Indirect measurement of $\sin^2 \theta_W$ (M_W) using e^+e^- pairs in the Z-boson region with $p\bar{p}$ collisions at a center-of-momentum energy of 1.96 TeV

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Drell-Yan lepton pairs are produced in the process $p\bar{p}\to e^+e^-+X$ through an intermediate γ^*/Z boson. The lepton angular distributions are used to provide information on the electroweak-mixing parameter $\sin^2\theta_W$ via its observable effective-leptonic $\sin^2\theta_W$, or $\sin^2\theta_{\rm eff}^{\rm lept}$. A new method to infer $\sin^2\theta_W$, or equivalently, the W-boson mass M_W , is developed and tested using a previous CDF Run II measurement of angular distributions from electron pairs in a sample corresponding to 2.1 fb⁻¹ of integrated luminosity from $p\bar{p}$ collisions at a center-of-momentum energy of 1.96 TeV. The value of $\sin^2\theta_{\rm eff}^{\rm lept}$ is found to be 0.2328±0.0011. Within a specified context of the standard model, this results in $\sin^2\theta_W=0.2246\pm0.0011$ which corresponds to a W-boson mass of $80.297\pm0.055~{\rm GeV}/c^2$, in agreement with previous determinations in electron-position collisions and at the Tevatron collider.

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I. INTRODUCTION

The angular distribution of electrons from the Drell-Yan [1] process is used to measure the electroweak-mixing parameter $\sin^2\theta_W$ [2]. At the Tevatron, Drell-Yan pairs are produced by the process $p\bar{p}\to e^+e^-+X$, where the e^+e^- pair is produced through an intermediate γ^*/Z boson, and X is the hadronic final state associated with the production of the boson. In the standard model, the Drell-Yan process at the Born level is described by two parton-level amplitudes:

$$q\bar{q} \to \gamma^* \to e^+e^-$$
, and $q\bar{q} \to Z \to e^+e^-$.

The fermions (f) couple to the virtual photon via a vector coupling, $Q_f \gamma_\mu$, where Q_f is the fermion charge (in units of e). The fermion coupling to Z bosons consists of both vector (V) and axial-vector (A) couplings: $g_V^f \gamma_\mu + g_A^f \gamma_\mu \gamma_5$. The Born-level couplings are

$$g_V^f = T_3^f - 2Q_f \sin^2 \theta_W$$

$$g_A^f = T_3^f,$$

where T_3^f is the third component of the fermion weak isospin. The $\sin^2 \theta_W$ parameter is related to the W-boson mass M_W , and the Z-boson mass M_Z , by the relationship $\sin^2 \theta_W = 1 - M_W^2/M_Z^2$. These couplings have been investigated both at the Tevatron [3, 4], and at LEP-1 and SLD [5].

In this article, the parameter $\sin^2 \theta_W$ is inferred from a previous measurement [6] of the angular distribution of Drell-Yan e^+e^- pairs produced at the Tevatron. The

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measurement investigates higher-order quantum chromodynamic (QCD) corrections to the angular distribution, using electron pairs in the Z-boson region 66–116 GeV/ c^2 from 2.1 fb^{-1} of collisions. This analysis utilizes the results of that measurement to test a new method to ob $tain sin^2 \theta_W$. Section II provides an overview of both the electron angular distributions and the method used to obtain $\sin^2 \theta_W$. Section III discusses QCD calculations required by the new method. A technique to use and incorporate electroweak radiative-correction form factors for high-energy e^+e^- collisions into the Drell-Yan process is presented. Section IV reviews and documents the event sample, simulation of the data, and methods used in the previous measurement, and describes how the measurement is used in this analysis. Section V describes the systematic uncertainties. Finally, Sec. VI gives the results, and Sec. VII the summary. The units $\hbar = c = 1$ are used for equations and symbols, but standard units are used for numerical values.

II. ELECTRON ANGULAR DISTRIBUTIONS

The angular distribution of electrons in the boson rest frame is governed by the polarization state of the γ^*/Z boson. In amplitudes at higher order than tree level, initial-state QCD interactions of the colliding partons impart transverse momentum, relative to the collision axis, to the γ^*/Z boson. This affects the polarization states.

The polar and azimuthal angles of the e^- in the rest frame of the boson are denoted as ϑ and φ , respectively. For this analysis, the ideal positive-z axis coincides with the direction of the incoming quark so that ϑ parallels the definition used in e^+e^- collisions at LEP [5]. This frame is approximated by the Collins-Soper (CS) rest frame [7] for $p\bar{p}$ collisions. The CS frame is reached from the laboratory frame via a Lorentz boost along the laboratory z axis into a frame where the z component of the lepton-pair momentum is zero, followed by a boost along the transverse momentum of the pair. The transverse momentum (P_T) in a reference frame is the magnitude of momentum transverse to the z axis. Within the CS frame, the z axis for the polar angle is the angular bisector between the proton direction and the negative of the anti-proton direction. The x axis for the azimuthal angle is the direction of the lepton-pair $P_{\rm T}$. At $P_{\rm T}=0$, the CS and laboratory coordinate systems are the same, and if the incoming quark of the Drell-Yan parton amplitude is from the proton, the z axis and quark directions coincide.

The general structure of the Drell-Yan lepton angular distribution in the boson rest frame consists of nine

helicity cross sections [8],

$$\frac{dN}{d\Omega} \propto (1 + \cos^2 \vartheta) +$$

$$A_0 \frac{1}{2} (1 - 3\cos^2 \vartheta) +$$

$$A_1 \sin 2\vartheta \cos \varphi +$$

$$A_2 \frac{1}{2} \sin^2 \vartheta \cos 2\varphi +$$

$$A_3 \sin \vartheta \cos \varphi +$$

$$A_4 \cos \vartheta +$$

$$A_5 \sin^2 \vartheta \sin 2\varphi +$$

$$A_6 \sin 2\vartheta \sin \varphi +$$

$$A_7 \sin \vartheta \sin \varphi .$$

The A_{0-7} coefficients are cross section ratios, and are functions of the boson kinematic variables. They vanish at $P_{\rm T}=0$, except for the electroweak part of A_4 responsible for the forward-backward e^- asymmetry in $\cos\vartheta$. The A_{5-7} coefficients appear at second order in the QCD strong coupling, α_s , and are small in the CS frame [8]. Hereafter, the angles (ϑ, φ) and the angular coefficients A_{0-7} are specific to the CS rest frame.

The $A_4\cos\vartheta$ term is parity violating, and is due to vector and axial-vector current amplitude interference. Its presence adds an asymmetry to the φ -integrated $\cos\vartheta$ cross section. Two sources contribute: the interference between the Z-boson vector and axial-vector amplitudes, and the interference between the photon vector and Z-boson axial-vector amplitudes. The asymmetric component from the γ -Z interference cross section is proportional to g_A^f . The asymmetric component from Z boson self-interference has a coupling factor that is a product of g_V^f/g_A^f from the electron and quark vertices, and thus is related to $\sin^2\theta_W$. At the Born level, this product is

$$(1-4|Q_e|\sin^2\theta_W)(1-4|Q_q|\sin^2\theta_W),$$

where e and q denote the electron and quark, respectively. For the Drell-Yan process, the quarks are predominantly light quarks: u, d, or s. As $\sin^2\theta_{\rm W}\approx 0.223$, the electron contribution is small (≈ 0.1), while the quark quark contribution is larger (≈ 0.4 for the u quark and ≈ 0.7 for the d and s quarks). The smallness of the electron factor (containing Q_e) relative to the quark factor (containing Q_q) enhances the sensitivity to $\sin^2\theta_{\rm W}$ at the electron-Z vertex. Loop and vertex electroweak-radiative corrections are multiplicative form-factor corrections to the couplings that change their value by a few percent.

Traditionally, $\sin^2 \theta_W$ is inferred from the forward-backward asymmetry of the $e^-\cos\vartheta$ distribution as a function of the dielectron-pair mass. The new method for the inference of $\sin^2 \theta_W$ has two inputs: an experimental measurement of the A_4 angular-distribution coefficient, and predictions of the A_4 coefficient for various input values of $\sin^2 \theta_W$. Electroweak and QCD radiative corrections are included in the predictions of the A_4 coefficient.

The new method to infer $\sin^2 \theta_W$ utilizes the value of the cross-section weighted average, \bar{A}_4 , for both the experimental input and predictions. The average is

$$\bar{A}_4 = \frac{1}{\sigma} \int_{-\infty}^{\infty} dy \int_0^{\infty} dP_{\mathrm{T}}^2 \int dM \ A_4 \frac{d^3 \sigma}{dy dP_{\mathrm{T}}^2 dM},$$

where σ is the integrated cross-section, and y, $P_{\rm T}$, and M are the lepton-pair rapidity, transverse momentum, and mass, respectively. The energy and momentum of particles are denoted as E and P, respectively. For a given coordinate frame, the rapidity is $y=\frac{1}{2}\ln[\,(E+P_{\rm z})/(E-P_{\rm z})\,]$, where $P_{\rm z}$ is the component of momentum along the z axis of the coordinate frame. The mass integration is limited to the Z-boson region 66–116 GeV/ c^2 .

The experimental input for the \bar{A}_4 coefficient is derived from a previous measurement of the angular-distribution coefficients A_0 , A_2 , A_3 , and A_4 , in independent ranges of the dielectron-pair $P_{\rm T}$ [6]. In this analysis, the individual measurements for the A_4 coefficient are combined into an average. The predictions provide the relationship between $\sin^2\theta_W$ and \bar{A}_4 . The QCD predictions of \bar{A}_4 include an implementation of electroweak radiative corrections derived from an approach adopted at LEP [9].

III. ENHANCED QCD PREDICTIONS

Drell-Yan process calculations with QCD radiation do not typically include the full electroweak-radiative corrections. However, the QCD, quantum electrodynamic (QED), and weak corrections can be organized to be individually gauge invariant so that they can be applied separately and independently.

QED radiative corrections with photons in the final state are not included in the calculation of the \bar{A}_4 coefficient. Instead, they are applied in the physics and detector simulation of the Drell-Yan process used in the measurement of the A_4 coefficients. For the process $q\bar{q} \to e^+e^-$, QED final-state radiation is most important, and is included. The effects of QED radiative corrections are removed from the measurement of the A_4 coefficients.

The Drell-Yan process and the production of quark pairs in high energy e^+e^- collisions are analog processes: $q\bar{q}\to e^-e^+$ and $e^-e^+\to q\bar{q}$. At the Born level, the process amplitudes are of the same form except for the interchange of the electron and quark labels. Electroweak radiative corrections, calculated and extensively used for precision fits of LEP-1 and SLD measurements to the standard model [5], can be applied to the Drell-Yan process.

In the remainder of this section, the technique used to incorporate independently calculated electroweak radiative corrections for e^+e^- collisions into existing QCD calculations for the Drell-Yan process is presented. The results of the QCD calculations for the value of the \bar{A}_4 coefficient are also presented.

A. Electroweak radiative corrections

The effects of electroweak radiative corrections are incorporated into Drell-Yan QCD calculations via form factors for fermion-pair production in e^+e^- collisions, $e^+e^- \to Z \to f\bar{f}$. The form factors are calculated by zfitter 6.43 [9], which is used with LEP-1 and SLD measurement inputs for standard-model tests [5]. It is a semi-analytical calculation for fermion-pair production and radiative corrections for high-energy e^+e^- collisions. The set of radiative corrections in each form factor is gauge invariant. Thus it includes W-boson loops in the photon propagator and Z propagators at fermion-photon vertices. Consequently, the weak and QED corrections are separately gauge invariant. The renormalization scheme used by zfitter is the on-shell scheme [10], where particle masses are on-shell, and

$$\sin^2 \theta_W = 1 - M_W^2 / M_Z^2 \tag{1}$$

holds to all orders of perturbation theory by definition. Since the Z-boson mass is accurately known (to ± 0.0021 GeV/ c^2 [5]), the inference of $\sin^2 \theta_W$ is equivalent to an indirect W-boson mass measurement.

Form factors calculated by ZFITTER are stored for later use in QCD calculations. Details of the form-factor calculation with its specific standard-model assumptions and parameters are presented in Appendix A. The calculated form factors are ρ_{eq} , κ_e , κ_q , and κ_{eq} , where the label e denotes an electron, and q a quark. As the calculations use the massless-fermion approximation, the form factors only depend on the charge and weak isospin of the fermions. Consequently, the stored form factors are distinguished by three labels: e (electron type), u (up-quark type), and d (down-quark type). The form factors are complex valued, and functions of the $\sin^2\theta_W$ parameter and the Mandelstam s variable of the $e^+e^- \to Z \to f\bar{f}$ process.

The first three form factors can be trivially incorporated into the $q\bar{q}\to Z\to e^+e^-$ interaction currents. The Born-level g_A^f and g_V^f couplings within the currents are replaced with

$$g_V^f \to \sqrt{\rho_{eq}} (T_3^f - 2Q_f \kappa_f \sin^2 \theta_W), \text{ and}$$

 $g_A^f \to \sqrt{\rho_{eq}} T_3^f,$

where f=e or q. The resulting electron-quark currentcurrent interaction amplitude contains a term proportional to $\kappa_e \kappa_q \sin^4 \theta_W$. However, as this is an approximation of the desired coefficient, $\kappa_{eq} \sin^4 \theta_W$, a further correction to the amplitude (which is discussed in Sec. III B) is required.

The combination $\kappa_f \sin^2 \theta_W$, called an effective-mixing parameter, is directly accessible from measurements of the asymmetry in the $\cos \vartheta$ distribution. However, neither the $\sin^2 \theta_W$ parameter nor the form factors can be inferrred from experimental measurements without the standard model. The effective-mixing parameters are denoted as $\sin^2 \theta_{\rm eff}$ to distinguish them from the on-shell

definition of $\sin^2 \theta_W$ (Eq. (1)). The Drell-Yan process is most sensitive to the parameter $\sin^2 \theta_{\rm eff}$ of the lepton vertex, or $\kappa_e \sin^2 \theta_W$, which is commonly denoted as $\sin^2 \theta_{\rm eff}^{\rm lept}$. At the Z pole, κ_e is independent of the quark type. For comparisons with other measurements, the value of $\sin^2 \theta_{\rm eff}^{\rm lept}$ at the Z pole ${\rm Re} \, \kappa_e(s_Z) \sin^2 \theta_W \, (s_Z = M_Z^2)$, is used.

Only the photon self-energy correction from fermion loops is used with the ZFITTER Z-amplitude form factors. The self-energy correction is a complex-valued form factor of the photon propagator, and its effect is often described as the running of the electromagnetic interaction coupling.

B. QCD calculations

The Drell-Yan QCD calculations are improved by incorporating the ZFITTER form factors into the process amplitude. This provides an enhanced Born approximation (EBA) to the electroweak terms of the amplitude. The QED photon self-energy correction is included as part of the EBA. The photon amplitude influences the shape of A_4 away from the Z pole via its interference with the axial-vector part of the Z amplitude. The γ -Z interference, whose cross section is proportional to $(s-M_Z^2)$, begins to dominate the total-interference cross section away from the Z pole. As it dilutes measurements of $\sin^2\theta_{\rm eff}$, photonic corrections also need to be included.

The ZFITTER form factors, ρ_{eq} , κ_e , and κ_q are inserted into the Born g_A^f and g_V^f couplings for the Drell-Yan process. To accomodate the κ_{eq} form factor, a correction term proportional to the $(\kappa_{eq} - \kappa_e \kappa_q)$ form factor is added to the Born amplitude. The photon self-energy correction is incorporated with the photon propagator in the amplitude. Complex-valued form factors are used in the amplitude. Operationally, only the electroweak-coupling factors in the QCD cross sections are affected. To be consistent with the standard LEP Z-boson resonant line shape, the Z-boson propagator is defined as in A_q (Eq. (A1)). The total-decay width Γ_Z , calculated with ZFITTER is also used.

A leading-order (LO) QCD or tree calculation of \bar{A}_4 for the process, $p\bar{p}\to\gamma^*/Z\to e^+e^-$, is used as the baseline EBA calculation with zfitter form factors. It is used to provide a reference for the sensitivity of \bar{A}_4 to QCD radiation. The CT10 [11] next-to-leading-order (NLO) parton distribution functions (PDF) provide the incoming parton flux used in all QCD calculations discussed in this section except where specified otherwise. The EBA calculation using zfitter form-factor tables is developed for this analysis. The EBA implementation of the form factors in the tree calculation is tested against zgrad, a LO QCD calculation with electroweak radiative corrections. Only expected differences are found. The details of the tests are in Appendix B.

Two NLO calculations, RESBOS [12] and the POWHEG-BOX framework [13], are modified to be EBA-based QCD

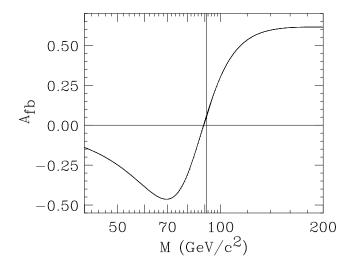


FIG. 1. Value of $A_{\rm fb}$ as a function of mass as resulting from a tree-level calculation with $\sin^2\theta_W=0.223$. The horizontal line corresponds to $A_{\rm fb}=0$ and the vertical line corresponds to $M=M_Z$.

calculations. For both calculations, the boson $P_{\rm T}^2$ distribution is finite as $P_{\rm T}^2$ vanishes. The RESBOS calculation combines a NLO fixed-order calculation at high boson- $P_{\rm T}$ with the Collins-Soper-Sterman resummation formalism [14] at low boson- $P_{\rm T}$, which is an all-orders summation of large terms from gluon emission. The RESBOS calculation uses CTEQ6.6 [15] NLO PDFs. The POWHEG-BOX is a fully unweighted partonic-event generator that implements Drell-Yan production of ee-pairs at LO and NLO. The NLO production implements a Sudakov form factor that controls the infrared diverence at low $P_{\rm T}$, and is constructed to be interfaced with parton showering to avoid double counting. The PYTHIA 6.41 [16] parton-showering algorithm is used to produce the final hadron-level event.

At tree level, the electron angular-distribution coefficient A_4 is a function of the ee-pair rapidity (y) and mass (M): $A_4(y, M)$. The mass dependence is significant, and typically represented as the forward-backward asymmetry in $\cos \vartheta$,

$$A_{\rm fb}(M) = \frac{\sigma^+(M) - \sigma^-(M)}{\sigma^+(M) + \sigma^-(M)} = \frac{3}{8} A_4(M) ,$$

where $\sigma^+(M)$ is the total cross section for $\cos \vartheta > 0$, and $\sigma^-(M)$ is the cross section for $\cos \vartheta < 0$. Figure 1 shows the typical behavior of $A_{\rm fb}(M)$. At $M = M_Z$, the asymmetry $A_{\rm fb}$ originates purely from Z bosons, and is sensitive to $\sin^2 \theta_{\rm eff}$.

Beyond leading order, the angular coefficients begin to depend on the boson $P_{\rm T}$, i.e., $A_4(y,M,P_{\rm T})$. The projections $A_4(y)$ and $A_4(P_{\rm T})$ for $66 < M < 116~{\rm GeV}/c^2$ are approximately constant except at the extremes of large |y| or $P_{\rm T}$. The POWHEG-BOX events are post-processed by the PYTHIA parton showering, which adds additional boson $P_{\rm T}$, i.e., higher-order QCD corrections. While the angular-distribution coefficients of the POWHEG-BOX

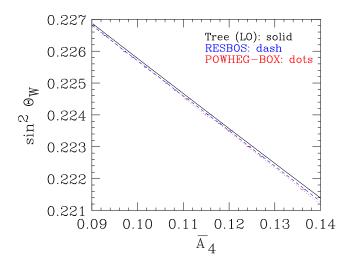


FIG. 2. Dependence of $\sin^2 \theta_W$ on \bar{A}_4 for various $\sin^2 \theta_W$ values from different QCD calculations. The tree calculation is represented by the solid (black) curve, the RESBOS calculation is represented by the dashed (blue) curve, and the POWHEGBOX NLO calculation is represented by the dotted (red) curve.

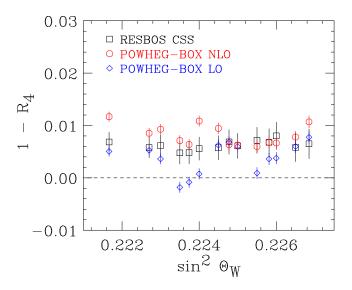


FIG. 3. $1 - R_4$ as a function of $\sin^2 \theta_W$. The open squares, circles, and diamonds correspond to the RESBOS, POWHEGBOX NLO, and POWHEGBOX LO calculations, respectively. The POWHEGBOX LO prediction includes higher-order QCD corrections from the parton-showering algorithm of PYTHIA.

LO events with PYTHIA parton showering and the NLO-based coefficients are similar at low $P_{\rm T}$, they can differ at large $P_{\rm T}$.

The tree and NLO calculations of the \bar{A}_4 coefficient for various input values of $\sin^2\theta_W$ are shown in Fig. 2. To quantify the effects of higher-order QCD corrections on \bar{A}_4 , the ratio $R_4 = \bar{A}_4(\text{NLO})/\bar{A}_4(\text{tree})$ is used, where NLO and tree denote \bar{A}_4 evaluated at NLO and at the tree level, respectively. Figure 3 shows the fractional difference $1-R_4$ for the RESBOS and POWHEG-BOX calcula-

TABLE I. Measured angular coefficients [6]. The first contribution to the uncertainty is statistical, and the second systematic. The lepton-pair mass range is restricted to 66–116 ${\rm GeV}/c^2$, and the mean lepton-pair $P_{\rm T}$ values of the events in the five bins are 4.8, 14.1, 26.0, 42.9, and 73.7 ${\rm GeV}/c$, respectively.

spectively.		
$P_{\rm T}$ bin (GeV/c)	$A_0 \ (\times 10^{-1})$	$A_2 (\times 10^{-1})$
0–10	$0.17 \pm 0.14 \pm 0.07$	$0.16 \pm 0.26 \pm 0.06$
10-20	$0.42 \pm 0.25 \pm 0.07$	$-0.01 \pm 0.35 \pm 0.16$
20 - 35	$0.86 \pm 0.39 \pm 0.08$	$0.52 \pm 0.51 \pm 0.29$
35 - 55	$3.11 \pm 0.59 \pm 0.10$	$2.88 \pm 0.84 \pm 0.19$
> 55	$4.97 \pm 0.61 \pm 0.10$	$4.83 \pm 1.24 \pm 0.02$
$P_{\rm T}$ bin (GeV/c)	$A_3 \ (\times 10^{-1})$	$A_4 \ (\times 10^{-1})$
$\frac{P_{\rm T} \operatorname{bin} (\operatorname{GeV}/c)}{0 - 10}$	$A_3 (\times 10^{-1}) \\ -0.04 \pm 0.12 \pm 0.01$	$A_4 \ (\times 10^{-1})$ $1.10 \pm 0.10 \pm 0.01$
		, ,
0–10	$-0.04 \pm 0.12 \pm 0.01$	$1.10 \pm 0.10 \pm 0.01$
0–10 10–20	$-0.04 \pm 0.12 \pm 0.01$ $0.18 \pm 0.16 \pm 0.01$	$1.10 \pm 0.10 \pm 0.01$ $1.01 \pm 0.17 \pm 0.01$
0-10 10-20 20-35	$-0.04 \pm 0.12 \pm 0.01 \\ 0.18 \pm 0.16 \pm 0.01 \\ 0.14 \pm 0.24 \pm 0.01$	$ \begin{aligned} 1.10 &\pm 0.10 \pm 0.01 \\ 1.01 &\pm 0.17 \pm 0.01 \\ 1.56 &\pm 0.26 \pm 0.01 \end{aligned} $

tions with various values of $\sin^2 \theta_W$. Higher-order QCD corrections do not significantly alter \bar{A}_A with respect to its value from tree-level amplitudes.

The RESBOS and POWHEG-BOX NLO calculations are similar and consistent. The RESBOS calculation is chosen as the default EBA-based QCD calculation of \bar{A}_4 with various input values of $\sin^2\theta_W$. As the POWHEG-BOX NLO program has a diverse and useful set of calculation options, it is used to estimate QCD systematic uncertainties.

IV. EXPERIMENTAL INPUT TO $ar{A}_4$

The value of the A_4 angular-distribution coefficient is derived from the previous measurement of electron angular-distribution coefficients [6]. Elements of the measurement are summarized in this section for completeness and supplemental documentation.

The coefficients A_0 , A_2 , A_3 , and A_4 are measured in the CS rest frame and in independent ranges of the dielectron-pair $P_{\rm T}$. These measurements are reproduced in Table I, and are derived from a $p\bar{p}$ collision sample corresponding to an integrated luminosity is 2.1 fb⁻¹. The data and simulation are understood, and the modeling of the data in the simulation is accurate. The measurement of the angular coefficients is data driven, and fully corrected for acceptance and detector resolution.

The description of the data simulation, Sec. IV A, is presented before the description of the event sample, Sec. IV B, to aid in the discussion of the data-driven corrections to the simulation. Section IV C describes the method used to measure the angular coefficients, A_0 , A_2 , A_3 , and A_4 in independent ranges of the dielectron-pair $P_{\rm T}$. Finally, Sec. IV D describes the method used to average the previous independent measurements of A_4 , and to estimate the uncertainties on the combination.

A. Data simulation

Drell-Yan pair production is simulated using the Monte Carlo event generator, PYTHIA [17], and CDF II detectorsimulation programs. This simulation is only used for the measurement of the angular coefficients. PYTHIA generates the hard, leading-order QCD interaction, q + $\bar{q} \rightarrow \gamma^*/Z$, simulates initial-state QCD radiation via its parton-shower algorithms, and generates the decay $\gamma^*/Z \rightarrow l^+l^-$. The CTEQ5L [18] nucleon partondistribution functions are used in the QCD calculations. The underlying event and boson $P_{\rm T}$ parameters are from PYTHIA tune AW (i.e., PYTUNE 101, which is a tuning to previous CDF data) [17, 19, 20]. In addition, Pho-TOS 2.0 [21, 22], adds final-state QED radiation to decay vertices with charged particles (e.g. $\gamma^*/Z \rightarrow ee$). The parton-shower simulation of PYTHIA uses a QCD resummation calculation. The resulting physics model is adequate to allow data-driven adjustments to the underlying angular-distribution coefficients and other physics distributions.

The measurement of the electron angular coefficient depends on the correct modeling of the physics and both the detector acceptance and efficiency. All data efficiencies, global and particle-trajectory dependent, as well as time-dependent, are measured in the data and incorporated into the simulation. The simulation also uses the calorimeter energy scales and resolutions measured in the data. The data-driven approach is iterative with simultaneous tuning of both the generator physics-model distributions and the detector-modeling parameters that make the distributions of reconstructed quantities of simulated events match the data precisely.

The PHOTOS program generates multiple photons at the $\gamma^*/Z \to ee$ vertex via a form factor to the production cross section. Soft and collinear photons are simulated to α_{em}^2 leading-logarithmic accuracy, where α_{em} is the fine-structure constant. The simulation of hard, noncollinear photon emission is a full α_{em} matrix-element algorithm, except that the interference terms are removed to make the algorithm process-independent [22]. For the $\gamma^*/Z \to ee$ process, the interference terms are restored in an approximate way. The real and virtual photonemission cross-section infrared divergences at each order are regularized and analytically combined to cancel the divergences. Photons with energies smaller than the default regularization energy are not generated.

In addition to QCD initial-state radiation, PYTHIA adds initial- and final-state QED radiation via its parton-showering algorithm. The regularization-energy threshold is very low, and most of the photons are very soft. This threshold is lower than the one in PHOTOS, so the soft-photon emission of PYTHIA is complementary to the hard-photon emission of PHOTOS.

The default implementation of PYTHIA plus PHOTOS (PYTHIA+PHOTOS) QED radiation in the CDF datasimulation infrastructure is validated with ZGRAD2 [23], a leading-order QCD Drell-Yan calculation with a $\mathcal{O}(\alpha_{em})$ matrix-element calculation for the emission of zero or one real photon. It includes both initial-state and final-state radiation. As ZGRAD2 has soft and collinear photon-regularization regions for the cancellation of divergences, these regions are excluded from comparisons with PYTHIA+PHOTOS. The $e^+e^- + n\gamma$ systems are boosted to their center-of-momentum frames to minimize distortions to the electron and photon kinematic distributions from QCD (QED) initial-state radiation. simplify the comparison of the multi-photon system of PYTHIA+PHOTOS to the single photon of ZGRAD2, the multi-photon system is clustered by adding up the photon momentum vectors. Good agreement is observed between PYTHIA+PHOTOS and ZGRAD2 in the photonenergy distributions and angular distibutions of the photon (cluster) with respect to the nearest e^+ or e^- .

B. Measurement event sample

The CDF experimental apparatus is a general-purpose detector [24] at the Fermilab Tevatron $p\bar{p}$ collider whose center-of-momentum (cm) energy is 1.96 TeV. The positive z-axis is directed along the proton direction. For particle trajectories, the polar angle $\theta_{\rm cm}$ is relative to the proton direction and the azimuthal angle $\phi_{\rm cm}$ is oriented about the beamline axis with $\pi/2$ being vertically upwards. The component of the particle energy transverse to the beamline is defined as $E_{\rm T} = E \sin \theta_{\rm cm}$. The pseudorapidity of a particle trajectory is $\eta = -\ln \tan(\theta_{\rm cm}/2)$. Detector coordinates are specified as $(\eta_{\rm det}, \phi_{\rm cm})$, where $\eta_{\rm det}$ is the pseudorapidity relative to the detector center (z=0).

central charged-particle tracking-detector (tracker) is a 3.1 m long, open-cell drift chamber [25] that radially extends from 0.4 to 1.4 m. Between the Tevatron beam pipe and the central tracker is a 2 m long silicon vertex-tracker [26–28]. Both trackers are immersed in a 1.4 T axial magnetic field. Outside the central tracker is a central barrel calorimeter [29, 30] that covers the region $|\eta_{\rm det}| < 1.1$. The forward end-cap regions are covered by the end-plug ("plug") calorimeters [31-33] that cover the regions $1.1 < |\eta_{\rm det}| < 3.5$. Both the central and plug calorimeters are segmented into electromagnetic and hadronic sections. The electromagnetic sections of both calorimeters have preshower and shower-maximum detectors for electron identification. The silicon tracker, in conjunction with the plug shower-maximum detector, provides tracking coverage in the plug region to $|\eta_{\text{det}}|$ of about 2.8. As $|\eta_{\text{det}}|$ increases for plug-region tracks, the transverse track length within the magnetic field decreases, resulting in increasingly poorer track-curvature resolutions.

Events are required to contain two electron candidates having a pair mass in the Z-boson region of 66–116 $\,\mathrm{GeV}/c^2$. Electrons in both the central and plug calorimeters are used. The events are classified into three dielectron topologies: CC, CP, and PP, where C (P) de-

notes that the electron is detected in the central (plug) calorimeter. Electrons are required to have an associated track, pass standard selection and fiducial requirements [24], and be isolated from other calorimeter activity. The electron kinematic variables are based on the electron energy measured in the calorimeters and the track direction. The kinematic and fiducial regions of acceptance for electrons in the three topologies are summarized below.

- 1. Central-Central (CC)
 - $E_{\rm T} > 25$ (15) GeV for electron 1 (2)
 - $0.05 < |\eta_{\rm det}| < 1.05$
- 2. Central-Plug (CP)
 - $E_{\rm T} > 20~{\rm GeV}$ for both electrons
 - Central electron: $0.05 < |\eta_{\rm det}| < 1.05$
 - Plug electron: $1.2 < |\eta_{\rm det}| < 2.8$
- 3. Plug-Plug (PP)
 - $E_{\rm T} > 25~{\rm GeV}$ for both electrons
 - $1.2 < |\eta_{\text{det}}| < 2.8$

The CC-electron $E_{\rm T}$ selection is asymmetric, with electron 1 having the highest $E_{\rm T}$. The asymmetric selection, an optimization from the previous measurement of electron angular-distribution coefficients, improves the acceptance in the electron phase space [6]. The PP-electron candidates, required to be in the same end of the CDF II detector, extend the rapidity coverage to $|y|\approx 2.9$. The kinematic limit of |y| for the production of ee-pairs at the Z-boson mass is 3.1. The acceptance is limited for PP-topology Drell-Yan electrons on opposite ends of the CDF II detector; the dielectrons tend to be at low ee-pair rapidities, and are overwhelmed by the QCD di-jet backgrounds.

The numbers of events passing all requirements in the CC, CP, and PP topologies are 51 951, 63 752, and 22 469, respectively. All requirements in the association of charged-particle tracks to both final-state electrons significantly reduces the backgrounds coming from QCD, the electroweak (EWK) processes of WW, WZ, ZZ, $t\bar{t}$, W+jets, and also $Z \to \tau^+\tau^-$. The QCD background is primarily from dijets where a particle in a jet is misidentified as an electron or is an electron from a photon conversion. The high- $E_{\rm T}$ electron sources have at least one real electron. The second electron is either a real second electron or a fake one. The backgrounds and the methods used to determine them are described further in previous measurements [6, 34]. The QCD backgrounds, determined from the same dielectron sample used for the measurement, constitute 0.3% of the sample. The EWK backgrounds are derived from PYTHIA [17] samples with detector simulation, and amount to 0.2%. The fraction of QCD plus EWK backgrounds is approximately constant over $\cos \vartheta$ for each topology. Background-subtracted distributions are used in measurements.

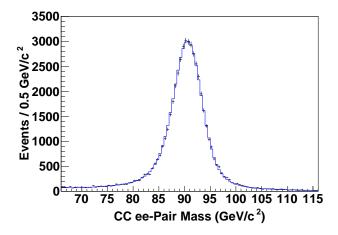


FIG. 4. The CC-topology *ee*-pair mass distribution. The crosses are the data and the histogram is the simulation.

The online-event selection and electron-identification efficiencies are measured as functions of $\eta_{\rm det}$ for both central and plug electrons. The measured efficiencies are incorporated in the simulation as scale factors (event weights). Plug-electron efficiencies are separately measured for the CP and PP electrons. A significant fraction of the PP-toplology electrons are in more forward regions of the calorimeter relative to those of the CP topology. The efficiencies for electrons to be identified in the plug calorimeter particularly in the very forward regions, have a significant time-dependence (due to increasing instantaneous luminosities) which are measured and incorporated into the simulation.

Corrections to the simulated-event electron energy-scales and resolutions are determined using both the eepair mass and electron- $E_{\rm T}$ distributions. The energy scales and resolutions of the simulation are adjusted so that both the simulated-electron $E_{\rm T}$ distributions and the ee-pair mass distributions are matched to the observed distributions [34]. The central- and plug-electron energy scales are accurately constrained by the three independent ee-pair topologies. Figures 4, 5, and 6 show the ee-pair mass distributions for the CC, CP, and PP topologies, respectively. The simulated-data to data χ^2 for the CC-, CP-, and PP-topology ee-pairs are 117, 126, and 127, respectively, for 100 bins. The event count of the simulated data is normalized to that of the data, and only statistical uncertainties are used in the calculation.

The Collins-Soper frame angle, $\cos \vartheta$ [7], is reconstructed using these laboratory-frame quantities: the lepton energies (E), the lepton momenta along the beam line (P_z) , the dilepton mass (M), and the dilepton transverse momentum (P_T) . The angle of the negatively-charged lepton is

$$\cos \vartheta = \frac{l_+^- l_-^+ - l_-^- l_+^+}{M \sqrt{M^2 + P_{\rm T}^2}} ,$$

where $l_{\pm}=(E\pm P_z)$ and the + (–) superscript specifies that l_{\pm} is for the positively- (negatively-)charged

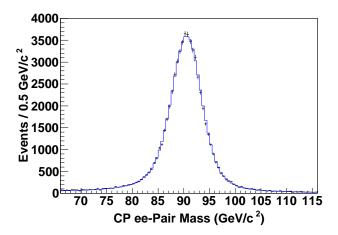


FIG. 5. The CP-topology ee-pair mass distribution. The crosses are the data and the histogram is the simulation.

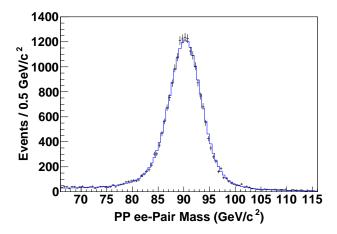


FIG. 6. The PP-topology ee-pair mass distribution. The crosses are the data and the histogram is the simulation.

lepton. A similar expression is used for φ . For plug electrons, charge identification is not used because of significant charge misidentification probability at large $|\eta_{\rm det}|$. As an interchange of the e^- with the e^+ changes the sign of $\cos\vartheta$, $|\cos\vartheta|$ is used for the PP-topology dielectrons. For CP-topology dielectrons, the central-electron charge determines whether the e^- is the central or plug electron. For the CC- and CP-topology dielectrons, the charge-misidentification probabilities are 0.3% and 0.4% respectively.

The $\cos\vartheta$ bias and resolution of the observed events are estimated using the simulation. The bias $\Delta\cos\vartheta$, is the difference between the true $\cos\vartheta$ before final-state QED radiation and the measurement. The $\Delta\cos\vartheta$ distribution is affected by the electron-energy resolution of the calorimeters and electron-charge misidentification. The effect of calorimeter energy-resolution smearing is small for all dielectron topologies. The bias distribution has a narrow non-Gaussian central core centered at zero with less than 1% rms deviation. The calorimeters have a negligible effect on the mean of the bias but dominate the

resolution. Charge misidentification in the CC- and CP-dielectron topologies contributes a relatively flat background with a negligible bias.

C. Angular coefficient measurement

The angular distribution integrated over φ is

$$N(\vartheta, A_0, A_4) \propto 1 + \cos^2 \vartheta + A_0 \frac{1}{2} (1 - 3\cos^2 \vartheta) + A_4 \cos \vartheta.$$
 (2)

In each $P_{\rm T}$ bin, this distribution is modified by the acceptance and resolution of the detector into the observed $\cos \vartheta$ distribution. The simulated events used to model the $\cos \vartheta$ distribution are selected as data. The underlying A_0 and A_4 values in the simulation physics model are simultaneously varied until the simulated $\cos \vartheta$ distributions match the corresponding data distributions. The variation is accomplished with an event weight

$$w = \frac{N(\vartheta, A_0', A_4')}{N(\vartheta, A_0, A_4)}.$$

The base physics-model angular coefficients are denoted as A_0 and A_4 , and variations to them are denoted as A_0' and A_4' . The best-fit values for A_0' and A_4' are determined using a binned log-likelihood fit between the data and simulation. The event normalization of the simulation sample relative to the data is a parameter in the log-likelihood fit as the detector acceptance depends on A_0 and A_4 . The log-likelihood of each dielectron topology is separately evaluated and then combined into a joint probability-density function.

The best-fit values of A_0' and A_4' for each $P_{\rm T}$ bin are incorporated into the physics model prior to the determination of φ -based angular coefficients. The angular distribution integrated over $\cos \vartheta$ is

$$N(\varphi,A_2,A_3) \propto \frac{8}{3} + \frac{2}{3}A_2 \cos 2\varphi + \frac{\pi}{2}A_3 \cos \varphi.$$

The A_5 and A_7 terms, expected to be relatively small [8], are dropped. The best-fit values to A_2 and A_3 , denoted as A_2' and A_3' respectively, are also obtained using the same method as for A_0' and A_4' . The fits to the observed $\cos \vartheta$ and φ distributions are iterated to obtain the final values of A_0' , A_1' , A_3' , and A_4' for each $P_{\rm T}$ bin. The measurements are fully corrected for detector acceptance and resolution.

D. A_4 average

The measured values of A_0 , A_2 , A_3 , and A_4 (Table I) are incorporated into the physics model. The one-dimensional $\cos \vartheta$ distribution of events with ee-pair masses in the range 66–116 GeV/ c^2 has the functional form, $N(\vartheta, \bar{A}_0, \bar{A}_4)$ (Eq. (2)). The best fit to the distribution for the functional form yields the parameters

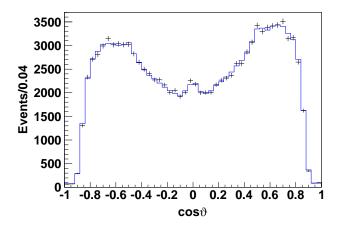


FIG. 7. The observed $\cos \vartheta$ distribution for the combined CC and CP topologies. The crosses are the background-subtracted data, and the solid histogram is the simulation.

 $\bar{A}_0 = 0.0514 \pm 0.0010$ and $\bar{A}_4 = 0.1100 \pm 0.0008$, where the uncertainties are due to the limited size of the simulated sample. These angular-coefficient parameters are the cross-section weighted averages based on the measurements.

Experimental uncertainties of \bar{A}_4 are evaluated directly from the observed and simulated $\cos \theta$ distributions of events selected for the angular-distribution measurement. There is no partitioning of events into different ranges of the ee-pair $P_{\rm T}$. A similar likelihood fit is used to determine the values of A_0 and A_4 that best describe the data. However, the variations of A_0' and A_4' are via P_{T} -independent scale factors. The best-fit values from the log-likelihood fits are $\bar{A}_0 = 0.0497 \pm 0.0073$ and $\bar{A}_4 = 0.1095 \pm 0.0079$, and the central values are consistent with the cross-section weighted averages. The uncertainties reflect the limited data-sample size. The correlation coefficient between the uncertainty of \bar{A}_4 and \bar{A}_0 or the simulation normalization is under 0.01. The angular function of the A_4 coefficient is an odd function in $\cos \theta$, and it is also orthogonal to both the angular function of the A_0 coefficient and $1 + \cos^2 \vartheta$.

The experimental value of \bar{A}_4 used to infer $\sin^2 \theta_W$ is

$$\bar{A}_4 = 0.1100 \pm 0.0079$$
,

where the central value is the cross-section weighted average, and its uncertainty is the statistical uncertainty from the log-likelihood fit.

The $\cos \vartheta$ distribution for the combined CC- and CP-topology dielectrons is shown in Fig. 7. The comparison of the simulation with the data yields a χ^2 of 44.8 for 50 bins. The yield of simulated events is determined by the fit. For the separate CC- and CP-topology $\cos \vartheta$ distributions, the comparison between the simulation and the data yields a CC-topology χ^2 of 49.0 for 50 bins, and a CP-topology χ^2 of 46.9 for 46 bins. Figure 8 shows the $\cos \vartheta$ distribution of the PP topology. The comparison of the simulation with the data yields a χ^2 of 31.7 for

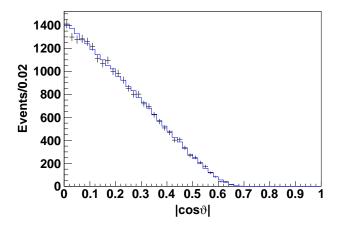


FIG. 8. The observed $|\cos \vartheta|$ distribution for the PP topology. The crosses are the background-subtracted data, and the solid histogram is the simulation.

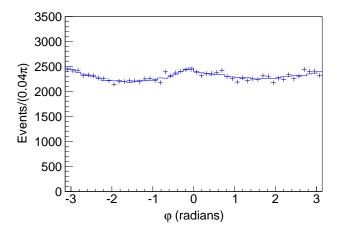


FIG. 9. The observed φ distribution for the combined CC and CP topologies. The crosses are the background-subtracted data, and the solid histogram is the simulation.

35 bins. The CC and CP topologies are the ones that mainly constrain the fit for \bar{A}_0 and \bar{A}_4 . The PP topology helps to constrain the simulation event normalization.

The observed φ distributions are also well described by the simulation. Figure 9 shows the distribution for the combined CC and CP ee-pair topologies. The comparison of the simulation with the data yields a χ^2 of 51.5 for 50 bins. For the separate CC- and CP-topology φ distributions, the χ^2 between the simulation and the data are 56.1 and 46.9, respectively, for 50 bins. Figure 10 shows the φ distribution for events in the PP topology. The comparison of simulation with the data yields a χ^2 of 47.4 for 50 bins.

V. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties on the inference of $\sin^2 \theta_W$ (or M_W) contain contributions from both the

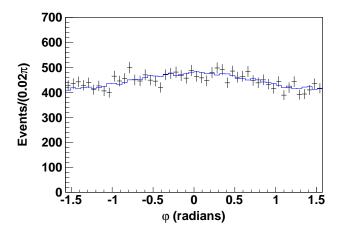


FIG. 10. The observed φ distribution of electrons for the PP topology. The crosses are the background-subtracted data, and the solid histogram is the simulation.

experimental input for \bar{A}_4 and the predictions of \bar{A}_4 for various input values of $\sin^2\theta_W$. The prediction uncertainties dominate. Both the experimental and prediction systematic uncertainties are small compared to the the experimental statistical uncertainty.

A. Experimental input

The \bar{A}_4 angular-coefficient uncertainties considered include the simulation energy scale, the background estimates, and the single-electron selection and tracking-efficiency measurements.

The central- and plug-electron energy scales for the simulation are accurately constrained by the data. Their residual uncertainties correspond to an estimated uncertainty for the \bar{A}_4 coefficient of ± 0.0003 . This is not completely independent of the experimental statistical uncertainty, but is included in quadrature with the other experimental systematic uncertainties.

The largest independent uncertainty is from the background subtraction. It is estimated by varying the fraction of the default background that is subtracted, then re-fitting the observed $\cos\vartheta$ distribution for a modified best-fit value of \bar{A}_4 . The level of background subtracted from the data is varied so that the change in the corresponding likelihood value corresponds to the nominal one-standard-deviation change of the results with respect to the central value. The result is $\Delta \bar{A}_4 = \pm 0.0003$.

The measured single-electron efficiences incorporated in the simulation have uncertainties. When propagated to the $\cos \vartheta$ bins, the fractional uncertainties of the CC, CP, and PP topologies are relatively constant. The levels of uncertainty for the CC, CP, and PP topology yields are 0.9%, 0.6%, and 4%, respectively. The PP-topology electron acceptance extends into very forward regions of the plug calorimeter, and signficantly beyond that for CP-topology electrons. As measurements are difficult in this

far forward region, the PP uncertainty is larger. Since the same single-electron measurements are used in each bin, they are treated as 100% correlated across the $\cos\vartheta$ bins. To estimate uncertainties, the overall dielectron-topology efficiency is rescaled within its uncertainty prior to log-likelihood fits of the observed $\cos\vartheta$ distribution. This is equivalent to a systematic offset in its event normalization relative to the other topologies. The uncertainty on the \bar{A}_4 coefficient from this source is found to be negligible. Because the angular function of the \bar{A}_4 coefficient $\cos\vartheta$, is odd, the normalization of the simulated events and \bar{A}_4 are nearly uncorrelated in all fits.

B. Predictions

The QCD mass-factorization and renormalization scales and uncertainties in the CT10 PDFs affect the calculated value of \bar{A}_4 . The corresponding systematic uncertainties on \bar{A}_4 are evaluated using POWHEG-BOX NLO. As the RESBOS calculation is chosen as the default for \bar{A}_4 , the associated uncertainty is also included in the overall systematic uncertainty.

In all QCD calculations, the mass-factorization and renormalization scales are both set to the *ee*-pair mass. To evaluate the effect on \bar{A}_4 from different scales, the running scales are varied independently by a factor ranging from 0.5 to 2 in the calculations. The largest observed deviation in \bar{A}_4 from the default value is the QCD-scale uncertainty. This uncertainty is $\Delta \bar{A}_4$ (QCD scale) = ± 0.0004 .

The CT10 set of 26 eigenvector pairs of uncertainty PDFs are used to evaluate the effect of PDF uncertainties on \bar{A}_4 . From each pair, the largest deviation from the default calculation for \bar{A}_4 is used as the uncertainty for the pair. The rms spread of the 26 eigenvector deviations is the PDF uncertainty, $\Delta \bar{A}_4(\text{PDF}) = \pm 0.0011$.

The default RESBOS calculation of the \bar{A}_4 coefficient for various input values of $\sin^2\theta_W$ yields coefficient values 0.5–0.8% larger than the baseline tree calculation. The POWHEG-BOX calculations are slightly different. A conservative systematic uncertainty of $\pm 1\%$ is assigned for differences, and this is denoted as the EBA uncertainty.

In summary, the total systematic uncertainty from the QCD mass-factorization and renormalization scales, and uncertainties in the CT10 PDFs is $\Delta \bar{A}_4(\text{QCD}) = \pm 0.0012$. The EBA uncertainty is $\Delta \bar{A}_4(\text{EBA}) = \pm 0.01\bar{A}_4$. These prediction uncertainties are combined in quadrature. At the measured value of \bar{A}_4 (0.1100), the total prediction uncertainty is ± 0.0017 .

VI. RESULTS

The fully-corrected value of the \bar{A}_4 coefficient for this analysis is

$$\bar{A}_4 = 0.1100 \pm 0.0079 \pm 0.0004$$

where the first contribution to the uncertainty is statistical and the second systematic. Prediction uncertainties are separated from experimental uncertainties. To be conservative, the prediction and measurement uncertainties are combined linearly for the total uncertainties of derived results which are presented in this section.

The A_4 angular coefficient is directly sensitive to the $\sin^2 \theta_{\text{eff}}$ parameter at the lepton and quark vertices of the Drell-Yan amplitude. However, it is most sensitive to the effective-mixing parameter at the lepton vertex, and consequently, the A_4 coefficient is primarily a measure of $\sin^2 \theta_{\text{eff}}^{\text{lept}}$. The standard model (SM) provides the means to express the effective-mixing parameters in terms of its static parameters and the collision dynamics, to map the correspondence between the effective-mixing parameters and the angular coefficient A_4 ,

$$SM(\sin^2 \theta_W) \stackrel{EWK}{\longmapsto} \sin^2 \theta_{eff}(s) \stackrel{QCD}{\longleftrightarrow} A_4(s),$$

and to interpret measurements of this coefficient in terms of the fundamental W-boson mass, M_W , or the $\sin^2\theta_W$ parameter. The symbol EWK denotes electroweak radiative corrections, and the symbol QCD denotes EBA-based QCD calculations. For the \bar{A}_4 coefficient, the kinematic dependencies of the $\sin^2\theta_{\rm eff}(s)$ parameters are averaged by the integration over the \sqrt{s} range of 66–116 GeV. Over this range, the predicted differences between the effective-leptonic and effective-quark mixing parameters are under 0.0005 in magnitude. The interpretation of the measured \bar{A}_4 coefficient in terms of the $\sin^2\theta_W$ or M_W parameter is interesting, but model dependent. Under different standard-model contexts, the same value of an effective-mixing parameter can be associated with different values of the $\sin^2\theta_W$ parameter.

The RESBOS predictions of \bar{A}_4 for various values of the M_W (or $\sin^2\theta_W$) parameter are shown in Fig. 11 along with the observed value. The intersection of the measured value with the prediction can be interpreted as the indirect measurement of M_W or $\sin^2\theta_W$ within the context of standard-model assumptions specified in Appendix A:

$$\sin^2 \theta_W = 0.2246 \pm 0.0011$$

 $M_W(\text{indirect}) = 80.297 \pm 0.055 \text{ GeV}/c^2,$

where the uncertainty includes both measurement and prediction uncertainties. The experimental statistical uncertainty for the value of M_W is $\pm 0.045 \,\mathrm{GeV/c^2}$. The systematic uncertainty, predominantly from the prediction, is $\pm 0.010 \,\mathrm{GeV/c^2}$. The corresponding statistical and systematic uncertainties for the value of $\sin^2\theta_W$ are ± 0.0009 and ± 0.0002 , respectively. The other W-mass measurements shown in Fig. 11 are from combinations of the Tevatron, and the LEP-1 and SLD measurements [35]:

$$M_W = 80.385 \pm 0.015 \text{ GeV}/c^2$$
, direct
= $80.365 \pm 0.020 \text{ GeV}/c^2$, Z pole,

where direct refers to the combination of LEP-2 and Tevatron W-mass measurements, and Z pole is an indirect measurement from electroweak standard-model fits

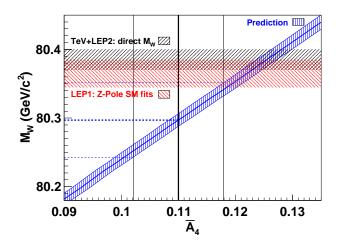


FIG. 11. Distribution of M_W as a function of the \bar{A}_4 value as predicted by RESBOS. The prediction is the solid (blue) diagonal line and its one standard-deviation limits are the bands. The \bar{A}_4 measurement is the bold vertical line, and its one standard-deviation limits are the lighter vertical lines. The hatched horizontal bands are uncertainty limits from other W-mass measurements (see text).

to LEP-1 and SLD Z-pole measurements with the topquark mass measurement. Figure 12 shows the comparison of these W-boson mass results.

The $\sin^2 \theta_W$ parameter also specifies the correspondence between the A_4 angular coefficient and the effective-mixing parameters. As the parameters are averaged in the \bar{A}_4 angular coefficient, a reference value of the effective-leptonic mixing parameter at the Z pole,

$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = \text{Re} \, \kappa_e(s_Z, \sin^2 \theta_W) \sin^2 \theta_W,$$

is provided for comparisons. Although the \bar{A}_4 coefficient is integrated across the \sqrt{s} range of 66–116 GeV, the bulk of the integrated cross section is near the vicinity of the Z pole ($s_Z = M_Z^2$). Therefore, it is an effective probe of the leptonic $\sin^2\theta_{\rm eff}$ at the reference s_Z value. The reference value of $\sin^2\theta_{\rm eff}$ corresponding to the \bar{A}_4 angular-coefficient measurement is

$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = 0.2328 \pm 0.0011,$$

where both statistical and systematic uncertanities are included. The experimental statistical uncertainty is ± 0.0009 . The systematic uncertainty, predominantly from the prediction, is ± 0.0002 . Relative to $\sin^2\theta_{\rm eff}^{\rm lept}$, the effective-mixing parameters of the *u*- and *d*-type quarks ${\rm Re}\,\kappa_{u,d}\sin^2\theta_W$ (at $s_Z)$, are lower by 0.0001 and 0.0002, respectively. The corresponding $\sin^2\theta_{\rm eff}^{\rm lept}$ measurements from LEP-1 and SLD are

$$0.23153 \pm 0.00016$$
 (Z-pole) and 0.2320 ± 0.0021 (light quarks),

where the "Z-pole" measurement is from the standard-model analysis of the combined Z-pole results, and the

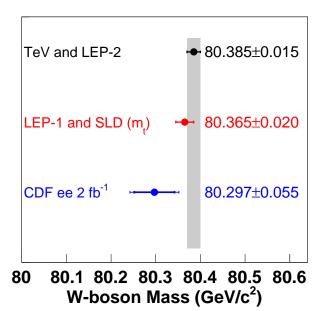


FIG. 12. Comparisons of experimental measurements of the W-boson mass: "TeV and LEP-2" represents direct measurements of the W-boson mass; "LEP-1 and SLD (m_t)" represents the standard-model analysis of Z-pole measurements; and "CDF ee 2 fb⁻¹" represents this analysis. The horizontal bars represent total uncertainties. For this analysis, the inner uncertainty bar is the measurement uncertainty.

"light quarks" measurement is from the light-quark (u, d, and s) asymmetries [5]. The previous corresponding Tevatron value from D0 derived from a measurement of $A_{\rm fb}(M)$ is $\sin^2\theta_{\rm eff}^{\rm lept} = 0.2309 \pm 0.0008 \pm 0.0006$, where the first contribution to the uncertainty is statistical and second systematic [4]. Figure 13 shows a comparison of these $\sin^2\theta_{\rm eff}^{\rm lept}$ measurements.

The admixture of light quarks in the Drell-Yan production and e^+e^- collisions is somewhat different. The contributions of the various quarks to the incoming parton flux in Tevatron $p\bar{p}$ collisions are evaluated with the CT10 PDFs at a virtuality scale of $Q=M_Z$ and at a momentum fraction of x=0.047 (corresponding to $\sqrt{s}=M_Z$). The $q\bar{q}$ fluxes of the d, s, c, and b quarks relative to the u-quark flux are 0.51, 0.06, 0.02, and 0.01, respectively.

VII. SUMMARY

The angular distribution of Drell-Yan e^+e^- pairs provides information on the electroweak-mixing parameter $\sin^2 \theta_W$. The electron forward-backward asymmetry in the polar-angle distribution $\cos \vartheta$ is governed by the $A_4 \cos \vartheta$ term, whose A_4 coefficient is directly related to the $\sin^2 \theta_{\rm eff}^{\rm lept}$ mixing parameter at the lepton vertex, and indirectly to $\sin^2 \theta_W$. A new method for the determination of $\sin^2 \theta_{\rm eff}^{\rm lept}$ using the average value of A_4 (\bar{A}_4) for ee-pairs in the Z-boson mass region of 66–116 GeV/ c^2 is

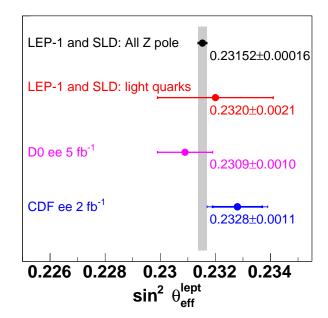


FIG. 13. Comparisons of experimental measurements of $\sin^2\theta_{\text{eff}}^{\text{lept}}$: "All Z pole" represents the LEP-1 and SLD standard-model analysis of Z-pole measurements and "light quarks" represents the LEP-1 and SLD results from the light-quark asymmetries; "D0 ee 5 fb⁻¹" represents the D0 $A_{\text{fb}}(M)$ analysis; and "CDF ee 2 fb⁻¹" represents this analysis. The horizontal bars represent total uncertainties. For this analysis, the inner uncertainty bar is the measurement uncertainty.

tested. The method utilizes standard-model calculations of \bar{A}_4 for different input values of $\sin^2\theta_W$, or equivalently, $\sin^2\theta_{\rm eff}^{\rm lept}$, for comparison with the measured value of \bar{A}_4 . These calculations include both quantum chromodynamic and electroweak radiative corrections. The result for $\sin^2\theta_W$ is equivalent to an indirect determination of the W-boson mass. However, unlike $\sin^2\theta_{\rm eff}^{\rm lept}$, the interpretation of $\sin^2\theta_W$ or the W-boson mass is dependent on the standard-model context. Using the value $\bar{A}_4=0.1100\pm0.0079$ observed in a sample corresponding to 2.1 fb⁻¹ of integrated luminosity from $p\bar{p}$ collisions at a center-of-momentum energy of 1.96 TeV,

$$\begin{split} \sin^2\theta_{\rm eff}^{\rm lept} &= 0.2328 \pm 0.0011, \\ \sin^2\theta_W &= 0.2246 \pm 0.0011, \text{ and} \\ M_W({\rm indirect}) &= 80.297 \pm 0.055 \; {\rm GeV}/c^2 \; . \end{split}$$

Each uncertainty includes statistical and systematic contributions. Both results are consistent with LEP-1 and SLD Z-pole measurements. The value of $\sin^2\theta_{\rm eff}^{\rm lept}$ is also consistent with the previous Tevatron value from D0. The results of the test for the new method are promising. As the uncertainties are predominantly statistical, the measurement will improve with the analysis of the full Tevatron sample corresponding to 9 fb⁻¹ of integrated luminosity.

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Appendix A: ZFITTER

The input parameters to the ZFITTER radiative-correction calculation are particle masses, the electromagnetic fine-structure constant α_{em} , the Fermi constant G_F , the strong coupling at the Z mass $\alpha_s(M_Z^2)$, and the contribution of the light quarks to the "running" α_{em} at the Z mass $\Delta\alpha_{em}^{(5)}(M_Z^2)$ (DALH5). The scale-dependent couplings are $\alpha_s(M_Z^2)=0.118$ and $\Delta\alpha_{em}^{(5)}(M_Z^2)=0.0275$ [36]. The mass parameters are $M_Z=91.1875~{\rm GeV}/c^2$ [5], $m_t=173.2~{\rm GeV}/c^2$ (top quark) [37], and $m_H=125~{\rm GeV}/c^2$ (Higgs boson). Form factors and the Z-boson total-decay width Γ_Z , are calculated.

The renormalization scheme used by ZFITTER is the on-shell scheme [10], where particle masses are on-shell, and

$$\sin^2 \theta_W = 1 - M_W^2 / M_Z^2$$

holds to all orders of perturbation theory by definition. If both G_F and m_H are specified, $\sin\theta_W$ is not independent, and is derived from standard-model constraints that use radiative corrections. To vary the $\sin\theta_W$ (M_W) parameter, the value of G_F is changed by a small amount prior to the calculation so that the derived M_W range is 80.0– $80.5~{\rm GeV}/c^2.^1$ The set of M_W values corresponds

to a family of physics models with standard-model like

faces. The calculation of form factors uses ZFITTER's interface to its $e\bar{e} \to Z \to f\bar{f}$ scattering-amplitude formalism (ROKANC). External QED and QCD radiation are turned off. The form factors include corrections from γ -Z mixing effects and from non-resonant γ and Z exchanges. The contributions from WW and ZZ box diagrams are included, but as they are not multiplicative form-factor corrections, these corrections are only approximate. The calculation is done in the massless-fermion approximation so the form factors only depend on the fermion weak isospin and charge. Consequently, the form factors are distinguished via three indices: e (electron type), u (upquark type), and d (down-quark type). The form factors are functions of the Mandelstam variable s, and with the inclusion of the box diagrams they also depend on $t = -\frac{1}{2}s(1-\cos\theta)$, where θ is the angle between the e and f. The ZFITTER scattering-amplitude ansatz is

$$A_{q} = \frac{i}{4} \frac{\sqrt{2}G_{F}M_{Z}^{2}}{s - (M_{Z}^{2} - i s\Gamma_{Z}/M_{Z})} 4T_{3}^{e}T_{3}^{q} \rho_{eq}$$

$$[\langle \bar{e}|\gamma^{\mu}(1+\gamma_{5})|e\rangle\langle \bar{q}|\gamma_{\mu}(1+\gamma_{5})|q\rangle +$$

$$-4|Q_{e}|\kappa_{e}\sin^{2}\theta_{W}\langle \bar{e}|\gamma^{\mu}|e\rangle\langle \bar{q}|\gamma_{\mu}(1+\gamma_{5})|q\rangle +$$

$$-4|Q_{q}|\kappa_{q}\sin^{2}\theta_{W}\langle \bar{e}|\gamma^{\mu}(1+\gamma_{5})|e\rangle\langle \bar{q}|\gamma_{\mu}|q\rangle +$$

$$16|Q_{e}Q_{q}|\kappa_{eq}\sin^{4}\theta_{W}\langle \bar{e}|\gamma^{\mu}|e\rangle\langle \bar{q}|\gamma_{\mu}|q\rangle], \quad (A1)$$

where q=u or d, the ρ_{eq} , κ_e , κ_q , and κ_{eq} are complex-valued form factors, the bilinear γ matrix terms covariantly are contracted, and $\frac{1}{2}(1+\gamma_5)$ is the left-handed helicity projector in the ZFITTER convention. The ρ_{eq} form factor is defined to be used with G_F . As their significant radiative corrections cancel to a large extent, they are combined to minimize the size of applied corrections. At $s=M_Z^2$, the κ_e form factors of the A_u and A_d amplitudes are numerically the same.

The amplitude A_q can be approximated with these Born-level g_V^f and g_A^f replacements,

$$g_V^f \to \sqrt{\rho_{eq}} (T_3^f - 2Q_f \kappa_f \sin^2 \theta_W)$$

 $g_A^f \to \sqrt{\rho_{eq}} T_3^f,$

where f = e or q. The Born electron-quark currentcurrent amplitude is nearly identical to A_q except that the last term contains $\kappa_e \kappa_q \sin^4 \theta_W$ rather than

couplings where $\sin^2\theta_W$ and the coupling (G_F) are defined by the M_W parameter. The Higgs-boson mass constraint $m_H=125~{\rm GeV}/c^2$ keeps the form factors within the vicinity of standard-model fit values from LEP-1 and SLD [5]. The primary purpose of ZFITTER is to provide tables of form factors for each model.

Access to ZFITTER calculations is through its *inter*-

¹ The ZFITTER electroweak radiative correction package (DIZET) is first used to iteratively estimate G_F from a target M_W input (IMOMS=3). Form factors are not calculated due to a partial

implementation. The code which calculates constants (CONST1) is modified to use this new G_F , then form factors are calculated using the default method (DIZET with IMOMS=1).

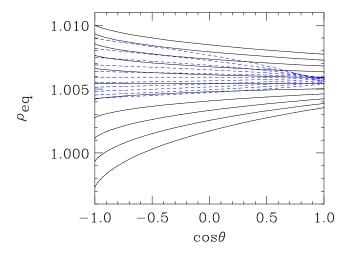


FIG. 14. Real part of ρ_{eq} as a function of $\cos\theta$ for $\sin^2\theta_W=0.2231$. Each curve corresponds to a different value of \sqrt{s} , varying from 66 to 116 GeV. The curves change monotonically with each step of s. The solid (black) curves are for u-type amplitudes, and the dashed (blue) curves are for d-type amplitudes. For the u-type amplitude, the highest mass corresponds to the lowermost curve at $\cos\theta=-1$, and for the d-type amplitude, the highest mass corresponds to the uppermost curve at $\cos\theta=-1$. The flat lines in the middle correspond to $\sqrt{s}=M_Z$.

 $\kappa_{eq} \sin^4 \theta_W$. The κ_{eq} form factor must be explicitly incorporated into the Born amplitude for a full implementation of the ZFITTER A_q amplitude; this is accomplished with the addition of an amplitude-correction term containing the $\kappa_{eq} - \kappa_e \kappa_q$ form factor. The space-time structure of the amplitude for the photon and the $\kappa_{eq} - \kappa_e \kappa_q$ correction is identical, and their amplitudes may be consolidated into a single term.

The s and t $(\cos\theta)$ dependencies of the form factors are illustrated for $\sin^2\theta_W=0.2231$ in distributions of the form factor as a function of $\cos\theta$, where curves of different s are superimposed on the same panel. The range of s is $66<\sqrt{s}<116$ GeV, and displayed in 5 GeV intervals. The real parts of the form factors ρ_{eq} , κ_e , κ_q , and κ_{eq} are shown in Figs. 14, 15, 16, and 17, respectively. The imaginary part of these form factors is on the order of ± 0.02 in value.

The t variation (from the box diagrams) for each s is averaged out, and this average is a cross-section (Born $d\sigma/d\cos\theta$) weighted average. The form factors used in QCD calculations are implemented as complex-valued look-up tables in ($\sin^2\theta_W$, s).

Only the photon self-energy correction from fermion loops is used with the ZFITTER Z-amplitude form factors. The correction is applied as a form factor to the photon propagator

$$\frac{i\,e^2Q_eQ_q}{s} \to \frac{i\,e^2Q_eQ_q}{s} \frac{1}{1-\Delta\alpha_{em}(s)}\;,$$

where $1 - \Delta \alpha_{em}(s)$ is the complex-valued form factor, which equals 1 when s = 0. The fermion-loop integrals

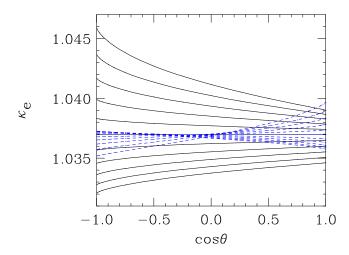


FIG. 15. Real part of κ_e as a function of $\cos\theta$ for $\sin^2\theta_W = 0.2231$. Each curve corresponds to a different value of \sqrt{s} , varying from 66 to 116 GeV. The curves change monotonically with each step of s. The solid (black) curves are for u-type amplitudes, and the dashed (blue) curves are for d-type amplitudes. For the u-type amplitude, the highest mass corresponds to the uppermost curve at $\cos\theta = -1$, and for the d-type amplitude, the highest mass corresponds to the lowermost curve at $\cos\theta = -1$. The flat lines in the middle corresponds to $\sqrt{s} = M_Z$.

of the form factor are complex-valued functions of s and the fermion mass, m_f . All fermion pairs above production thresholds, i.e., $4m_f^2 < s$ contribute to the imaginary part of the form factor. The leptonic-loop contributions and the imaginary part of quark loops are calculated. The contribution of the light quarks to the real part of the form factor is derived from measurements of $e^+e^- \to {\rm hadrons}$ and is a function of s. At the Z pole, the sum of contributions from the u, c, d, s, and b quarks is $\Delta\alpha_{em}^{(5)}(M_Z^2) = 0.0275 \pm 0.0001$ [36]. Figure 18 illustrates $\Delta\alpha_{em}(s)$.

Appendix B: EBA Operational Tests

The ZGRAD2 calculation [23] is a LO QCD calculation with $\mathcal{O}(\alpha)$ standard-model corrections to the Drell-Yan $p\bar{p}\to e^+e^-$ process. As the calculation of EWK corrections differs from that of ZFITTER, it provides a test of the implementation of the ZFITTER form-factor input to the EBA calculations. A full test is not possible because a few parts of the ZFITTER EBA implementation differ from ZGRAD2. Form-factor corrections are calculated by ZGRAD2 for the g_A^f and g_V^f couplings of both the γ and Z bosons, i.e., $g_{A,V}^f\to F_{A,V}^f$ $g_{A,V}^f$, where $F_{A,V}^f$ is the form factor. Bosonic self-energy corrections are included. In the cross-section amplitude, the corrected g_A^f and g_V^f are complex-valued couplings. The WW and ZZ box diagram cross-sections are separately calculated, and added to the total cross section. For the following test, both

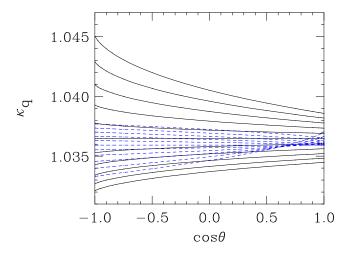


FIG. 16. Real part of κ_q as a function of $\cos\theta$ for $\sin^2\theta_W = 0.2231$. Each curve corresponds to a different value of \sqrt{s} , varying from 66 to 116 GeV. The curves change monotonically with each step of s. The solid (black) curves are for u-type amplitudes, and the dashed (blue) curves are for d-type amplitudes. For the u-type amplitude, the highest mass corresponds to the uppermost curve at $\cos\theta = -1$, and for the d-type amplitude, the highest mass corresponds to the lowermost curve at $\cos\theta = -1$. The flat lines in the middle corresponds to $\sqrt{s} = M_Z$.

box-diagram and initial- and final-state QED radiation contributions are disabled. The couplings from ZGRAD2 are converted into ZFITTER (ρ and κ) form factors, and the ratio of the ZGRAD2-to-ZFITTER form factors (which are complex valued) are evaluated for comparisons. The κ form factors are very similar for $\sin^2\theta_W=0.2230$: The fractional differences of both the real and imaginary parts of the ratio range from -0.1% to 0.2% over $66 < \sqrt{s} < 116$ GeV. The ρ form factors have offsets over the range of \sqrt{s} . The real part decreases from -0.5% to -0.7%, and the imaginary part increases from 0.2% to 0.5%. The Z-boson coupling schemes of ZGRAD2 and ZFITTER differ, and can affect ρ .

Next, the effect of WW and ZZ box diagrams on the value of the \bar{A}_4 coefficient is calculated with both the ZGRAD2 and the ZFITTER EBA-based tree calculation. For both, the effect is small and essentially the same: The value of the coefficient with box-diagram contributions is 0.0001 smaller in difference than without box-diagram contributions. This confirms that the averaging of the t dependence of the ZFITTER form factors from the box diagrams used in the EBA form-factor tables does not impact the EBA-based calculations.

In standard-model tests of the process $e^+e^- \to f\bar{f}$, ZFITTER calculates cross sections and final-state fermion asymmetries using all form factors in their complex-valued form: the vertex form factors ρ_{eq} , κ_e , κ_q , and κ_{eq} , and the photon self-energy correction form factor. The ZGRAD2 calculations do not have the κ_{eq} form factor or the imaginary part of the photon self-energy correction

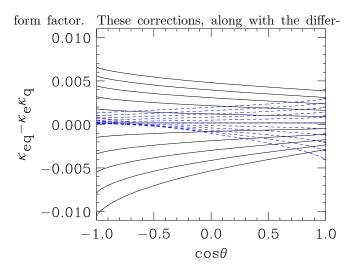


FIG. 17. Real part of $\kappa_{eq} - \kappa_e \kappa_q$ as a function of $\cos \theta$ for $\sin^2 \theta_W = 0.2231$. Each curve corresponds to a different value of \sqrt{s} , varying from 66 to 116 GeV. The curves change monotonically with each step of s. The solid (black) curves are for u-type amplitudes, and the dashed (blue) curves are for d-type amplitudes. For the u-type amplitude, the highest mass corresponds to the lowermost curve at $\cos \theta = -1$, and for the d-type amplitude, the highest mass corresponds to the uppermost curve at $\cos \theta = -1$. The flat lines in the middle correspond to $\sqrt{s} = M_Z$.

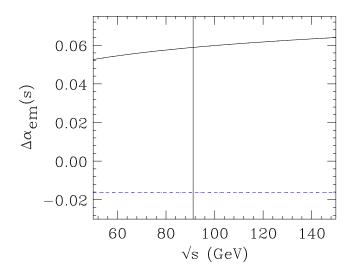


FIG. 18. The $\Delta\alpha_{em}(s)$ form factor for $50 < \sqrt{s} < 150$ GeV. The upper solid curve corresponds to the real part and the lower dashed curve corresponds the imaginary part. The vertical line is $\sqrt{s} = M_Z$.

ence in the ρ form factor, induce a shift of -0.0025 in the value of \bar{A}_4 from the default EBA-based tree calculation, with 75% due to the imaginary part of the photon self-energy correction. The calculation of \bar{A}_4 by ZGRAD2 yields a value 0.0036 ± 0.0006 smaller than the ZFITTER EBA-based tree calculation, but is consistent with the expected difference.

- S. D. Drell and T.-M. Yan, Phys. Rev. Lett. 25, 316 (1970).
- [2] J. Beringer et al. (Particle Data Group), Phys. Rev. D 86, 010001 (2012).
- [3] D. Acosta et al. (CDF Collaboration), Phys. Rev. D 71, 052002 (2005).
- [4] V. M. Abazov et al. (D0 Collaboration), Phys. Rev. D 84, 012007 (2011).
- [5] S. Schael et al. (ALEPH, DELPHI, L3, OPAL, and SLD Collaborations, LEP Electroweak Working Group, and SLD Electroweak and Heavy Flavour Groups), Phys. Rept. 427, 257 (2006).
- [6] T. Aaltonen et al. (CDF Collaboration), Phys. Rev. Lett. 106, 241801 (2011).
- [7] J. C. Collins and D. E. Soper, Phys. Rev. D 16, 2219 (1977).
- [8] E. Mirkes, Nucl. Phys. **B387**, 3 (1992); E. Mirkes and J. Ohnemus, Phys. Rev. D **50**, 5692 (1994).
- D. Bardin, M. Bilenky, T. Riemann, M. Sachwitz, and H. Vogt, Comput. Phys. Commun. 59, 303 (1990);
 D. Bardin, P. Christova, M. Jack, L. Kalinovskaya, A. Olchevski, S. Riemann, and T. Riemann, *ibid.* 133, 229 (2001); A. Arbuzov, M. Awramik, M. Czakon, A. Freitas, M. Grünewald, K. Monig, S. Riemann, and T. Riemann, *ibid.* 174, 728 (2006).
- [10] A. Sirlin, Phys. Rev. D 22, 971 (1980).
- [11] H.-L. Lai, M. Guzzi, J. Huston, Z. Li, P. Nadolsky, J. Pumplin, and C.-P. Yuan, Phys. Rev. D 82, 074024 (2010).
- [12] G. A. Ladinsky and C.-P. Yuan, Phys. Rev. D 50, 4239 (1994); C. Balàzs and C.-P. Yuan, *ibid.* 56, 5558 (1997);
 F. Landry, R. Brock, P. M. Nadolsky, and C.-P. Yuan, *ibid.* 67, 073016 (2003); A. Konychev and P. Nadolsky, Phys. Lett. B 633, 710 (2006).
- [13] S. Alioli, P. Nason, C. Oleari, and E. Re, J. High Energy Phys. 07, 060 (2008).
- [14] J. C. Collins, D. E. Soper, and G. Sterman, Nucl. Phys. B250, 199 (1985); J. C. Collins and D. E. Soper, *ibid.* B193, 381 (1981); B213, 545(E) (1983); B197, 446(E) (1982).
- [15] P. M. Nadolsky *et al.* (CTEQ Collaboration), Phys. Rev. D 78, 103004 (2008).
- [16] T. Sjöstrand, S. Mrenna, and P. Z. Skands, J. High Energy Phys. 05 (2006).

- [17] T. Sjöstrand, P. Edén, L. Lönnblad, G. Miu, S. Mrenna, and E. Norrbin, Comput. Phys. Commun. 135, 238 (2001).
- [18] H. L. Lai et al. (CTEQ Collaboration), Eur. Phys. J. C 12, 375 (2000).
- [19] T. Affolder *et al.* (CDF Collaboration), Phys. Rev. Lett. 84, 845 (2000).
- [20] M. Albrow et al. (Tev4LHC QCD Working Group), arXiv:0610012v1 [hep-ph].
- [21] E. Barberio and Z. Was, Computer Phys. Comm. 79, 291 (1994); E. Barberio, B. van Eijk, and Z. Was, 66, 115 (1991).
- [22] P. Golonka and Z. Was, Eur. Phys. J. C 45, 97 (2006).
- [23] U. Baur, O. Brein, W. Hollik, C. Schappacher, and D. Wackeroth, Phys. Rev. D 65, 033007 (2002).
- [24] A. Abulencia et al. (CDF Collaboration), J. Phys. G: Nucl. Part. Phys. 34, 2457 (2007).
- [25] T. Affolder et al., Nucl. Instrum. and Methods A 526, 249 (2004).
- [26] A. Sill et al., Nucl. Instrum. and Methods A 447, 1 (2000).
- [27] A. Affolder *et al.*, Nucl. Instrum. and Methods A **453**, 84 (2000).
- [28] Christopher S. Hill, Nucl. Instrum. and Methods A 511, 118 (2004).
- [29] L. Balka et al., Nucl. Instrum. and Methods A 267, 272 (1988).
- [30] S. Bertolucci et al., Nucl. Instrum. and Methods A 267, 301 (1988).
- [31] M. Albrow et al., Nucl. Instrum. and Methods A 480, 524 (2002).
- [32] G. Apollinari et al., Nucl. Instrum. and Methods A 412, 515 (1998).
- [33] P. de Barbaro, IEEE Trans. Nucl. Sci. 42, 510 (1995).
- [34] T. Aaltonen et al. (CDF Collaboration), Phys. Rev. D 86, 052010 (2012).
- [35] J. Beringer et al. (Particle Data Group), Phys. Rev. D 86, 010001 (2012).
- [36] F. Jegerlehner, Nuovo Cim. C 034S1, 31 (2011), arXiv:1107.4683 [hep-ph].
- [37] T. Aaltonen *et al.* (CDF and D0 Collaborations), Phys. Rev. D 86, 092003 (2012).