

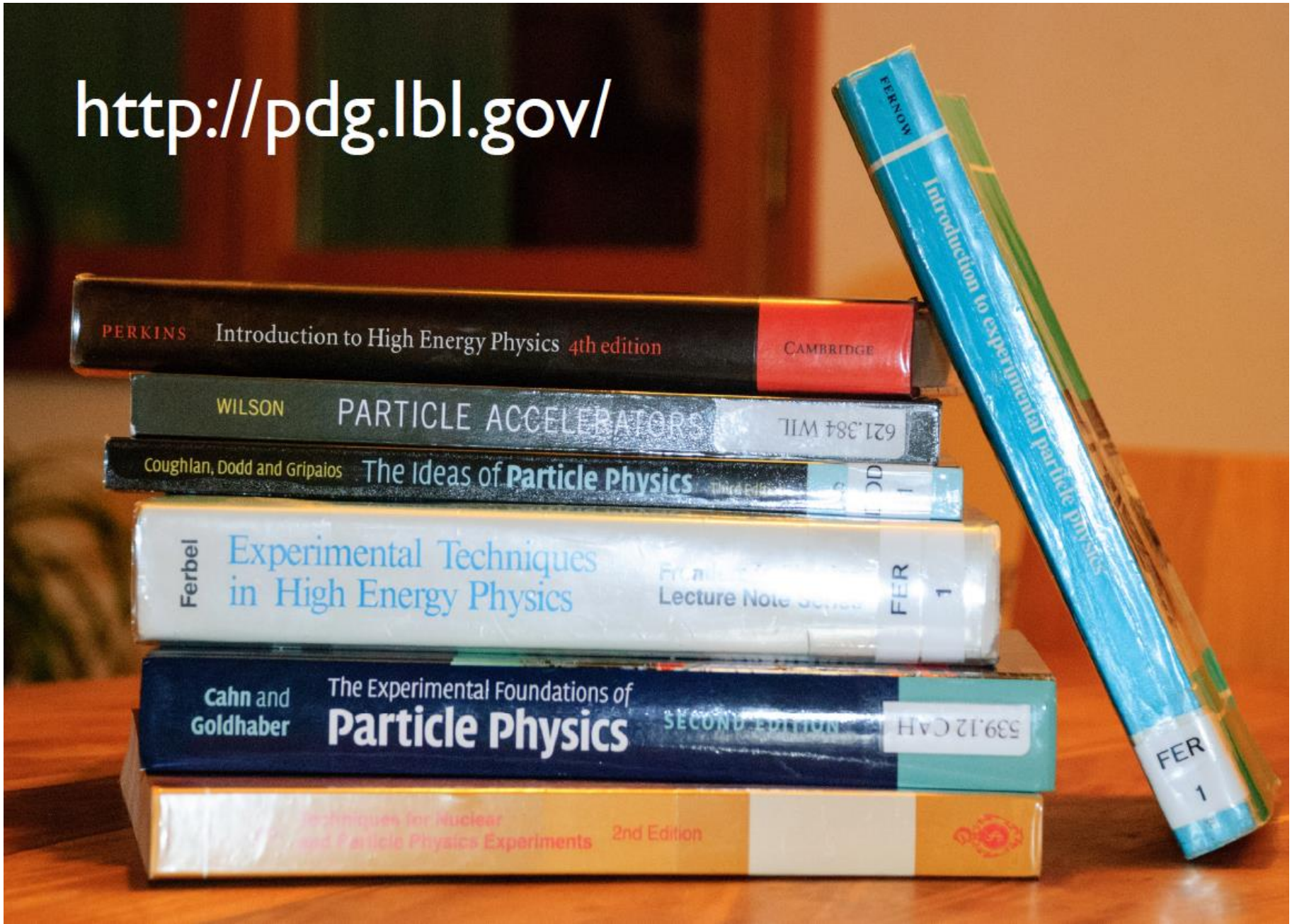
# Introduction to particle physics: experimental part

**Introduction**

**Units, kinematics**

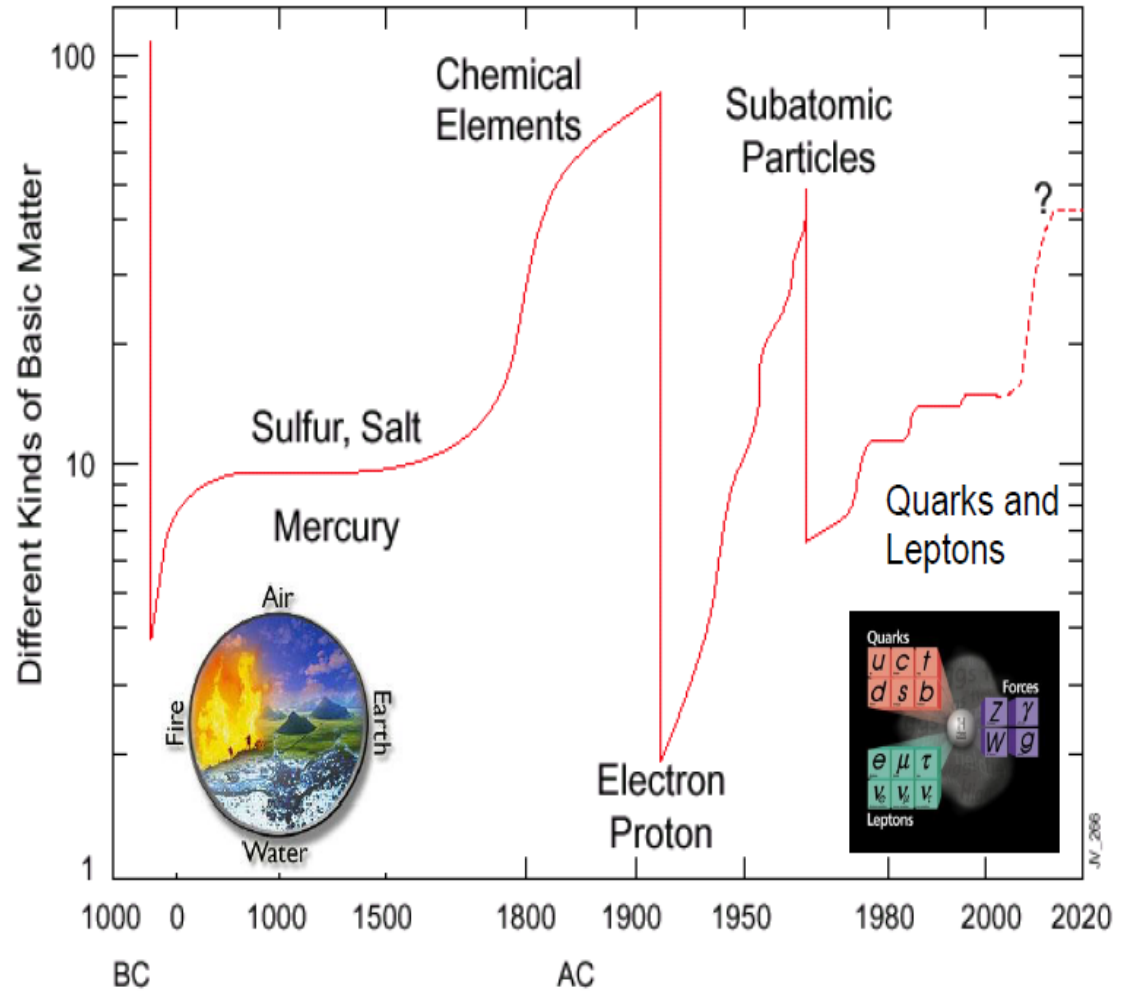
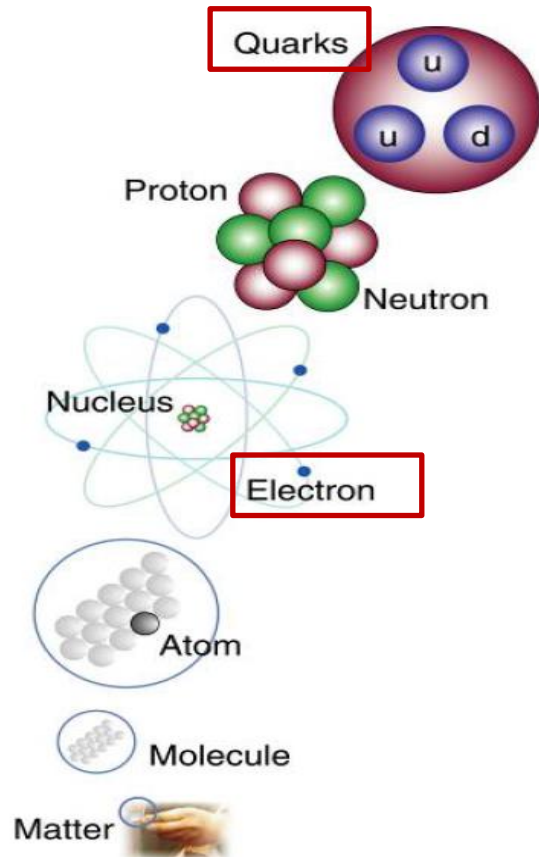
Large fraction of those slides from M. Delmastro lectures at ESIPAP school

<http://pdg.lbl.gov/>



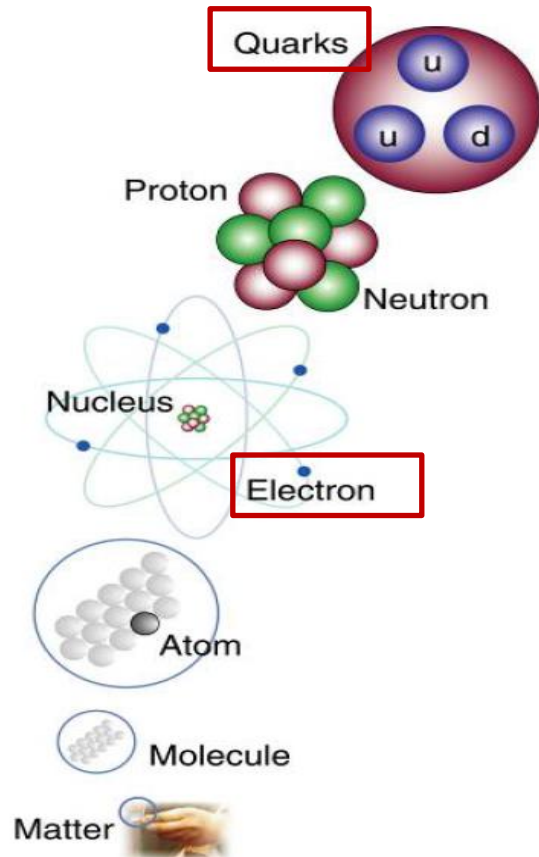
# Constituents of matter along History

Quantum mechanics



# Particles of the Standard Model

Quantum mechanics



**Matter particles**  
( $< 10^{-16}$  cm)

**Interaction particles**

2.4M <b>u</b> up 2/3 1/2	1.27G <b>c</b> charm 2/3 1/2	171.2G <b>t</b> top 2/3 1/2	strong nuclear force (color charge)
4.8M <b>d</b> down -1/3 1/2	104M <b>s</b> strange -1/3 1/2	4.2G <b>b</b> bottom -1/3 1/2	
0.511M <b>e</b> electron -1 1/2	105.7M <b>μ</b> muon -1 1/2	1.777G <b>τ</b> tau -1 1/2	
< 2.2 <b>ν<sub>e</sub></b> e-neutrino 0 1/2	< 0.17M <b>ν<sub>μ</sub></b> μ-neutrino 0 1/2	< 15.5M <b>ν<sub>τ</sub></b> τ-neutrino 0 1/2	electromagnetic (charge)
			<b>γ</b> photon 1
			weak nuclear force
			<b>Z</b> 1

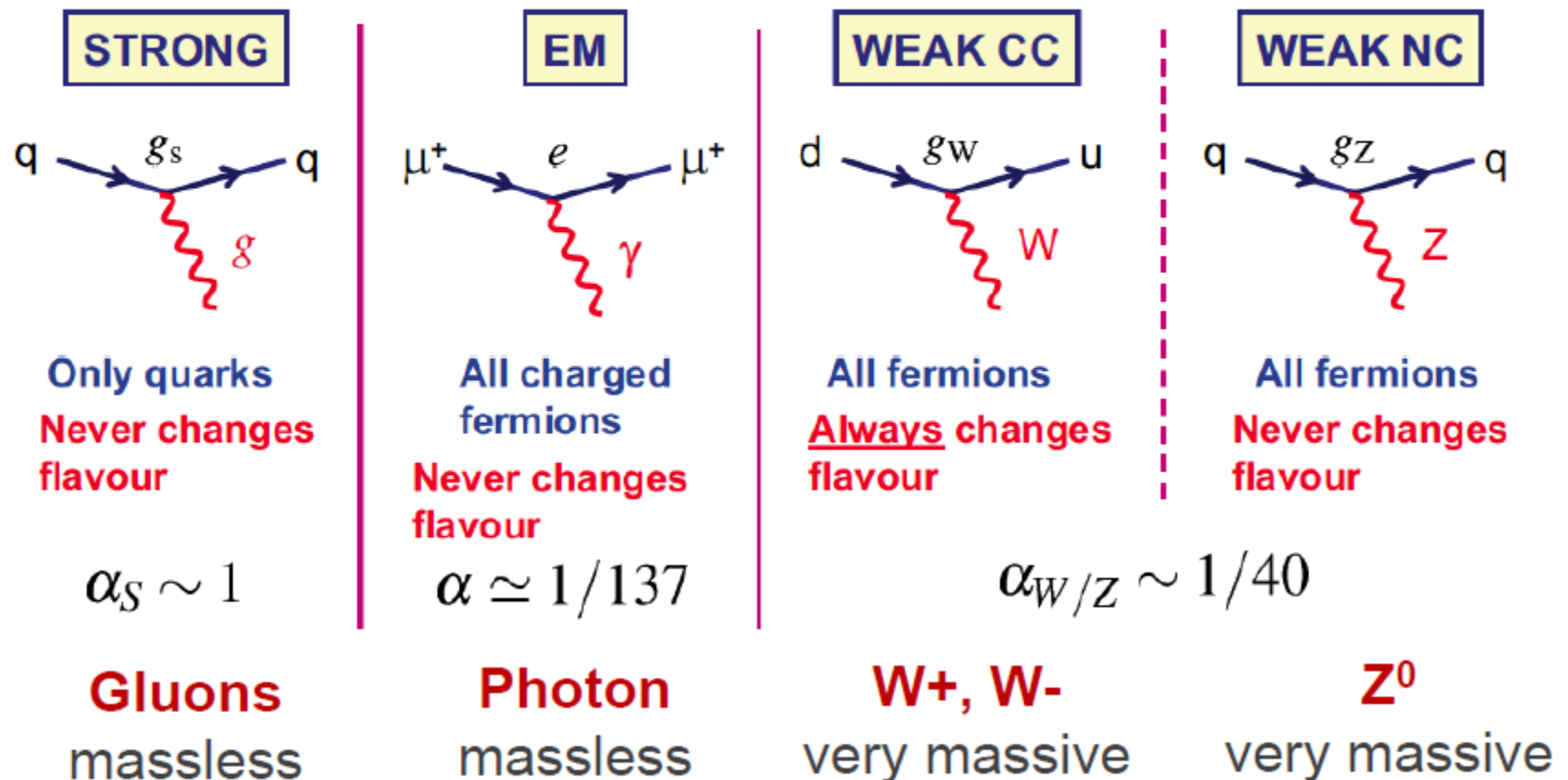


**Higgs particle**  
Is not a matter particle and  
not an interaction particle

$$L_H = \frac{1}{2}(\partial_\mu H)^2 - m_H^2 H^2 - h\lambda H^3 - \frac{h}{4}H^4 + \frac{g^2}{4}(W_\mu^+ W^\mu + \frac{1}{2\cos^2\theta_W} Z_\mu Z^\mu)(\lambda^2 + 2\lambda H + H^2) + \sum_{l,q,q'} (\frac{m_l \bar{l}l}{\lambda} + \frac{m_q \bar{q}q}{\lambda} + \frac{m_{q'} \bar{q}'q'}{\lambda})H$$

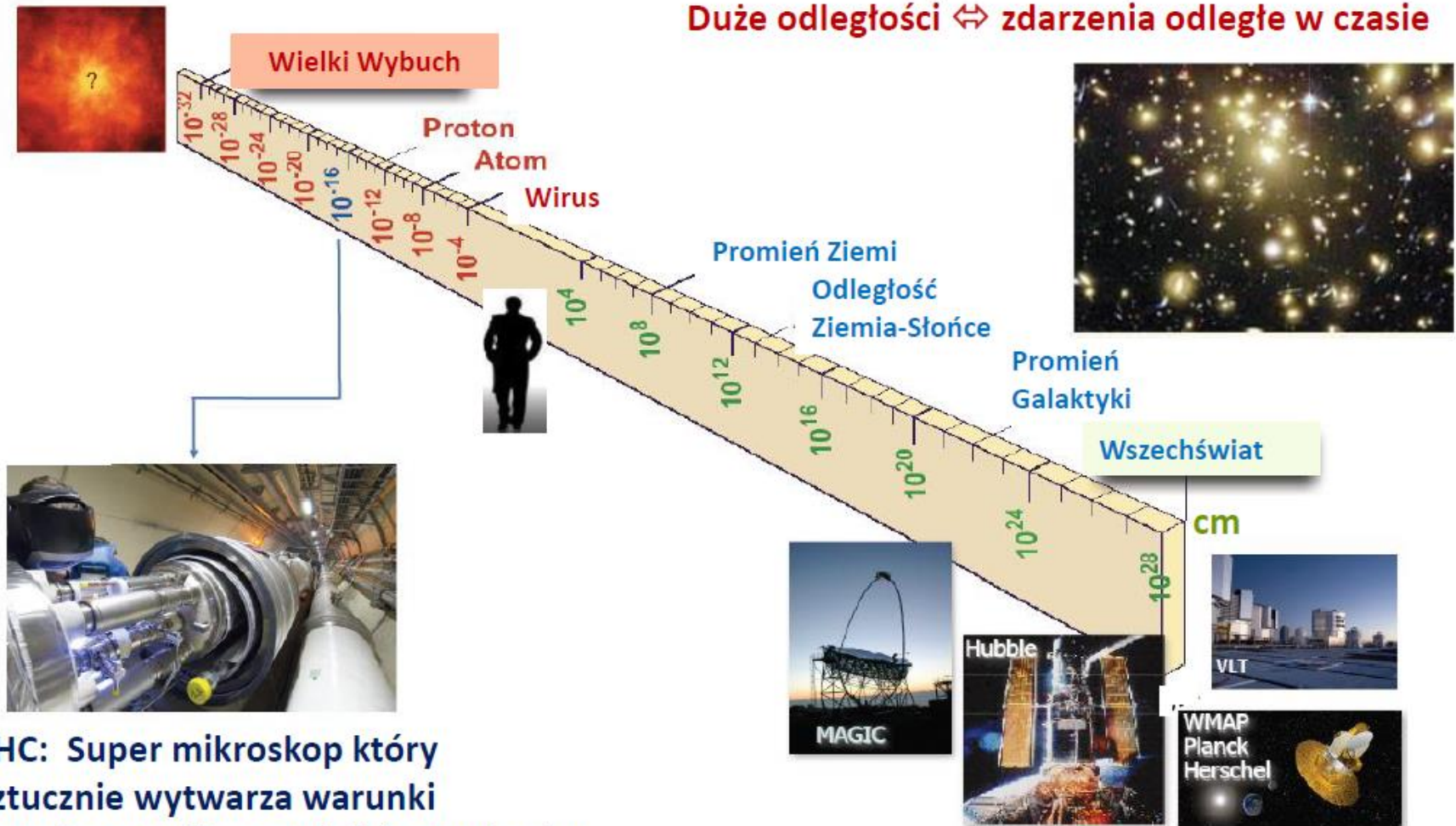
# Interactions

The interaction of gauge bosons with fermions is described by the Standard Model





# How we are probing structure of matter and how structure of the Universe



Duże odległości ⇔ zdarzenia odległe w czasie

Małe odległości ⇔ bardzo duże energie

# Nobel Prizes in Elementary Particle Physics



Sin-Itiro Tomonaga



Julian Schwinger



Richard P. Feynman



Sheldon Lee Glashow



Abdus Salam



Steven Weinberg

**GREEN** - theoretical  
**BLUE** - experimental

1964: „Higgs mechanism”  
was born



Leon M. Lederman



Melvin Schwartz



Jack Steinberger

1957 – C. N. Yang, T. Lee

1965 – S. I. Tomonaga, J. Schwinger, R.P Feynman

1969 – M. Gell-Mann

1976 – B. Richter and S. Ting

1979 – S.L. Glashow, A. Salam, S. Weinberg

1980 – J. Cronin, V. Fitch

1984 – C. Rubbia, S. van der Meer

1988 – L. M. Lederman, M. Schwartz, J. Steinberger

1990 – J. Friedman, J. Kendall, R. Taylor

1992 - G. Charpak

1995 – M. Perl, F. Reines

1999 - G. tHooft, M. J. Veltman

2004 - D. J. Gross, H. D. Politzer, F. Wilczek

2008 – Y. Nambu, M. Kobayashi, T. Masakawa

2013 – F. Englert and P. Higgs

2012: „Higgs particle”  
was discovered

2015 - T. Kajita and A. B. McDonald



Carlo Rubbia



Simon van der Meer



Georges Charpak



Gerardus 't Hooft



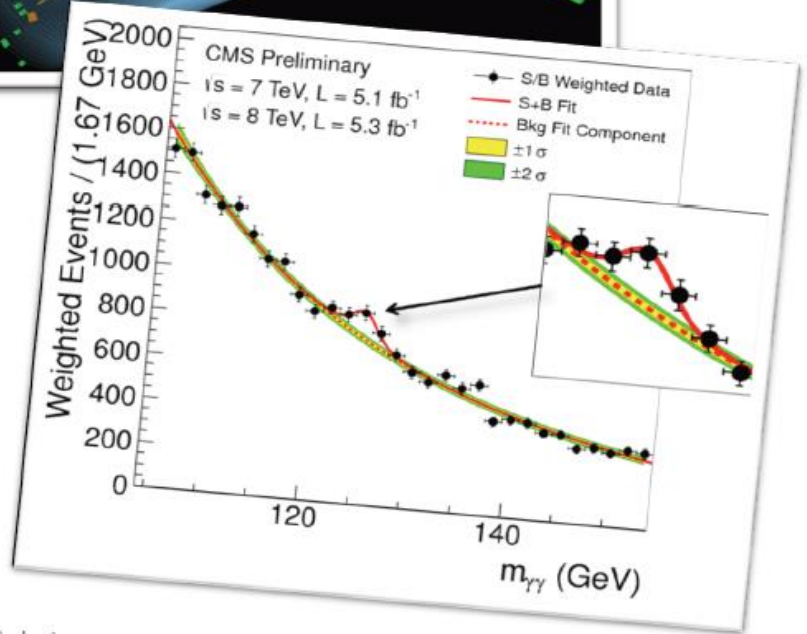
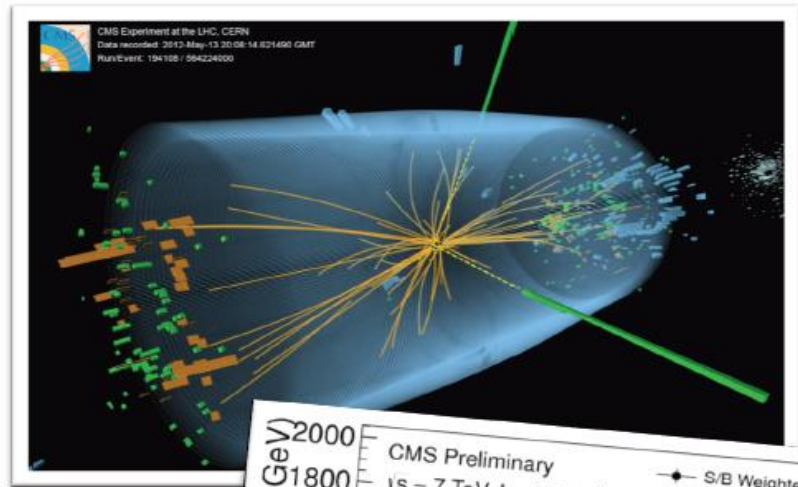
Martinus J.G. Veltman



M. Gell-Mann

# Experiment = probing theories with data

$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^\nu \partial_\nu g_\mu^\nu - g_s f^{abc} \partial_\mu g_\nu^\mu \partial_\nu g_\mu^\nu - \frac{1}{2} g_s^2 f^{abc} f^{ade} g_\mu^\mu g_\nu^\nu g_\rho^\rho g_\sigma^\sigma + \\
 & \frac{1}{2} 19 g_s^2 (g_1^\mu \gamma^\mu q_2^\nu) g_\mu^\nu + G^a \partial^\mu G^a + g_s f^{abc} \partial_\mu G^a G^b G^c - \partial_\mu W_\nu^+ \partial_\mu W_\nu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2} \partial_\mu H \partial_\mu H - \\
 & \frac{1}{2} m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2} \partial_\nu \phi^\mu \partial_\nu \phi^\mu - \frac{1}{2} M \phi^\mu \phi^\mu - \beta_h \frac{[2M]^2}{2} + \\
 & 2M H + \frac{1}{2} (H^2 + \phi^\mu \phi^\mu + 2\phi^+ \phi^-) + \frac{2M^4}{\Lambda^2} \alpha_h - ig_{c_w} [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\mu^- W_\nu^+) - Z_\mu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\mu W_\mu^+) + Z_\mu^0 (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\mu W_\mu^+) - ig_{s_w} [\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^- W_\mu^+) - A_\mu (W_\mu^+ \partial_\nu W_\mu^- - \\
 & W_\nu^- \partial_\mu W_\mu^+) + A_\mu (W_\mu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\mu W_\mu^+) - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \\
 & \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^- W_\nu^+ + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^-) + g^2 s_w^2 (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - \\
 & g^2 s_w^2 (A_\mu W_\nu^+ A_\nu W_\mu^- - A_\mu A_\nu W_\mu^+ W_\nu^-) - g\alpha [H^2 + H\phi^\mu \phi^\mu + 2(\phi^\mu)^2 H^2] - \\
 & W_\nu^+ W_\nu^-) - 2A_\mu Z_\mu^0 (W_\mu^+ W_\nu^-) - g\alpha [H^2 + H\phi^\mu \phi^\mu + 2(\phi^\mu)^2 H^2] - \\
 & \frac{1}{2} g^2 \alpha_h [H^4 + (\phi^\mu)^4 + 4(\phi^\mu)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 4(\phi^\mu)^2 H^2] - \\
 & g M W_\mu^+ W_\nu^- H - \frac{1}{2} g \frac{M}{c_w} Z_\mu^0 Z_\nu^0 H - \frac{1}{2} ig [W_\mu^+ (H \partial_\nu \phi^- - \phi^- \partial_\nu H) - W_\nu^- (H \partial_\mu \phi^+ - \\
 & W_\mu^+ \partial_\nu \phi^+ - \phi^+ \partial_\nu \phi^\mu)] + \frac{1}{2} ig [W_\mu^+ (H \partial_\nu \phi^- - \phi^- \partial_\nu H) - W_\nu^- (H \partial_\mu \phi^+ - \\
 & \phi^+ \partial_\nu H)] + \frac{1}{2} g \frac{1}{c_w} (Z_\mu^0 (H \partial_\nu \phi^\mu - \phi^\mu \partial_\nu H) - ig_{c_w}^2 M Z_\mu^0 (W_\mu^+ \phi^- - W_\nu^- \phi^+) + \\
 & ig_{s_w} M A_\mu (W_\mu^+ \phi^- - W_\nu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\nu \phi^- - \phi^- \partial_\nu \phi^+) - \\
 & ig_{s_w} A_\mu (\phi^+ \partial_\nu \phi^- - \phi^- \partial_\nu \phi^+) - \frac{1}{2} g^2 W_\mu^+ W_\nu^- [H^2 + (\phi^\mu)^2 + 2\phi^+ \phi^-] - \\
 & ig_{s_w} A_\mu (\phi^+ \partial_\nu \phi^- - \phi^- \partial_\nu \phi^+) + 2(2s_w^2 - 1)^2 \phi^+ \phi^- - \frac{1}{2} g^2 c_w^2 Z_\mu^0 \phi^\mu (W_\mu^+ \phi^+ + \\
 & \frac{1}{4} g^2 \frac{1}{c_w} Z_\mu^0 Z_\nu^0 [H^2 + (\phi^\mu)^2 + 2\phi^+ \phi^-] + \frac{1}{2} g^2 s_w A_\mu \phi^\mu (W_\mu^+ \phi^+ - \\
 & W_\nu^- \phi^-) - \frac{1}{2} ig^2 \frac{2c_w}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\nu^- \phi^+) - g^2 \frac{2c_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & W_\nu^- \phi^+) + \frac{1}{2} ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\nu^- \phi^+) - g^2 \frac{2c_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - \\
 & g^2 s_w^2 A_\mu A_\nu \phi^+ \phi^- - e^\lambda (\gamma^\mu \partial^\nu e^\lambda - \partial^\lambda \gamma^\mu e^\lambda) - \partial^\lambda \gamma^\mu \partial^\nu u_1^\lambda - \frac{1}{2} (d_1^\lambda \gamma^\mu d_1^\lambda) + \\
 & d_1^\lambda (\gamma^\mu + m_1^\lambda) d_1^\lambda + ig_{s_w} A_\mu [-(e^\lambda \gamma^\mu e^\lambda) + \frac{1}{2} (\bar{u}_1^\lambda \gamma^\mu u_1^\lambda) - \frac{1}{2} (d_1^\lambda \gamma^\mu d_1^\lambda)] + \\
 & \frac{ig}{4c_w} Z_\mu^0 [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (e^\lambda \gamma^\mu (4s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_1^\lambda \gamma^\mu (\frac{3}{2}s_w^2 - \\
 & 1 - \gamma^5) u_1^\lambda) + (d_1^\lambda \gamma^\mu (1 - \frac{3}{2}s_w^2 - \gamma^5) d_1^\lambda)] + \frac{ig}{2\sqrt{2}} W_\mu^+ [(\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + \\
 & (\bar{u}_1^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda u} d_1^\lambda) + \frac{ig}{2\sqrt{2}} W_\mu^- [(e^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (d_1^\lambda \gamma^\mu C_{\lambda \nu} \nu^\lambda) + \\
 & (\bar{u}_1^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda u} d_1^\lambda) + \frac{ig}{2\sqrt{2}} W_\mu^- [(e^\lambda \gamma^\mu (1 - \gamma^5) e^\lambda) + \phi^- (e^\lambda (1 + \gamma^5) \mu^\lambda) - \\
 & \frac{ig}{2\sqrt{2}} M \bar{u}_1^\lambda [-\phi^+ (\nu^\lambda (1 - \gamma^5) e^\lambda) + \frac{ig}{2\sqrt{2}} \phi^+ [-m_0^2 (\bar{u}_1^\lambda C_{\lambda \nu} (1 - \gamma^5) d_1^\lambda) + \\
 & \frac{ig}{2\sqrt{2}} M [H (e^\lambda e^\lambda) + i\phi^0 (e^\lambda \gamma^5 e^\lambda) + \frac{ig}{2\sqrt{2}} \phi^+ [-m_0^2 (\bar{u}_1^\lambda C_{\lambda \nu} (1 + \gamma^5) u_1^\lambda) - m_0^2 (d_1^\lambda C_{\lambda \nu} (1 - \\
 & \gamma^5) u_1^\lambda) - \frac{ig}{2\sqrt{2}} M H (\bar{u}_1^\lambda u_1^\lambda) - \frac{ig}{2\sqrt{2}} M H (\bar{d}_1^\lambda d_1^\lambda) + \frac{ig}{2\sqrt{2}} \phi^0 (\bar{u}_1^\lambda \gamma^5 u_1^\lambda) - \\
 & \frac{ig}{2\sqrt{2}} \phi^0 (\bar{d}_1^\lambda \gamma^5 d_1^\lambda) + X^+ (\partial^\mu - M^2) X^+ + X^- (\partial^\mu - M^2) X^- + X^0 (\partial^\mu - \\
 & \frac{M^2}{c_w} X^0 + \bar{Y} \partial^\mu Y + ig_{c_w} W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + ig_{s_w} W_\mu^+ (\partial_\mu \bar{Y} X^- - \\
 & \partial_\mu \bar{X}^+ Y) + ig_{c_w} W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^+) + ig_{s_w} W_\mu^- (\partial_\mu \bar{X}^- Y - \\
 & \partial_\mu \bar{Y} X^+) + ig_{c_w} Z_\mu^0 (\partial_\mu \bar{X}^+ X^- - \partial_\mu \bar{X}^- X^+) + ig_{s_w} A_\mu (\partial_\mu \bar{X}^+ X^- + \\
 & \partial_\mu \bar{X}^- X^+) - \frac{1}{2} g M [\bar{X}^+ X^+ H + \bar{X}^- X^- H + \frac{1}{c_w} \bar{X}^0 X^0 H] + \\
 & \frac{1-2c_w^2}{2c_w} ig M [\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-] + \frac{1}{2c_w} ig M [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \\
 & ig M s_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2} ig M [\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]
 \end{aligned}$$



- Delamater

(experimental) LHC physics



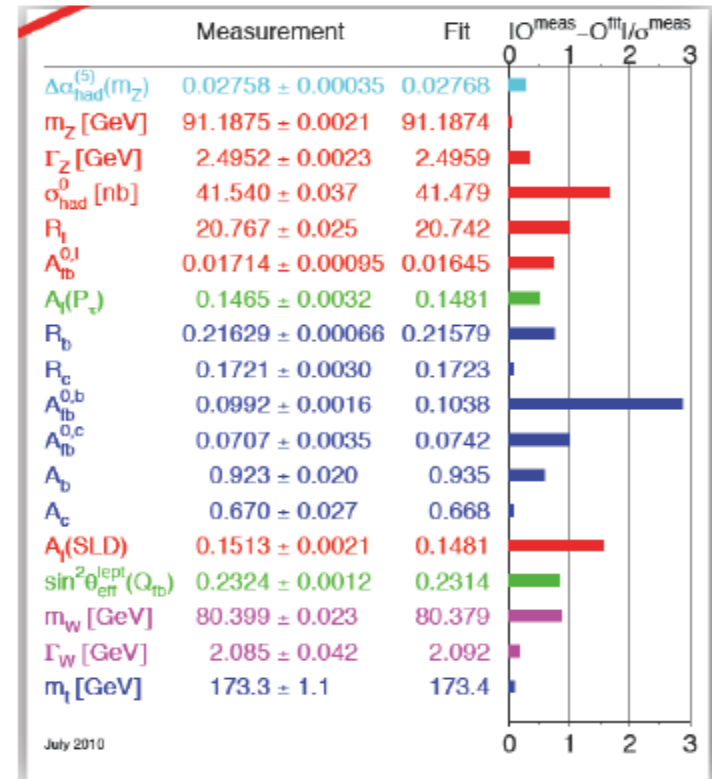
# Standard Model confirmed by the data

	I	II	III	
mass →	2.4 MeV/c <sup>2</sup>	1.27 GeV/c <sup>2</sup>	171.2 GeV/c <sup>2</sup>	0
charge →	2/3	2/3	2/3	0
spin →	1/2	1/2	1/2	1
name →	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>γ</b> photon
	4.8 MeV/c <sup>2</sup>	104 MeV/c <sup>2</sup>	4.2 GeV/c <sup>2</sup>	0
	-1/3	-1/3	-1/3	0
	1/2	1/2	1/2	1
Quarks	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>g</b> gluon
	<2.2 eV/c <sup>2</sup>	<0.17 MeV/c <sup>2</sup>	<15.5 MeV/c <sup>2</sup>	91.2 GeV/c <sup>2</sup>
	0	0	0	0
	1/2	1/2	1/2	1
Leptons	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>Z<sup>0</sup></b> Z boson
	0.511 MeV/c <sup>2</sup>	105.7 MeV/c <sup>2</sup>	1.777 GeV/c <sup>2</sup>	80.4 GeV/c <sup>2</sup>
	-1	-1	-1	±1
	1/2	1/2	1/2	1
	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>W<sup>±</sup></b> W boson

Gauge bosons

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + h.c.$$

## STANDARD MODEL OF ELEMENTARY PARTICLES



Confirmed at sub 1% level!

# HEP, SI and „natural” units

Quantity	HEP units	SI units
length	1 fm	$10^{-15}$ m
charge	e	$1.602 \cdot 10^{-19}$ C
energy	1 GeV	$1.602 \times 10^{-10}$ J
mass	1 GeV/c <sup>2</sup>	$1.78 \times 10^{-27}$ kg
$\hbar = h/2\pi$	$6.588 \times 10^{-25}$ GeV s	$1.055 \times 10^{-34}$ Js
c	$2.988 \times 10^{23}$ fm/s	$2.988 \times 10^8$ m/s
$\hbar c$	197 MeV fm	...

## “natural” units ( $\hbar = c = 1$ )

mass	1 GeV
length	1 GeV <sup>-1</sup> = 0.1973 fm
time	1 GeV <sup>-1</sup> = $6.59 \times 10^{-25}$ s

# Measuring particles

- Particles are characterized by
  - ✓ **Mass** [Unit: eV/c<sup>2</sup> or eV]
  - ✓ **Charge** [Unit: e]
  - ✓ **Energy** [Unit: eV]
  - ✓ **Momentum** [Unit: eV/c or eV]
  - ✓ (+ spin, lifetime, ...)

Particle identification via measurement of:

e.g. (E, p, Q) or (p, β, Q)  
(p, m, Q) ...

- ... and move at **relativistic speed**

$$\beta = \frac{v}{c} \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$l = \frac{l_0}{\gamma} \quad \text{length contraction}$$

$$t = t_0 \gamma \quad \text{time dilatation}$$

$$E^2 = \vec{p}^2 c^2 + m^2 c^4$$

$$E = m \gamma c^2 = m c^2 + E_{\text{kin}}$$

$$\vec{\beta} = \frac{\vec{p}c}{E} \quad \vec{p} = m \gamma \vec{\beta} c$$

# Relativistic kinematics

$$\begin{aligned} E^2 &= \vec{p}^2 + m^2 \\ \ell &= \frac{\ell_0}{\gamma} & E &= m\gamma \\ t &= t_0\gamma & \vec{p} &= m\gamma\vec{\beta} \\ & & \vec{\beta} &= \frac{\vec{p}}{E} \end{aligned}$$

## Center of mass energy

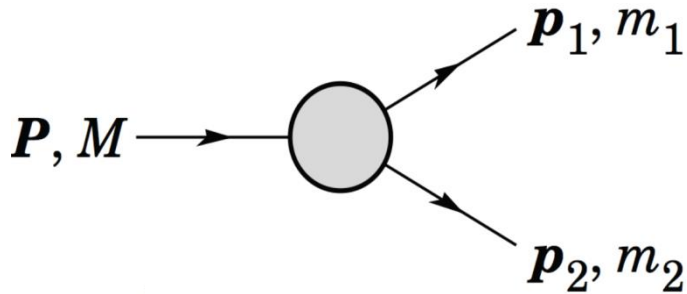
- In the **center of mass frame** the total momentum is 0
- In **laboratory frame** center of mass energy can be computed as:

$$E_{\text{cm}} = \sqrt{s} = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \vec{p}_i\right)^2}$$



# Kinematics

## 2-bodies decays

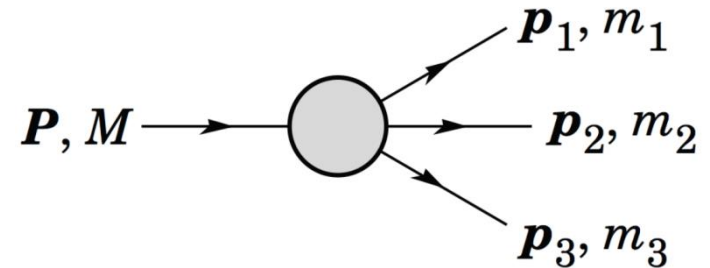


$$E_1 = \frac{M^2 - m_2^2 + m_1^2}{2M}$$

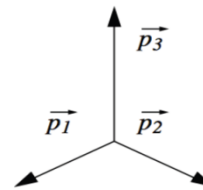
$$|\mathbf{p}_1| = |\mathbf{p}_2|$$

$$= \frac{[(M^2 - (m_1 + m_2)^2)(M^2 - (m_1 - m_2)^2)]^{1/2}}{2M}$$

## 3-bodies decays



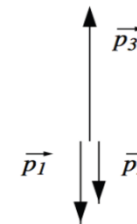
$$|\mathbf{p}_3| = \frac{[(M^2 - (m_{12} + m_3)^2)(M^2 - (m_{12} - m_3)^2)]^{1/2}}{2M}$$



(a)

$$\max(|\vec{p}_3|)$$

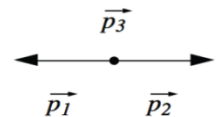
$$\min(|\vec{p}_3|)$$



(b)

$$(m_{12})_{min} = m_1 + m_2$$

$$(m_{12})_{max} = M - m_3$$



(c)

## Invariant mass

$$M = \sqrt{\left(\sum E_i\right)^2 - \left(\sum \vec{p}_i\right)^2}$$

# A real example: pion decays

pion decays at rest

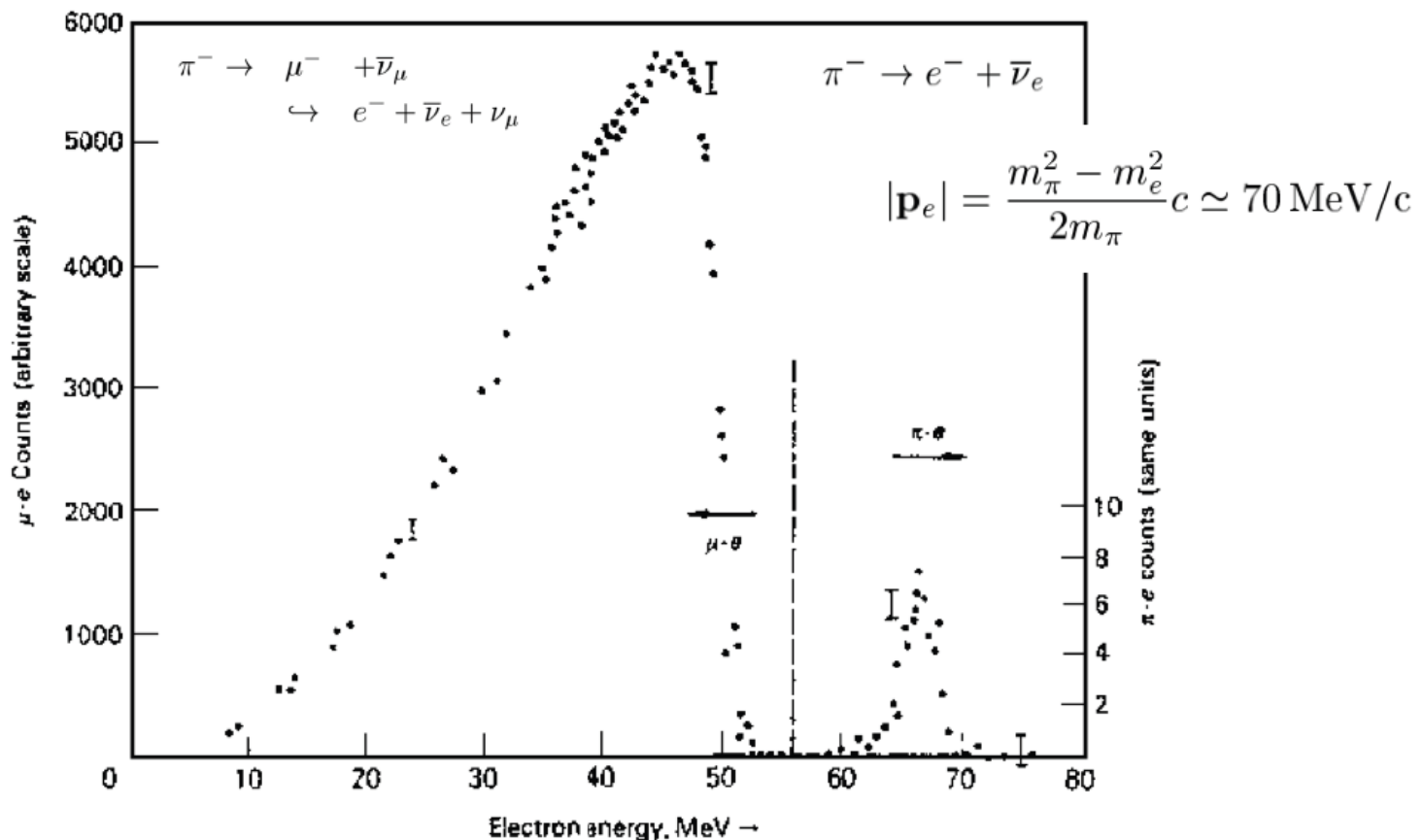
$$|\mathbf{p}_\mu| = \frac{m_\pi^2 - m_\mu^2}{2m_\pi} c \simeq 30 \text{ MeV}/c$$

$m_\nu = 0$ .

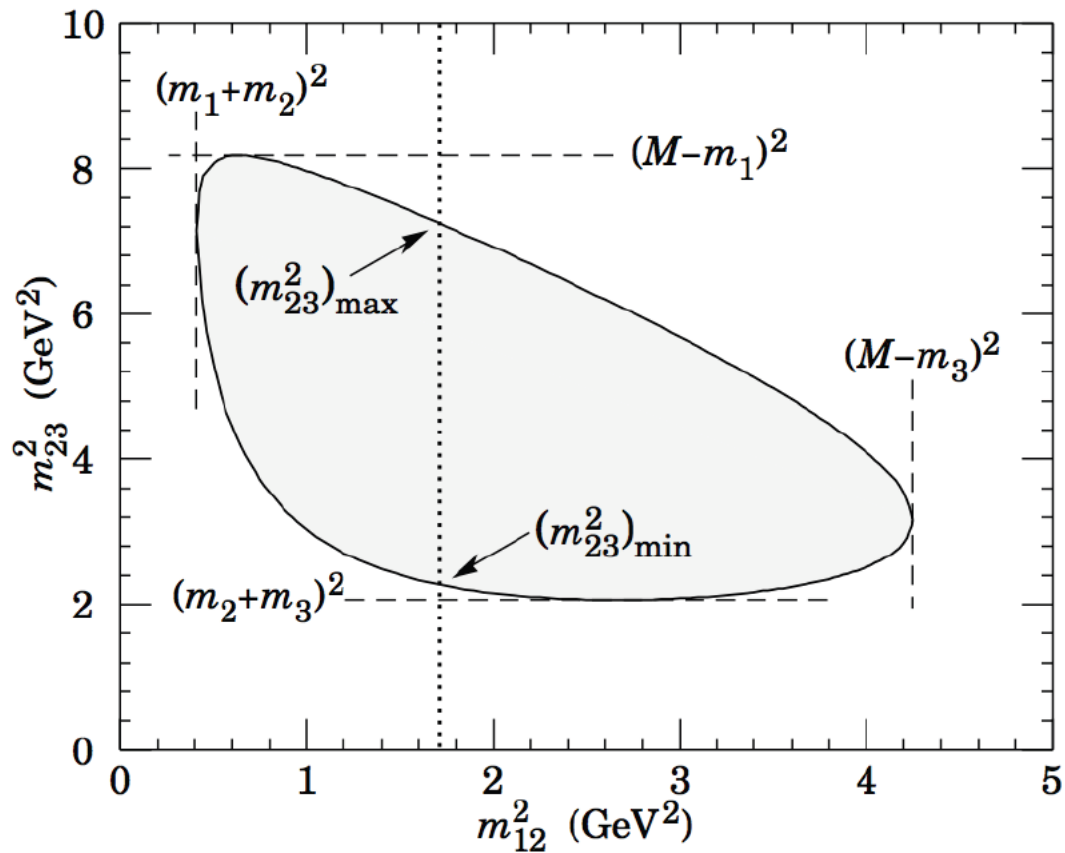
in most cases  
muon decays  
at rest

$$|\mathbf{p}_e|_{max} = \frac{m_\mu^2 - m_e^2}{2m_\mu} c \simeq 52 \text{ MeV}/c$$

$$|\mathbf{p}_e|_{min} = 0$$

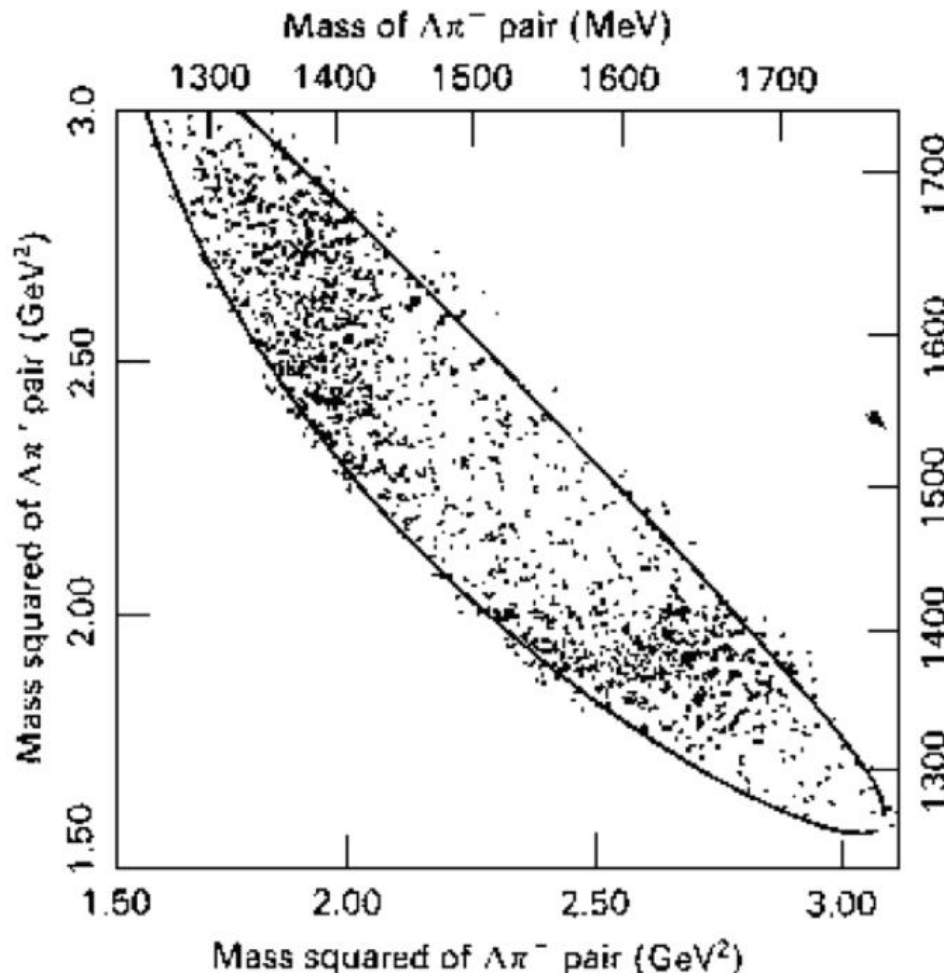
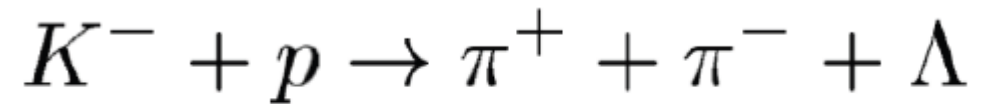


# 3-bodies decay: Dalitz plot



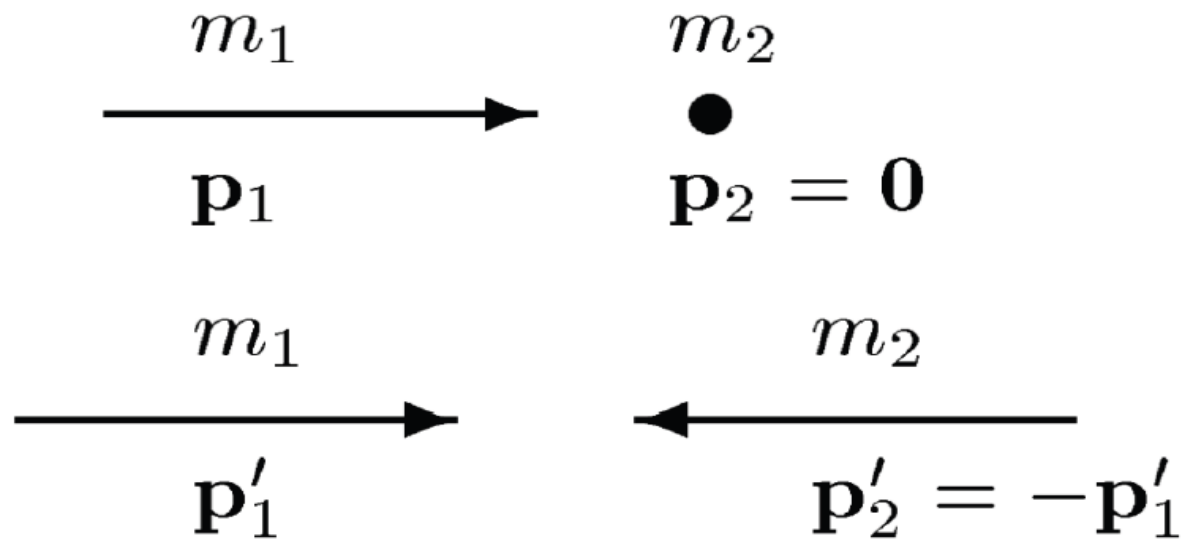
**Figure 45.3:** Dalitz plot for a three-body final state. In this example, the state is  $\pi^+ \bar{K}^0 p$  at 3 GeV. Four-momentum conservation restricts events to the shaded region.

# Multi-bodies decay





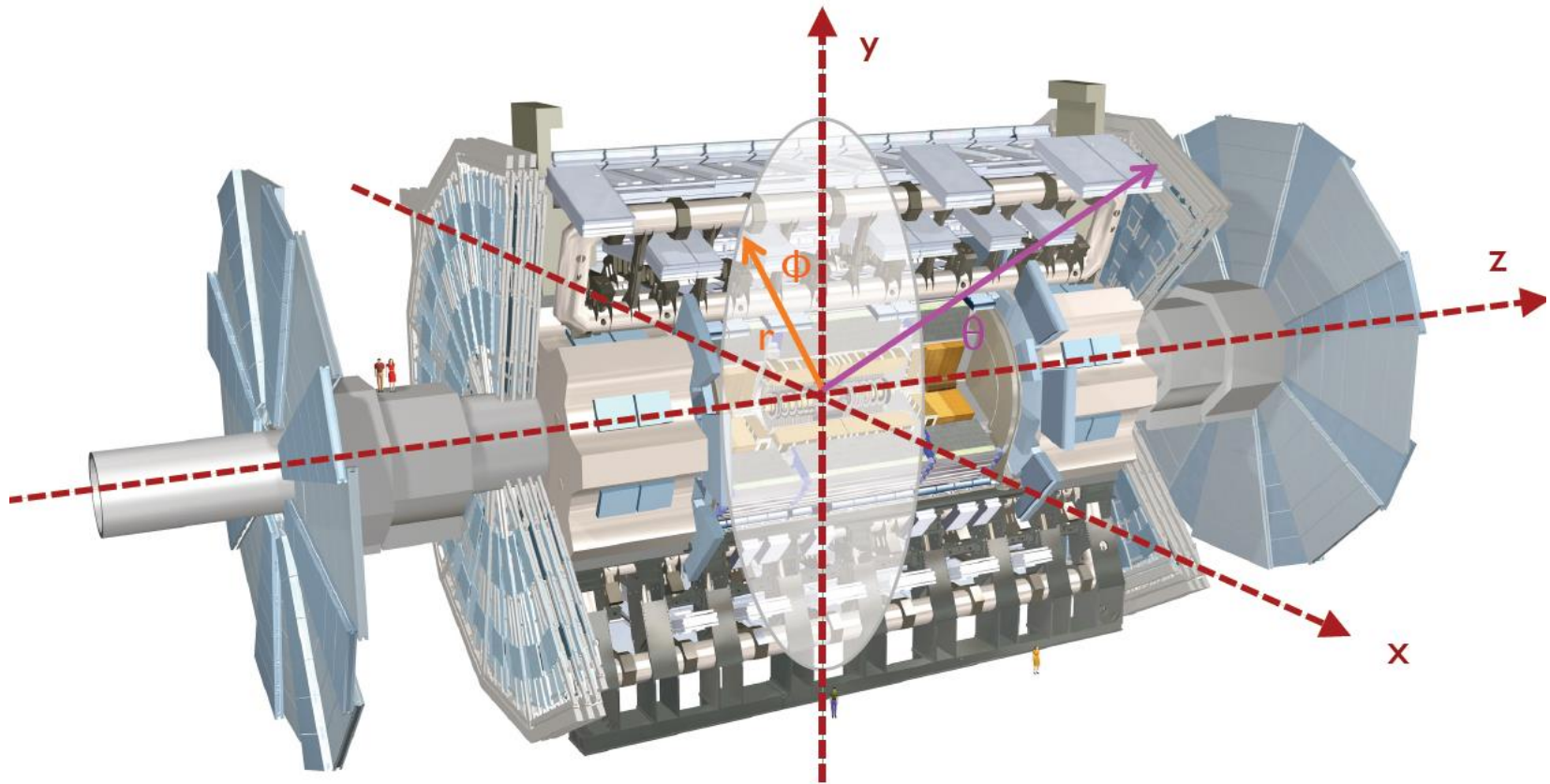
# Fixed target vs collider



How much energy should a fixed target experiment have to equal the center of mass energy of two colliding beam?

$$E_{\text{fix}} = 2 \frac{E_{\text{col}}^2}{m} - m$$

# Collider experiment coordinates



# Rapidity

Lorentz factor  $\gamma = \frac{1}{\sqrt{1 - \beta^2}} = \cosh \varphi$  Hyperbolic cosine of “rapidity”

$$\begin{aligned} E &= m \cosh \varphi & \varphi &= \tanh^{-1} \frac{E}{|\vec{p}|} = \frac{1}{2} \ln \frac{E + |\vec{p}|}{E - |\vec{p}|} \\ |\vec{p}| &= m \sinh \varphi \end{aligned}$$

- Particle physicists prefer to use modified rapidity along beam axis

$$y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

# Pseudorapidity

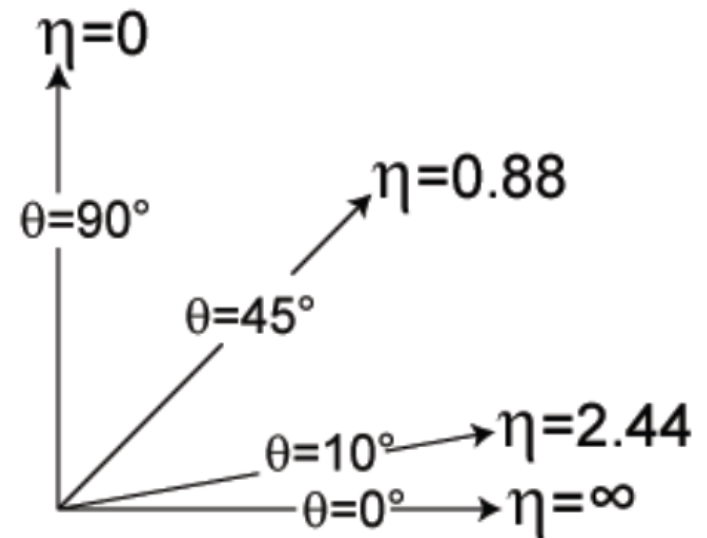
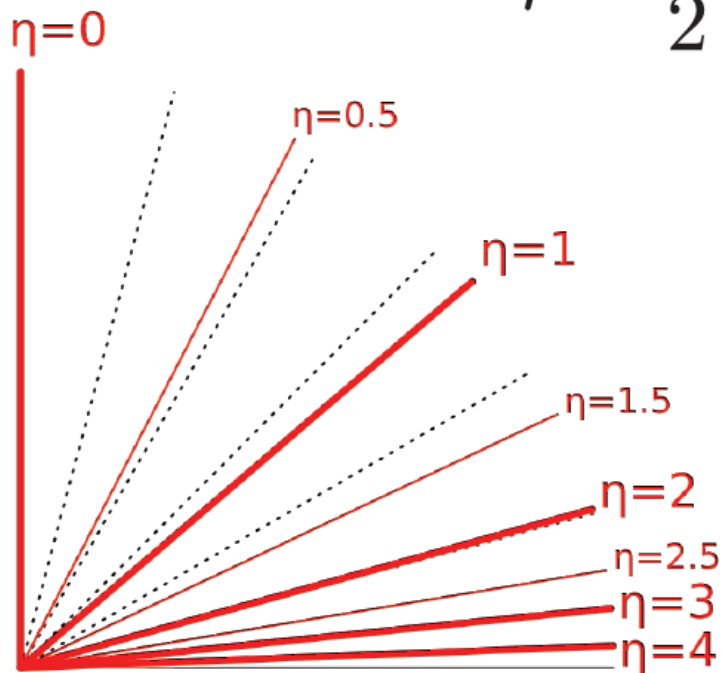
$$\eta = \frac{1}{2} \ln \frac{|\vec{p}| + p_z}{|\vec{p}| - p_z}$$

$$y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

$$\eta \simeq y$$

if  $E \gg m$

$$\eta = \frac{1}{2} \ln \left( \tan \frac{\theta}{2} \right)$$





# Transverse variables

- At hadron colliders, a significant and unknown fraction of the beam energy in each event escapes down the beam pipe.
- Net momentum can only be constrained in the plane transverse to the beam z-axis!

$$p_T = \sqrt{p_x^2 + p_y^2}$$
$$p_x = p_T \cos \phi$$
$$p_y = p_T \sin \phi$$
$$p_z = p_T \sinh \eta$$
$$|p| = p_T \cosh \eta$$
$$E_T = \frac{E}{\cosh \eta}$$

$$\sum p_x(i) = 0 \quad \sum p_y(i) = 0$$

# Missing transverse energy and transverse mass

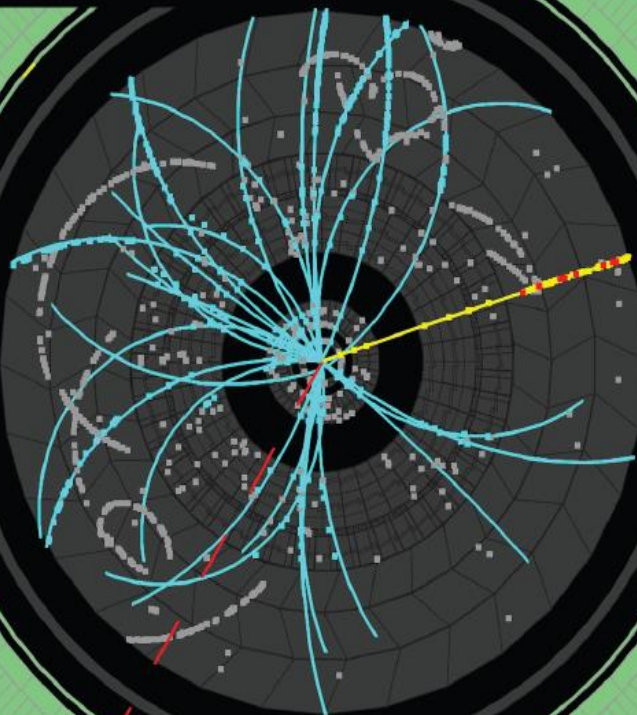
- If invisible particles are created, only their transverse momentum can be constrained: **missing transverse energy**

$$E_T^{\text{miss}} = \sum p_T(i)$$

- If a heavy particle is produced and decays into two particles one of which is invisible, the mass of the parent particle can be constrained with the **transverse mass quantity**

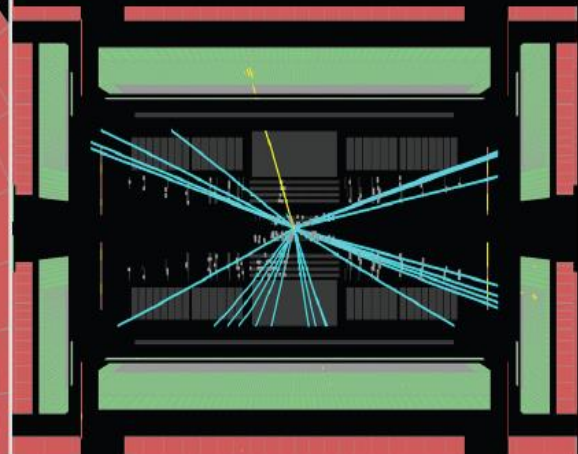
$$\begin{aligned} M_T^2 &\equiv [E_T(1) + E_T(2)]^2 - [\mathbf{p}_T(1) + \mathbf{p}_T(2)]^2 \\ &= m_1^2 + m_2^2 + 2[E_T(1)E_T(2) - \mathbf{p}_T(1) \cdot \mathbf{p}_T(2)] \end{aligned}$$

if  $m_1 = m_2 = 0$        $M_T^2 = 2|\mathbf{p}_T(1)||\mathbf{p}_T(2)|(1 - \cos \phi_{12})$



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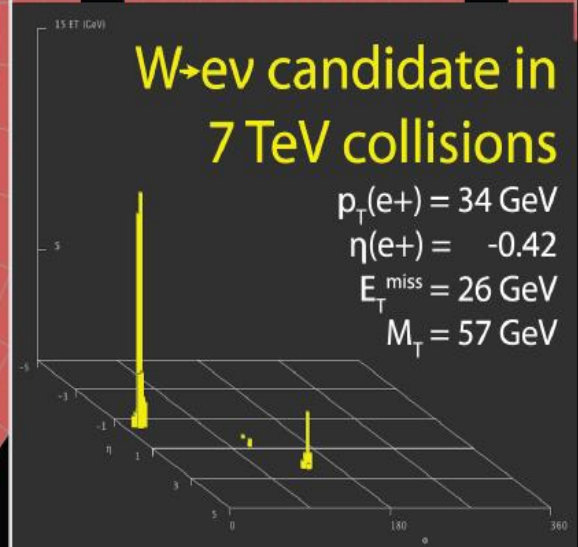
## W $\rightarrow$ ev candidate in 7 TeV collisions

$$p_T(e^+) = 34 \text{ GeV}$$

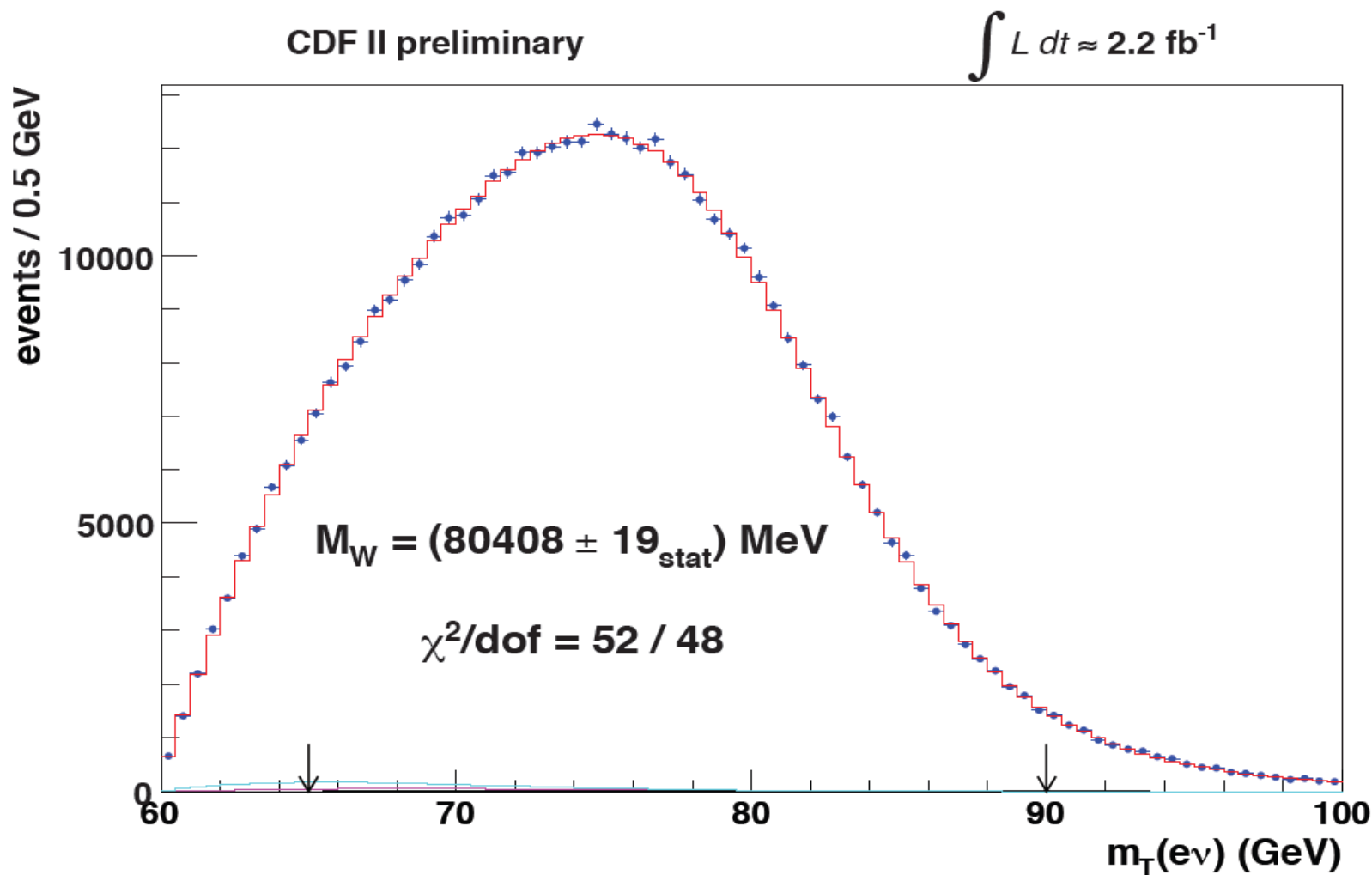
$$\eta(e^+) = -0.42$$

$$E_T^{\text{miss}} = 26 \text{ GeV}$$

$$M_T = 57 \text{ GeV}$$

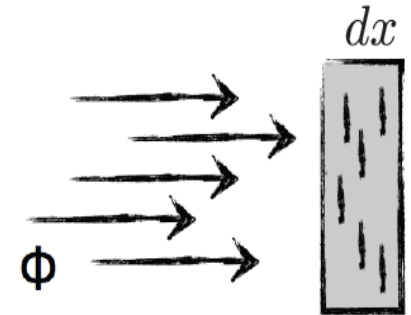


# Mass of the W boson



# Interaction cross-section

Flux  $\Phi = \frac{1}{S} \frac{dN_i}{dt}$   $[L^{-2} t^{-1}]$



Reactions per unit of time  $\frac{dN_{\text{reac}}}{dt} = \Phi \underbrace{\sigma}_{\text{area obscured by target particle}} N_{\text{target}} dx$   $[t^{-1}]$

$[L^{-2} t^{-1}]$   $[?]$   $[L^{-1}]$   $[L]$

Reaction rate per target particle  $W_{if} = \Phi \sigma$   $[t^{-1}]$

Cross section per target particle  $\sigma = \frac{W_{if}}{\Phi}$   $[L^2]$  = reaction rate per unit of flux

$1b = 10^{-28} \text{ m}^2$  (roughly the area of a nucleus with  $A = 100$ )

# Fermi Golden rule

From non-relativistic perturbation theory...

transition probability      matrix element      energy density of final states

$$W_{if} = \frac{2\pi}{\hbar} |M_{if}|^2 \frac{dN}{dE_f}$$

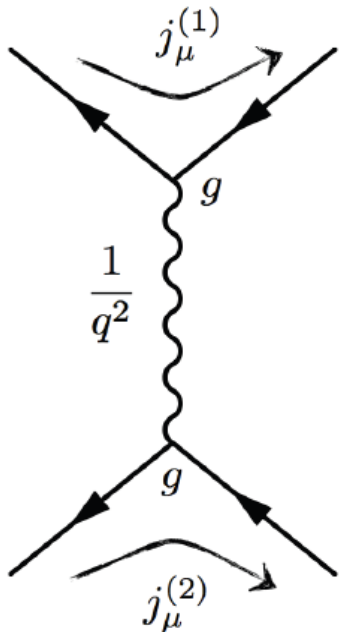
[t<sup>-1</sup>]

[E]

[E<sup>-1</sup>]

$$M_{if} = -i \int j_\mu^{(1)} \left( \frac{1}{q^2} \right) j_\mu^{(2)} d^4x$$

$$\sigma \sim |M_{if}|^2 \sim g^4 \left( \frac{1}{q^4} \right)$$





# Cross-section: magnitude and units

Standard

cross section unit:

$$[\sigma] = \text{mb}$$

with  $1 \text{ mb} = 10^{-27} \text{ cm}^2$

or in

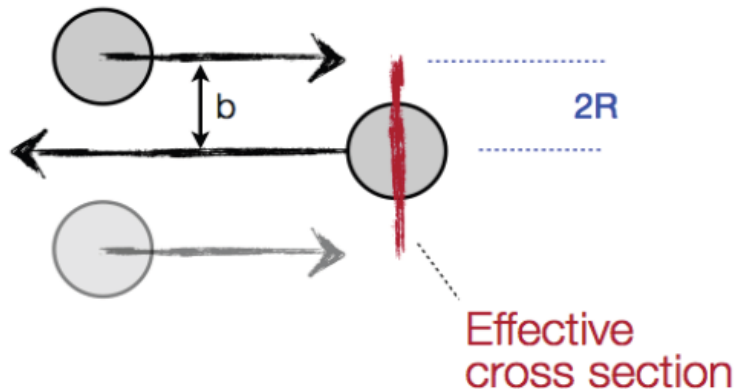
natural units:

$$[\sigma] = \text{GeV}^{-2}$$

with  $1 \text{ GeV}^{-2} = 0.389 \text{ mb}$

$$1 \text{ mb} = 2.57 \text{ GeV}^{-2}$$

Estimating the  
proton-proton cross section:



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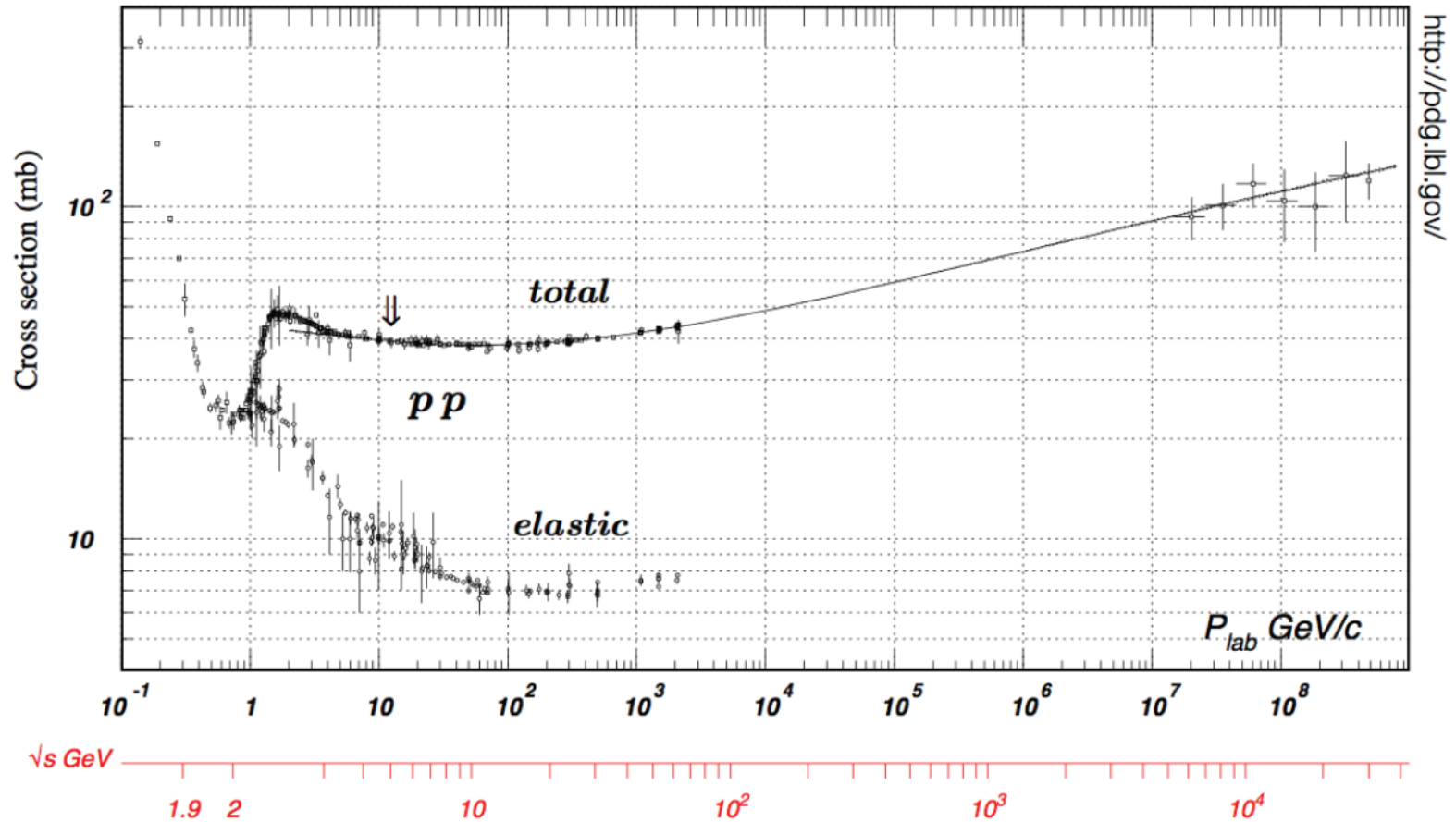
using:  $\hbar c = 0.1973 \text{ GeV fm}$   
 $(\hbar c)^2 = 0.389 \text{ GeV}^2 \text{ mb}$

Proton radius:  $R = 0.8 \text{ fm}$

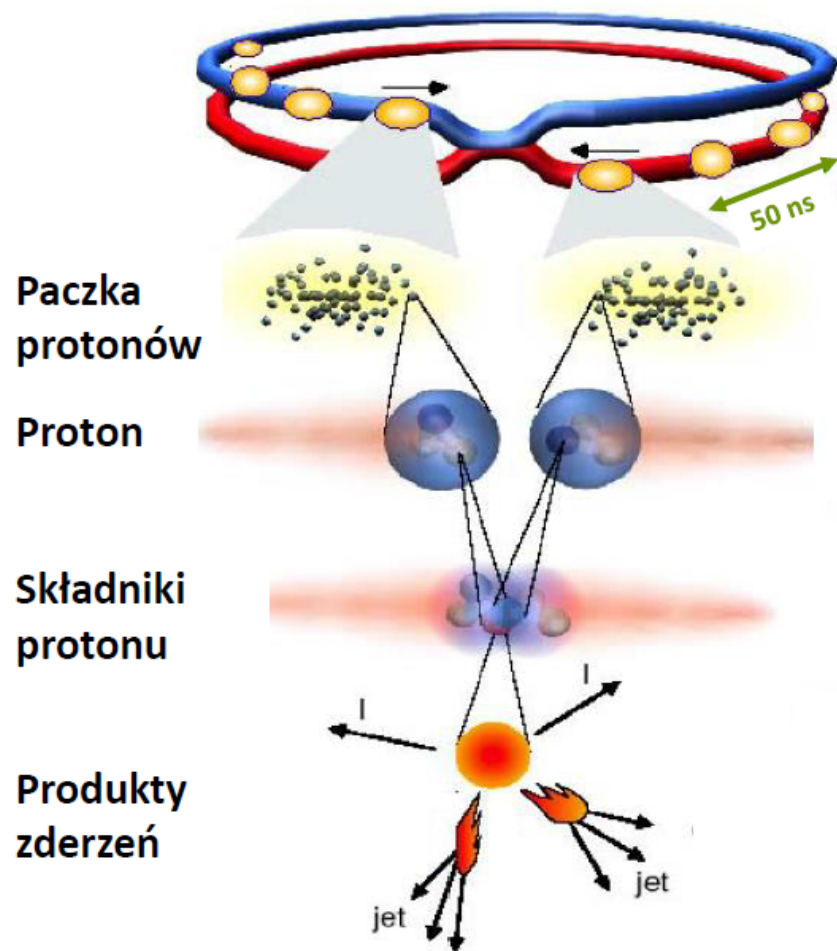
Strong interactions happens up to  $b = 2R$

$$\begin{aligned}\sigma &= \pi (2R)^2 = \pi \cdot 1.6^2 \text{ fm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10^{-26} \text{ cm}^2 \\ &= \pi \cdot 1.6^2 \cdot 10 \text{ mb} \\ &= 80 \text{ mb}\end{aligned}$$

# Proton-proton scattering cross-section



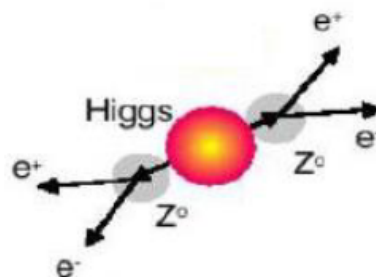
# Proton-proton collisions at LHC



Proton-Proton	1380 paczek/wiązkę
Protonów/paczka	$1.7 \cdot 10^{11}$
Energia wiązki	4 TeV

Każdy proton porusza się z prędkością bliską prędkości światła i niesie kinetyczną energię muchy w locie, okrąża pierścień akceleratora 1100 razy na sekundę.

Rozmiar poprzeczny wiązki:  $16 \mu\text{m}$  (4 razy mniejszy niż grubość ludzkiego włosa).  
Każda z wiązek niesie energię pociągu TGV o dł. 200 m i jadącego z prędkością 155km/godz (360M Jula).



**Takie zdarzenie pojawia się raz na 10 bilionów zderzeń**

# Cross-sections at LHC

