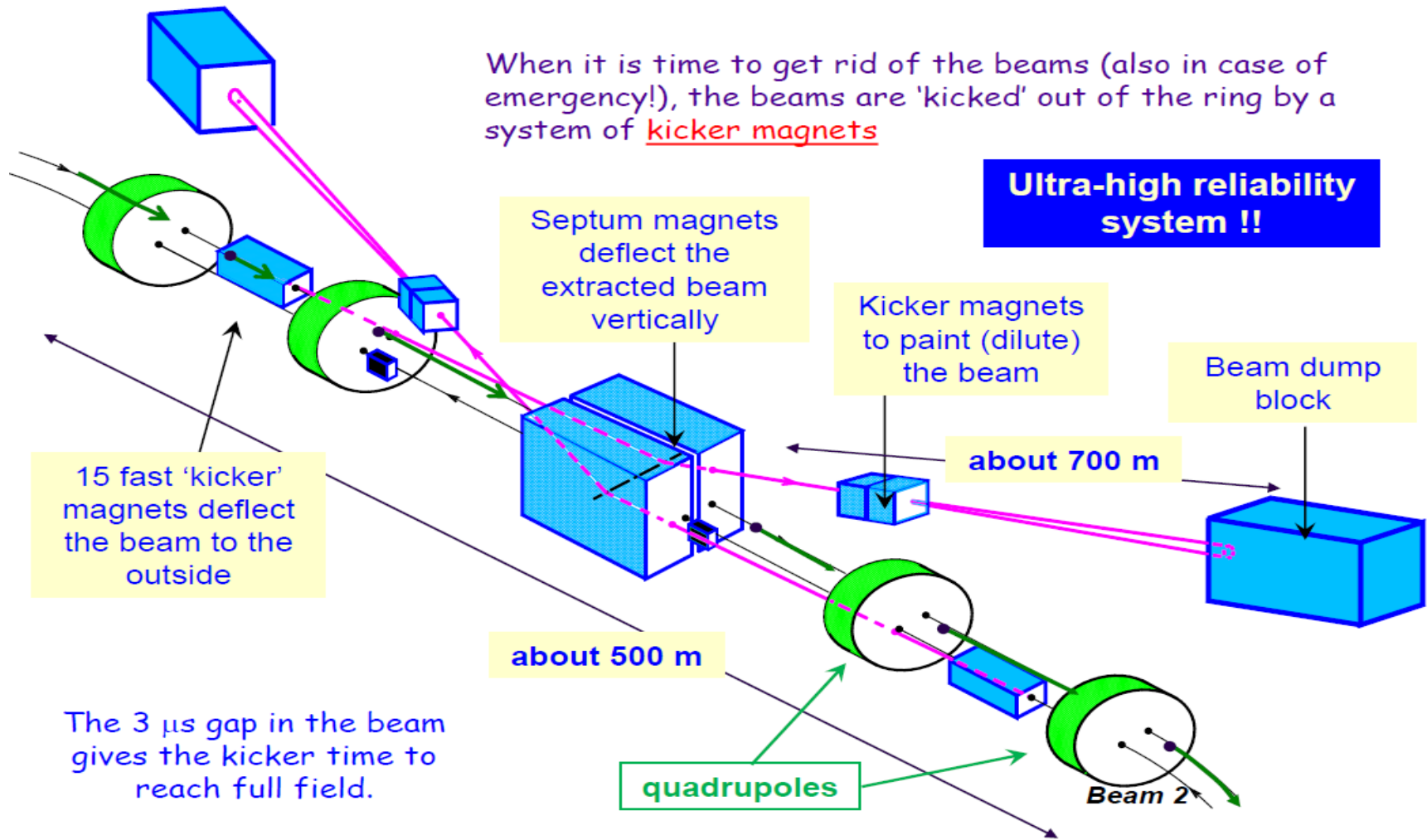


2011: ~ 10 events/x-ing



2012: ~ 20 events/x-ing

Layout of beam system dump



Dump line



Beam Loss Monitors

- Ionization chambers to detect beam losses:
 - Reaction time $\sim \frac{1}{2}$ turn ($40 \mu\text{s}$)
 - Very large dynamic range ($> 10^6$)
- There are **~ 3600 chambers** distributed over the ring to detect abnormal beam losses and if necessary trigger a beam abort !
- Very important beam instrumentation!



The LHC: just another collider?

| | Start | Type | Max proton energy [GeV] | Length [m] | B Field [Tesla] | Lumi [$\text{cm}^{-2}\text{s}^{-1}$] | Stored beam energy [MJoule] |
|--------------------------------------|-------|------------------|-------------------------|------------|-----------------|--|-----------------------------|
| TEVATRON Fermilab Illinois USA | 1983 | p-pbar | 980 | 6300 | 4.5 | $4.3 \cdot 10^{32}$ | 1.6 for protons |
| HERA DESY Hamburg | 1992 | p – e+ p – e- | 920 | 6300 | 5.5 | $5.1 \cdot 10^{31}$ | 2.7 for protons |
| RHIC Brookhaven Long Island | 2000 | Ion-Ion p-p | 250 | 3834 | 4.3 | $1.5 \cdot 10^{32}$ | 0.9 per proton beam |
| LHC CERN | 2008 | Ion-Ion p-p | 7000 Now 4000 | 26800 | 8.3 | 10^{34} Now 7.7×10^{33} | 362 per beam |
| Factor | | | 7 | 4 | 2 | 50 | 100 |

LHC pp and ions

7 TeV/c –up to
now 4 TeV/c

26.8 km
Circumference

The confusion with 7 TeV: energy of one
proton or two protons ? ...watch out

Switzerland
Lake Geneva

LHC Accelerator
(100 m down)

CMS, TOTEM

CERN-
Prevezin

ALICE

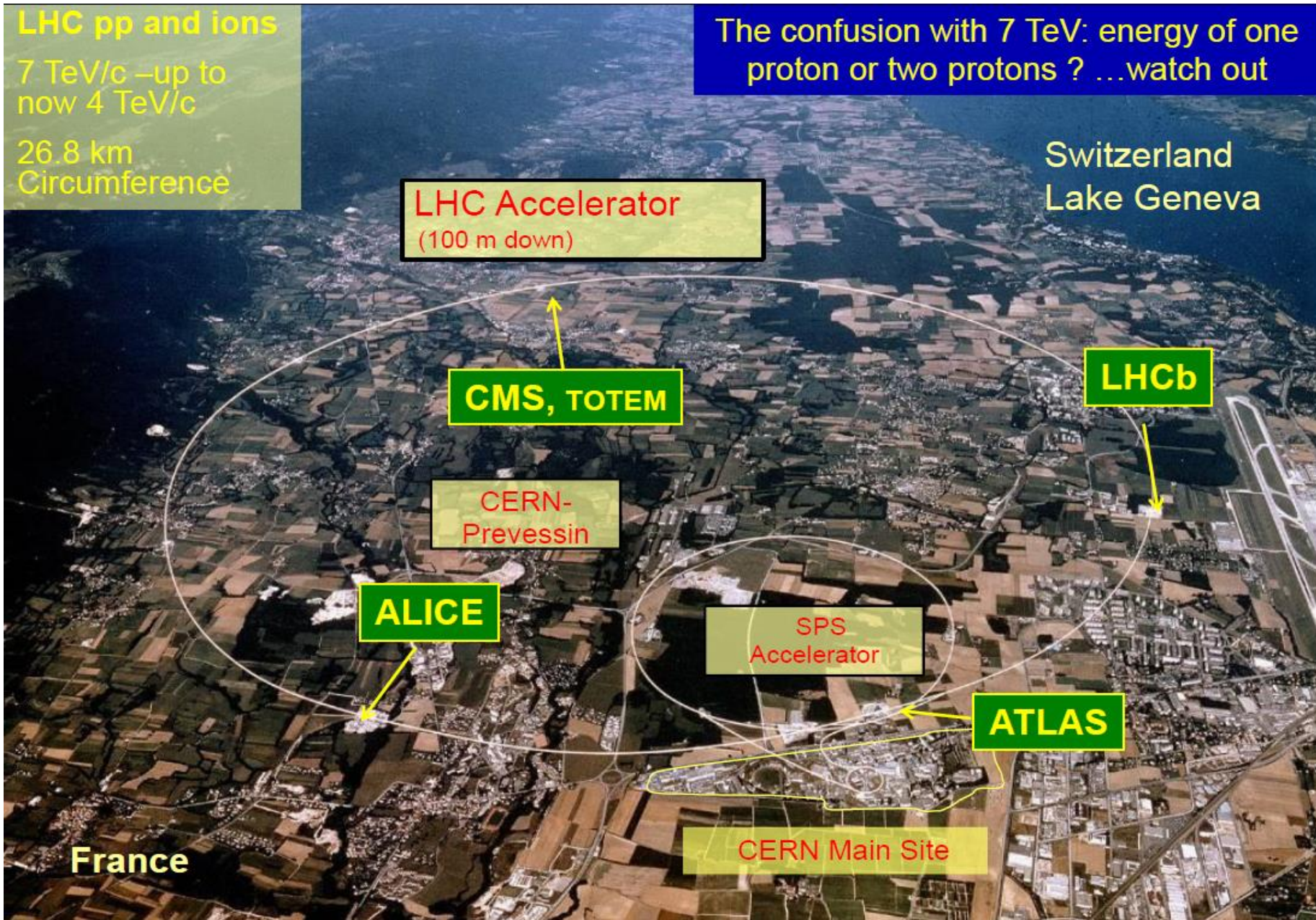
SPS
Accelerator

LHCb

ATLAS

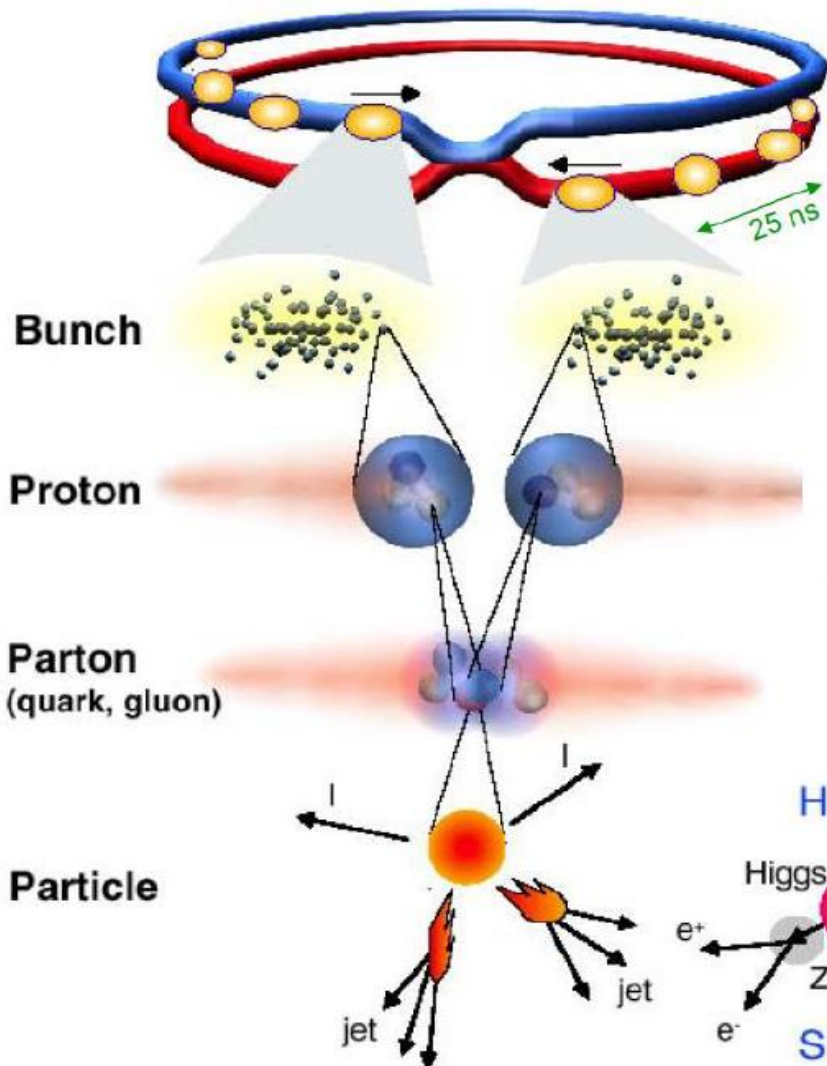
CERN Main Site

France



Collisions at LHC

| | |
|----------------------|--|
| Proton-Proton | 2835 bunch/beam |
| Protons/bunch | 10^{11} |
| Beam energy | 7 TeV (7×10^{12} eV) |
| Luminosity | 10^{34} cm ⁻² s ⁻¹ |



In the experiments:
 10^9 pp interactions per second
 ~ 1500 particles (p, n, π) produced in the detectors at each bunch-crossing

**Selection of 1 in
 10,000,000,000,000**

Summary: 2010 - 2012

$$L = \frac{kN_b^2 f \gamma}{4\pi \beta^* \varepsilon^*} F$$

| Parameter | 2010 | 2011 | 2012 | Nominal |
|---|---------|---------------------|----------------|---------|
| Energy [TeV] | 3.5 | 3.5 | 4.0 | 7.0 |
| N_b [10^{11} p/bunch] | 1.2 | 1.45 | 1.6 | 1.15 |
| k (no. bunches) | 368 | 1380 | 1380 | 2808 |
| Bunch spacing [ns] | 150 | 75 / 50 | 50 | 25 |
| Stored energy [MJ] | 25 | 112 | 140 | 362 |
| ε^* [μm] | 2.4 | 2.4 | 2.5 | 3.75 |
| β^* [m] | 3.5 | 1.5 \rightarrow 1 | 0.6 | 0.55 |
| Crossing angle [μrad] | 200 | 240 | 290 | 285 |
| L [10^{34} $\text{cm}^{-2}\text{s}^{-1}$] | 0.02 | 0.35 | 0.76 | 1.0 |
| Beam-beam parameter/IP (ΔQ_{bb}) | -0.0054 | -0.0065 | -0.0069 | -0.0033 |
| Average Pile-up @ beg. of fill | 8 | 17 | 38 | 26 |

The next years

