

The QCD phase diagram at high densities

An experimental overview (2)

63. Cracow School of Theoretical Physics 2023
Nuclear Matter at Extreme Densities and High Temperatures
Zakopane, Tatra Mountains, Poland

17. — 23. Sep. 2023

Christoph Blume, University of Frankfurt



Observables

Observables

Collectivity + Vorticity

Radial, directed and elliptic flow (+ higher orders)
Global polarization

Criticality ($\Rightarrow$ Anar's lecture)

Strangeness in Matter

Maximum in relative strangeness production
Hypernuclei: hyperon interaction $\rightarrow$ neutron star EOS

Emissivity

Thermal radiation

Collectivity

Evolution of a Heavy-Ion Collision

Kinetic freeze-out at T_{fo} :

Elastic collisions cease

Momentum spectra frozen

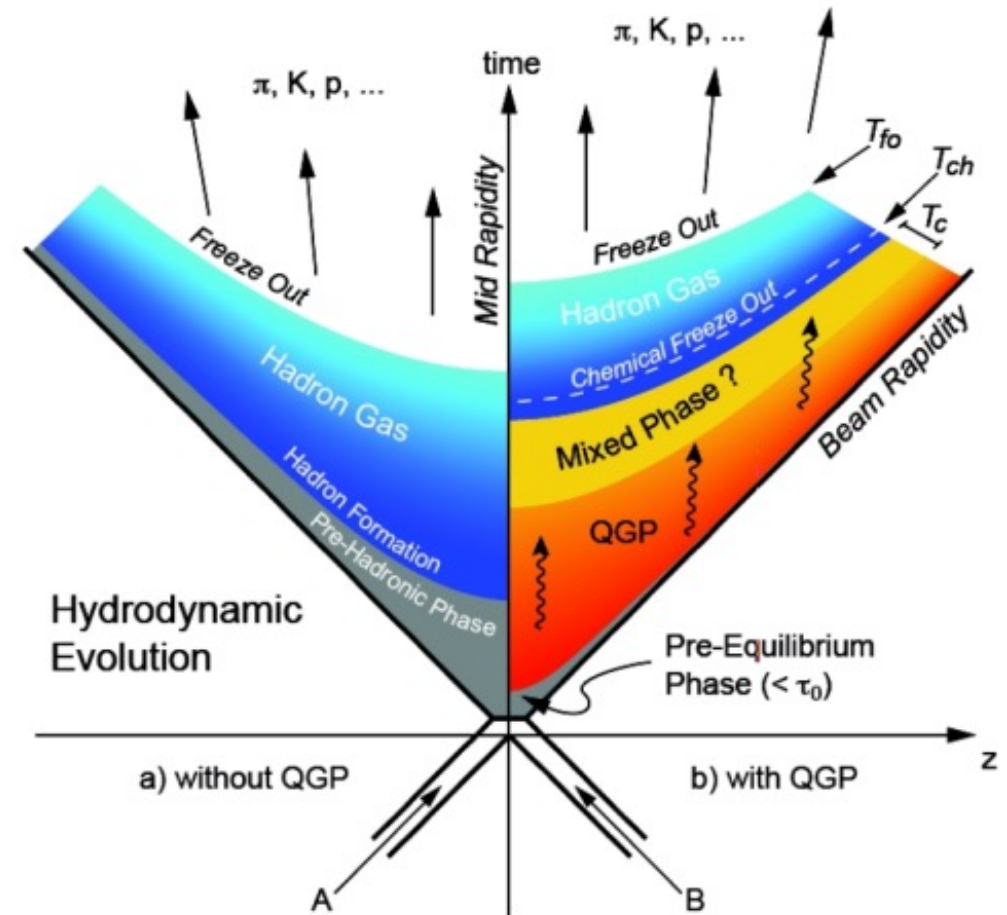
Chemical freeze-out at T_{ch} :

Inelastic collisions cease

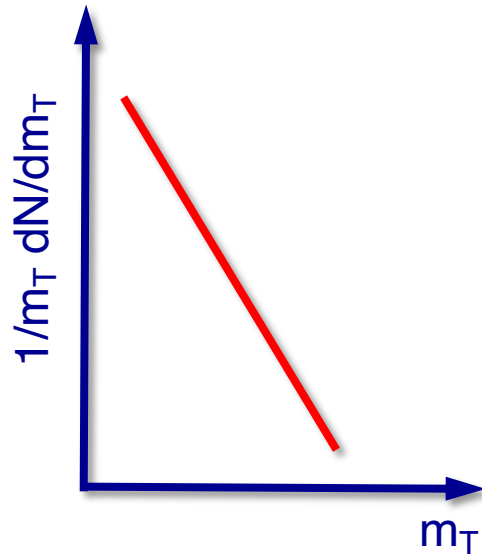
Particle yields frozen ($\rightarrow$ statistical models)

Pressure generated throughout system evolution
(hadronic and partonic phase)

$\rightarrow$ Modifies particle spectra

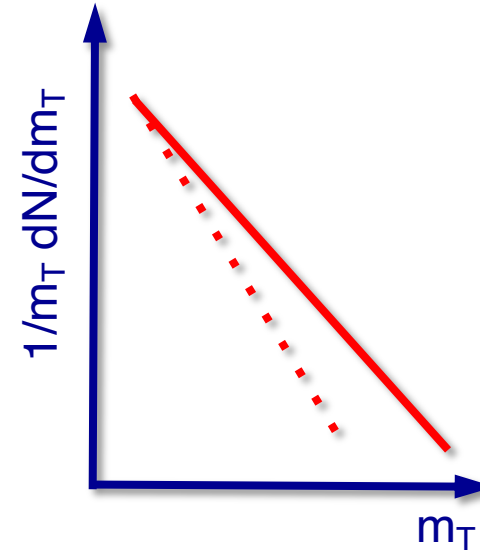


Radial Flow: Transverse Spectra



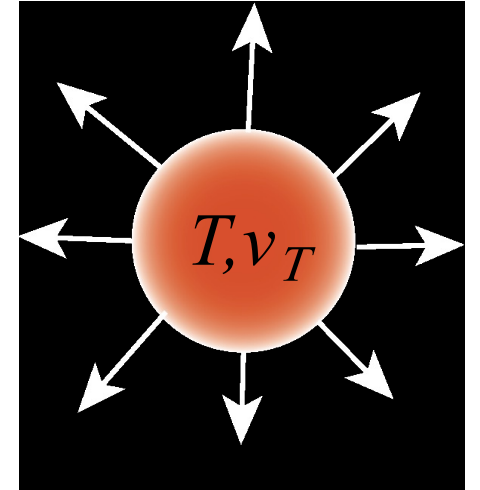
No radial flow:
exponential spectrum
(e.g.: p+p collisions)

$$\frac{1}{m_T} \frac{dN}{dm_T} \propto \exp\left(-\frac{m_T}{T_f}\right)$$

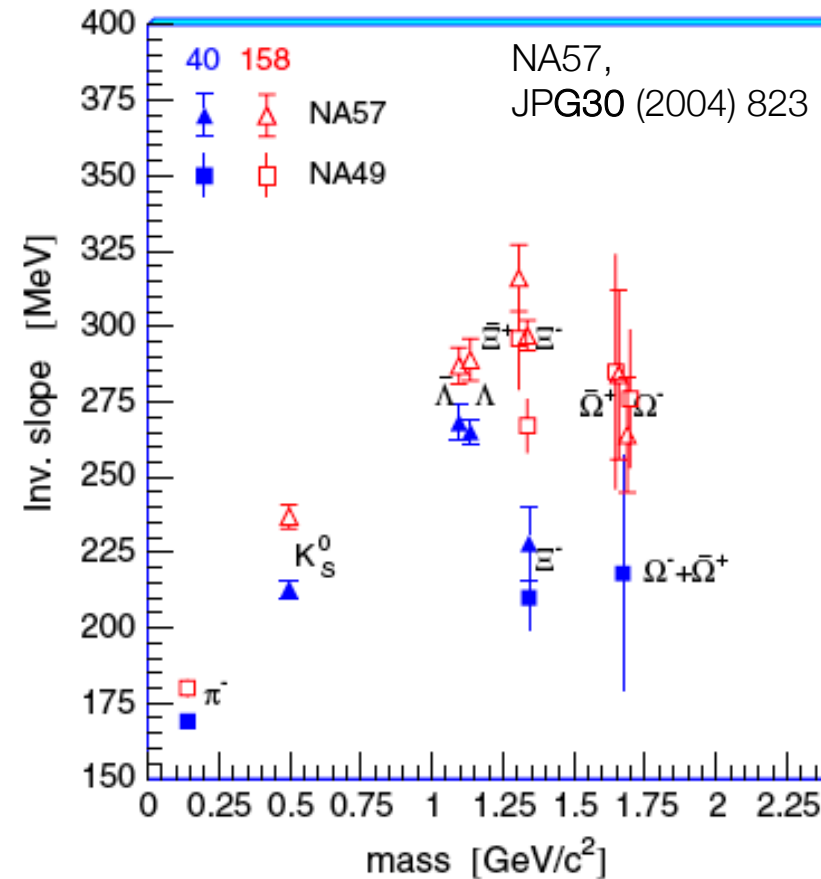
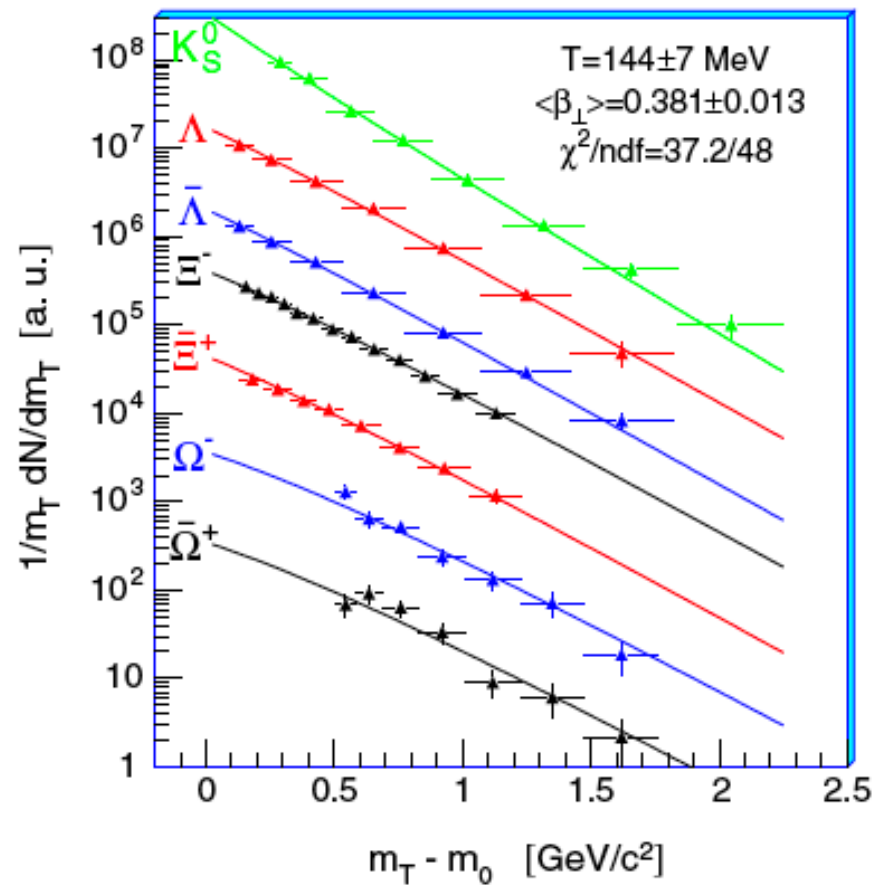


With radial flow:
additional boost by expansion (v_T)
 $\Rightarrow$ blue shifted spectrum

$$T_{eff} \approx T_f + \frac{1}{2} m v_T^2$$



Radial Flow: Transverse Spectra

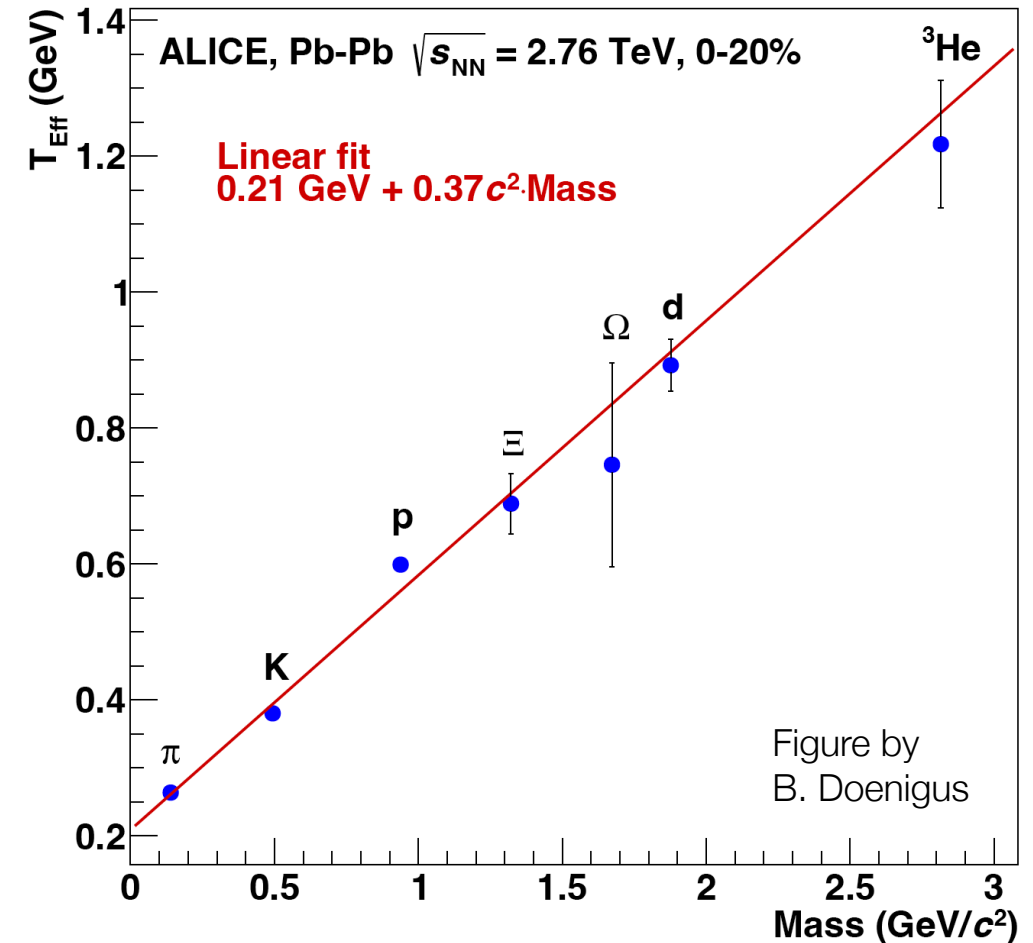


Radial Flow: Transverse Spectra

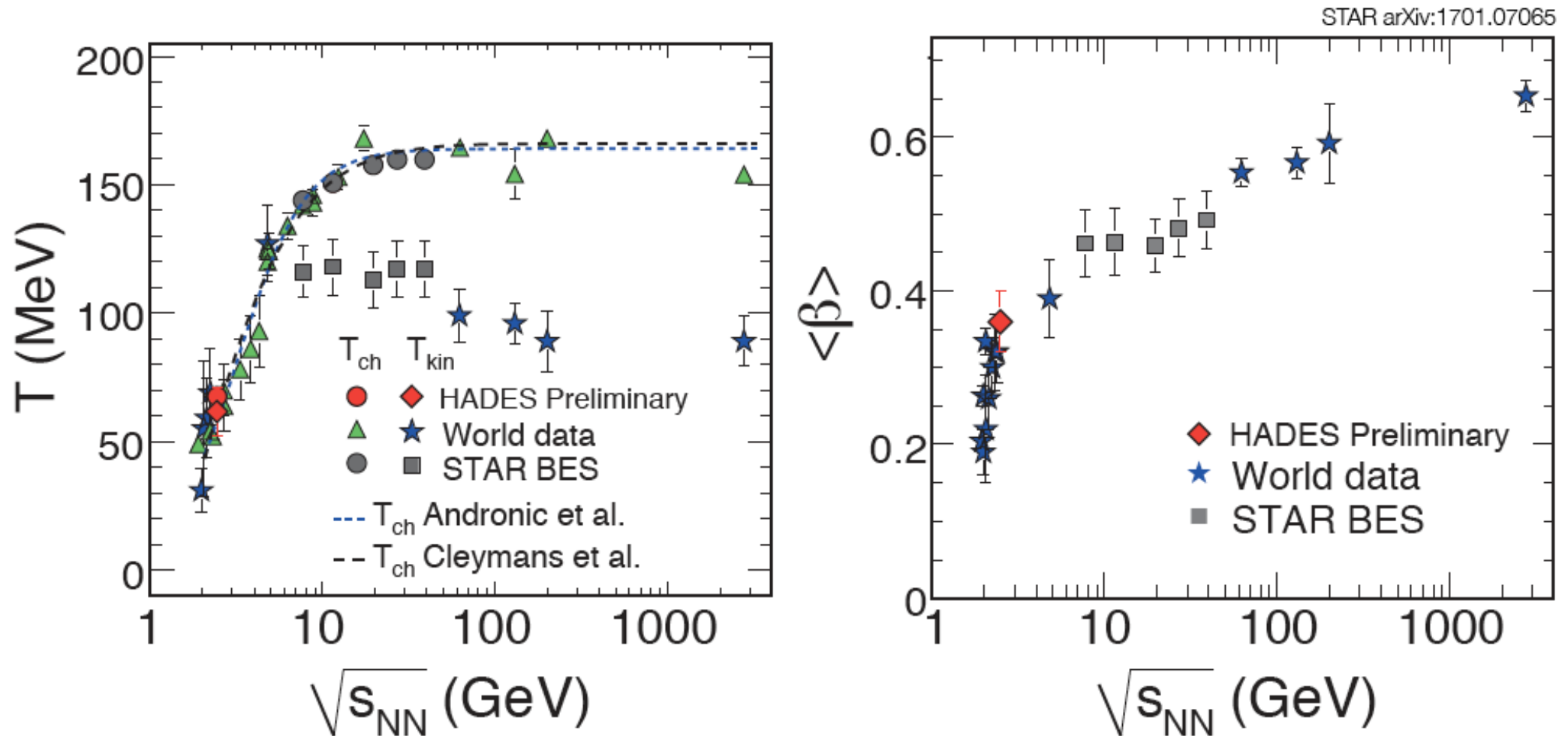
Low hadronic cross section
of rare particles (Ξ , Ω , J/ψ)

Radial flow dominated by partonic
contribution at very high energies

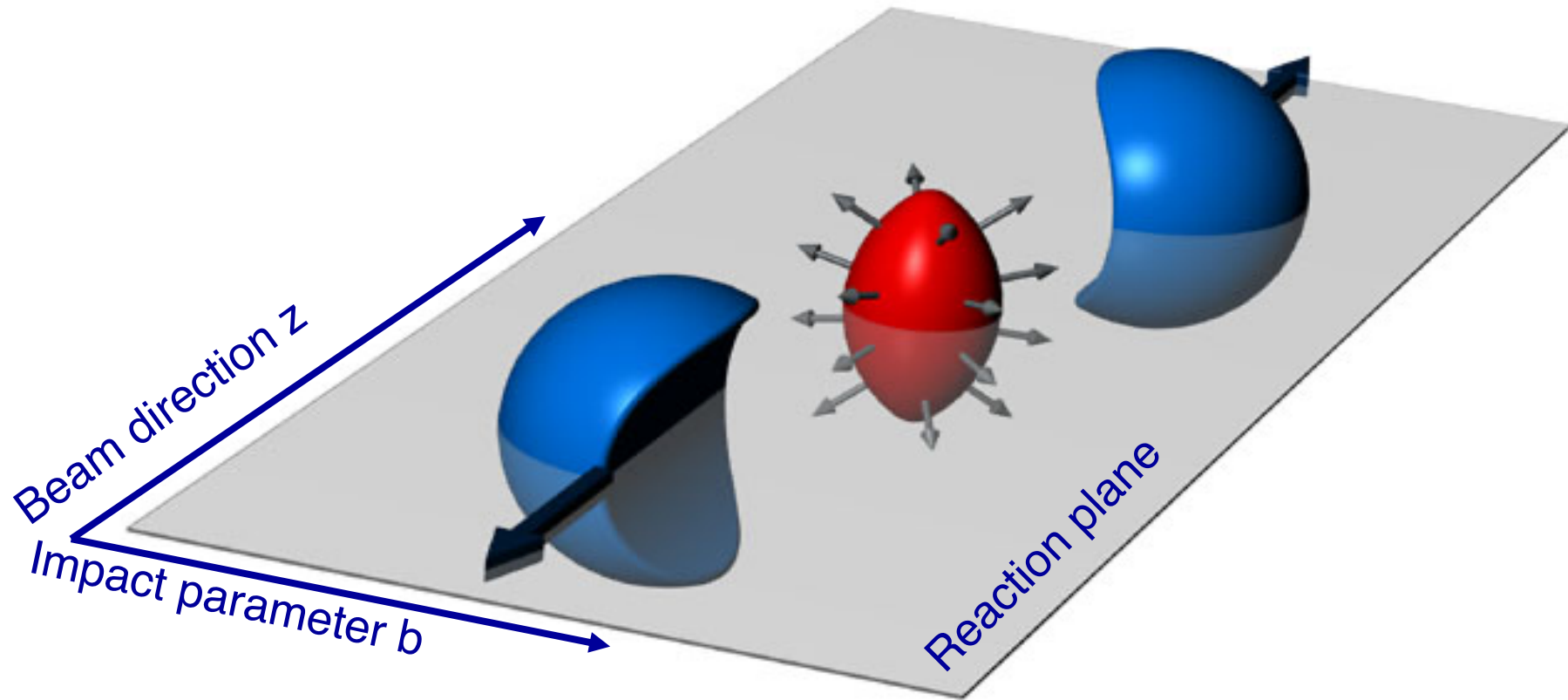
Different to lower energies



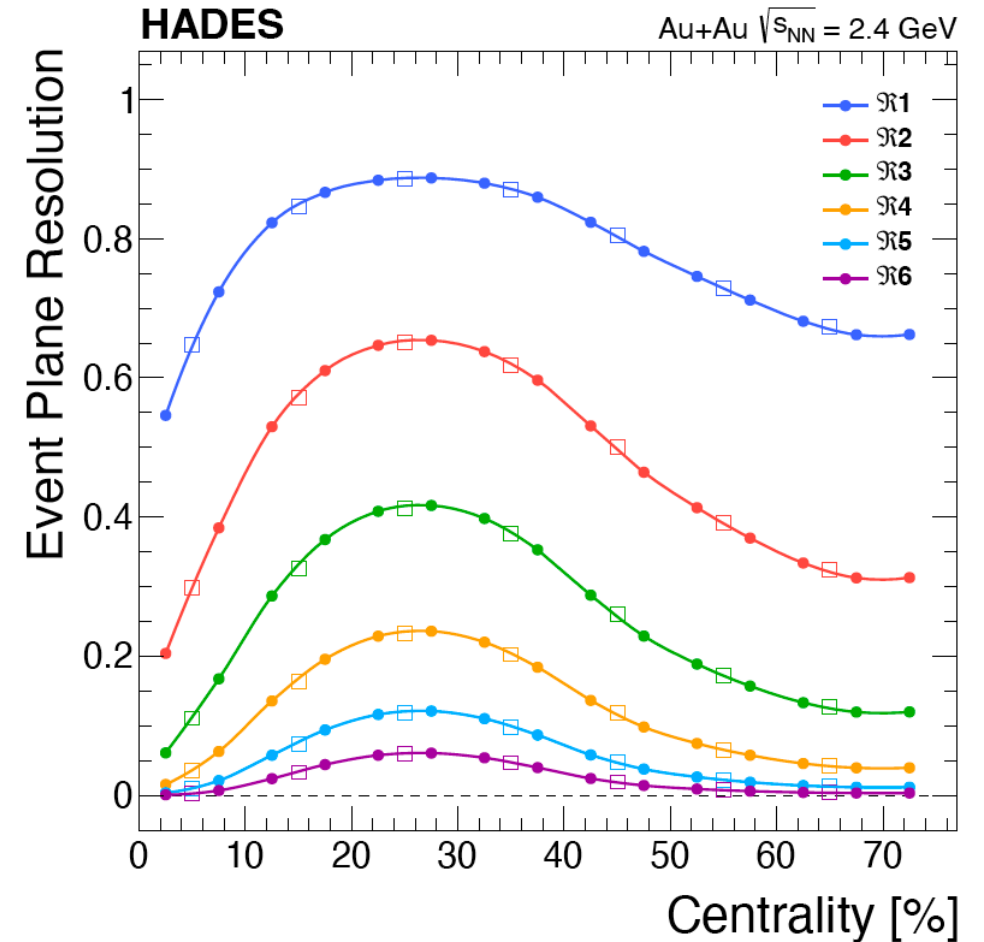
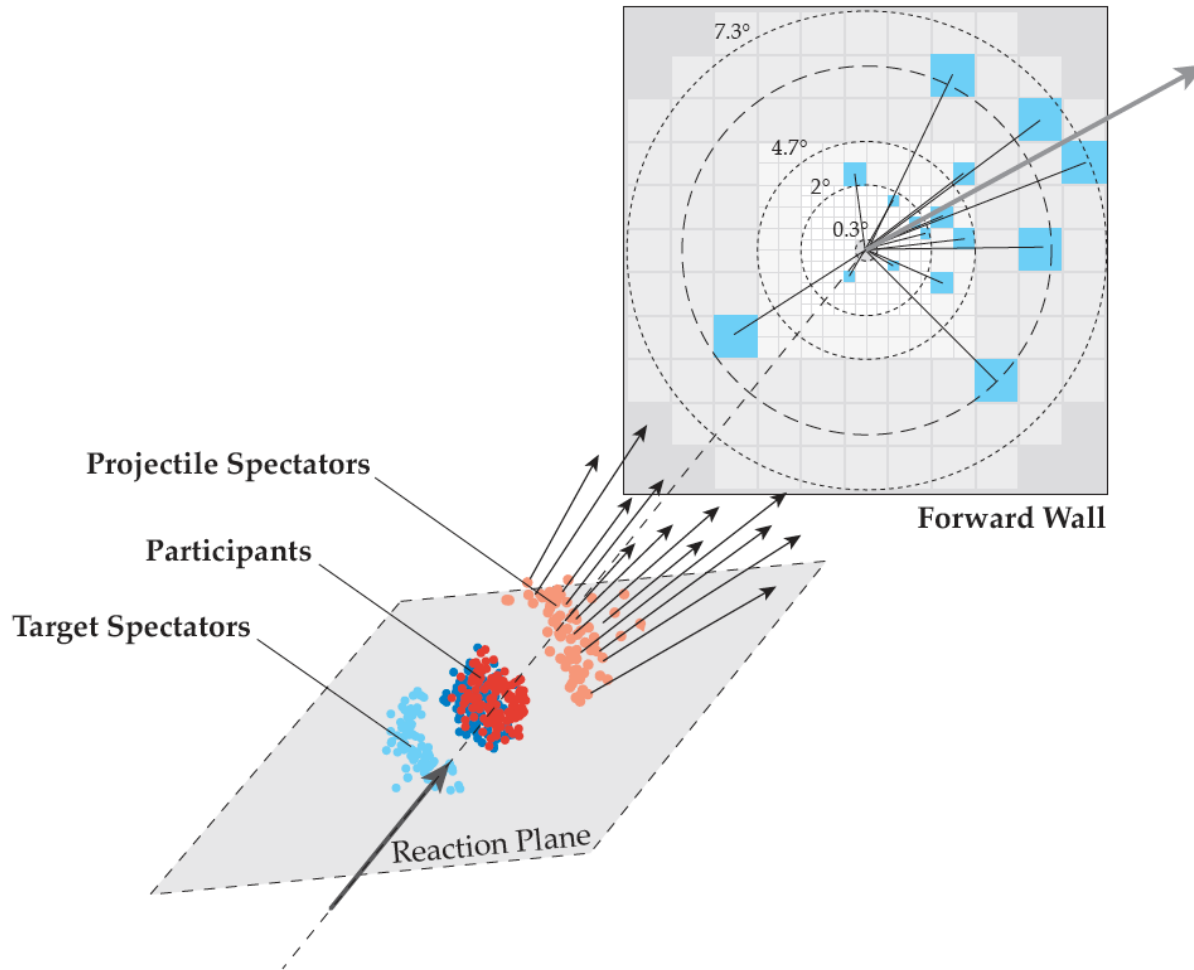
Radial Flow: Transverse Spectra



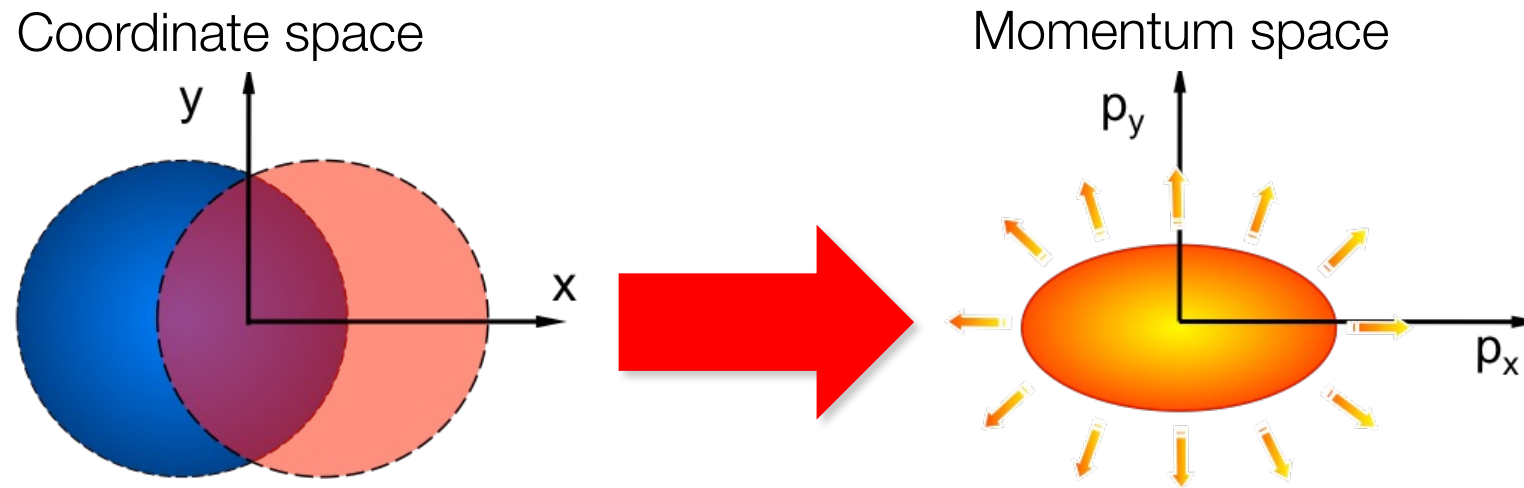
Reaction plane



Reaction plane: Measurement



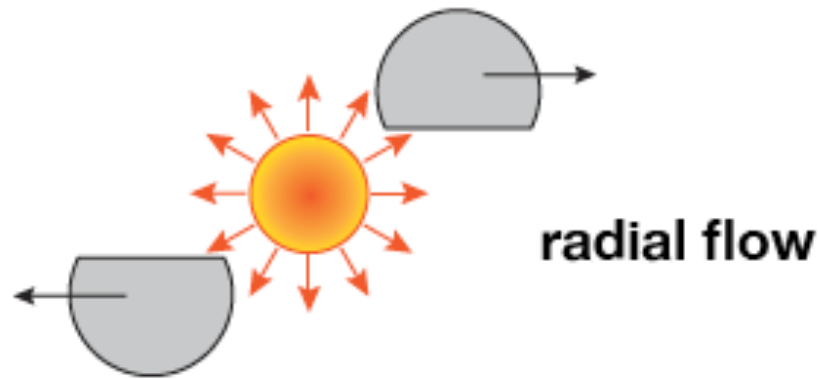
Flow: Fourier Decomposition



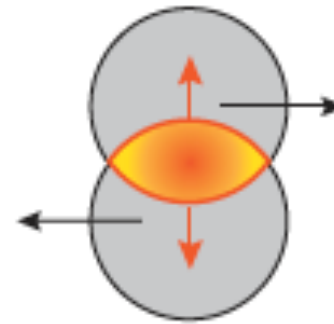
$$E \frac{d^3 N}{d^3 \mathbf{p}} = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\varphi - \Psi_{RP})] \right)$$

$$v_n(p_t, y) = \langle \cos[n(\varphi - \Psi_{RP})] \rangle$$

Flow Coefficients



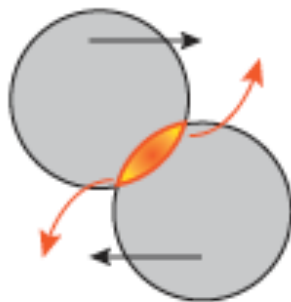
$$\phi = (\varphi - \Psi_{RP})$$



elliptic flow

$$v_2 = \langle \cos(2\phi) \rangle$$

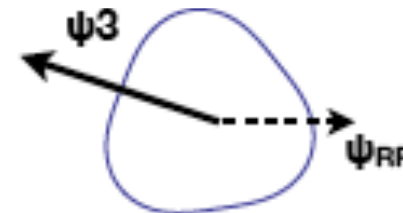
$$= \left\langle \frac{p_x^2 - p_y^2}{p_t^2} \right\rangle$$



directed flow

$$v_1 = \langle \cos(\phi) \rangle$$

$$= \left\langle \frac{p_x}{p_t} \right\rangle$$

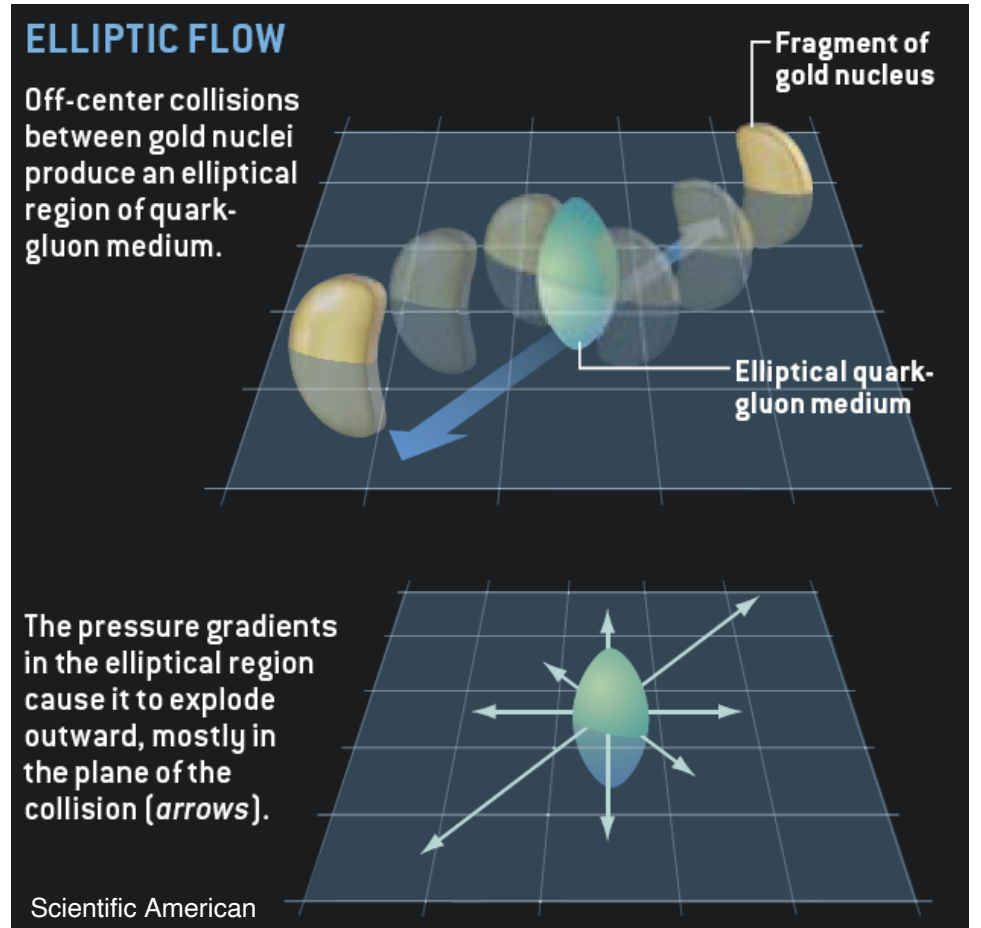
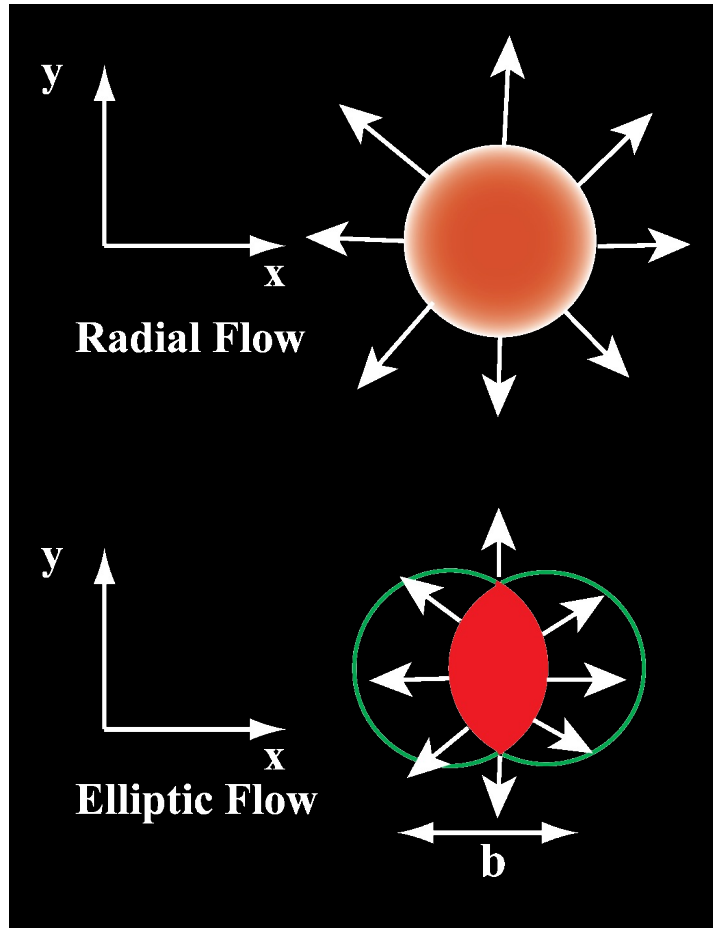


triangular flow

$$v_3 = \langle \cos(3\phi) \rangle$$

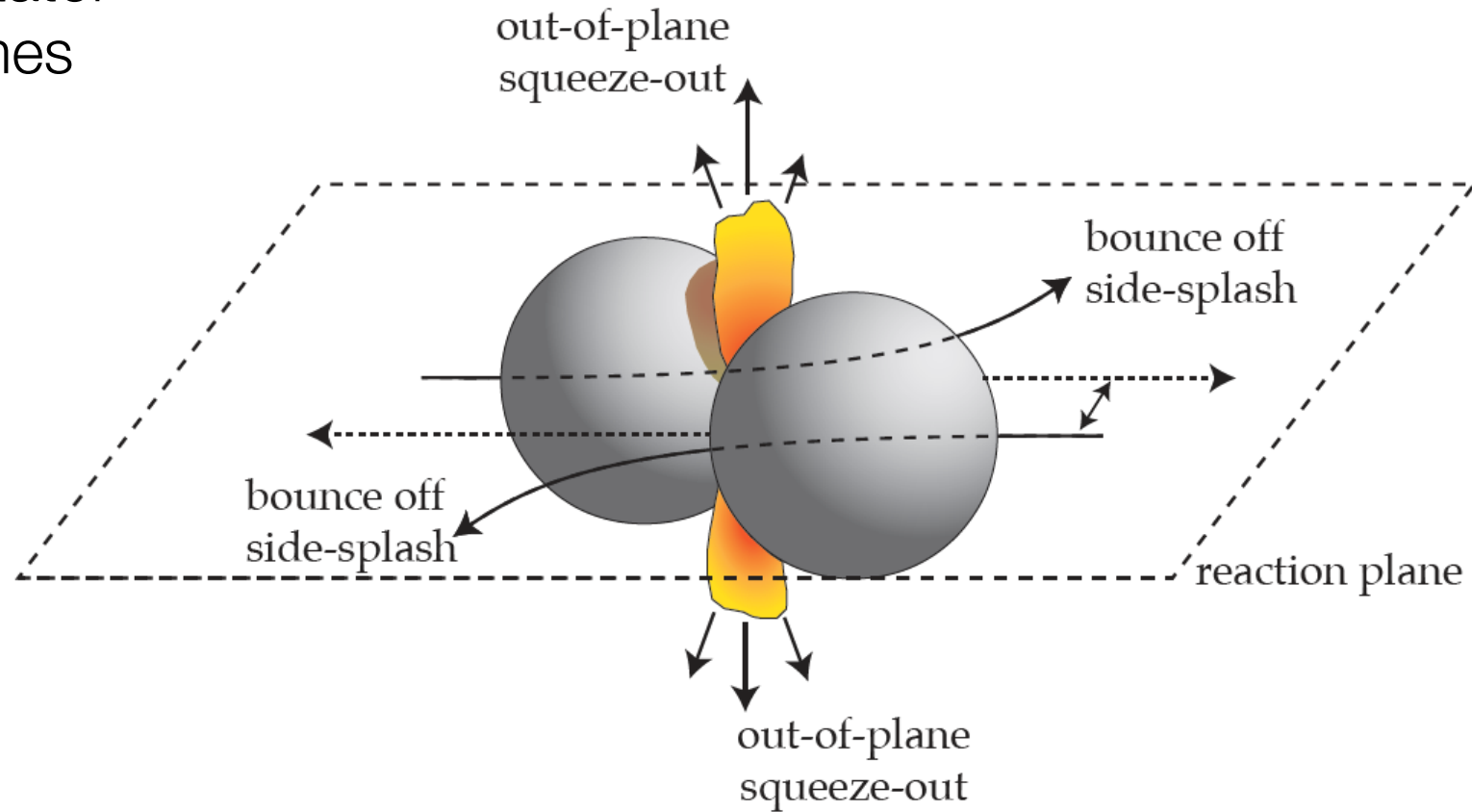
$$= \left\langle \frac{p_x^3 - 3p_x p_y^2}{p_t^3} \right\rangle$$

Elliptic Flow



Configuration at Lower Energies

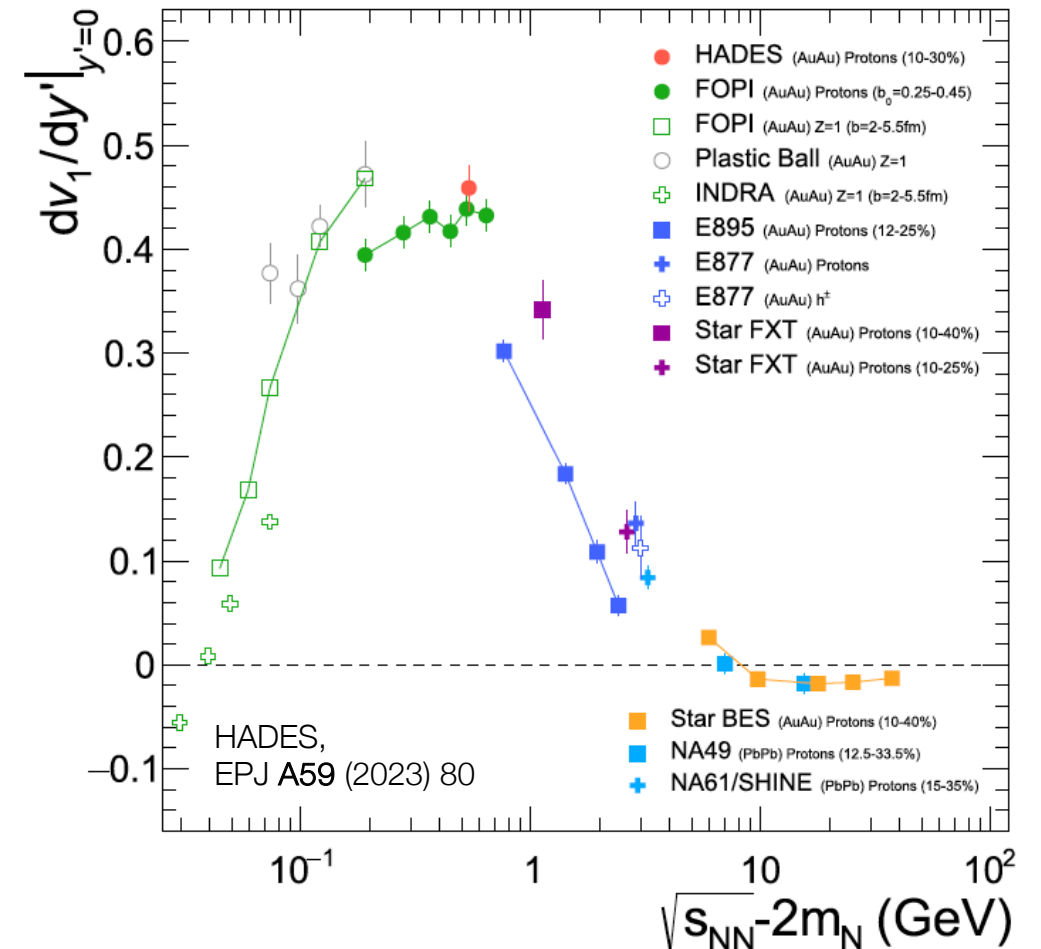
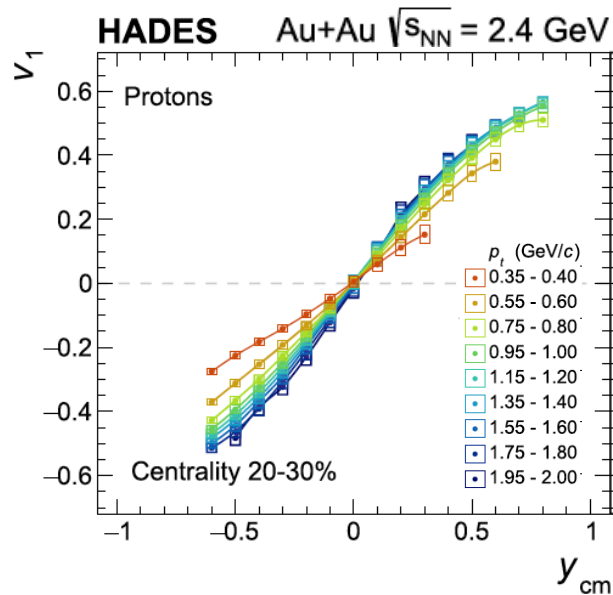
Long spectator
passing times



Energy Dependence of v_1

Slope of directed flow (v_1) at mid-rapidity:

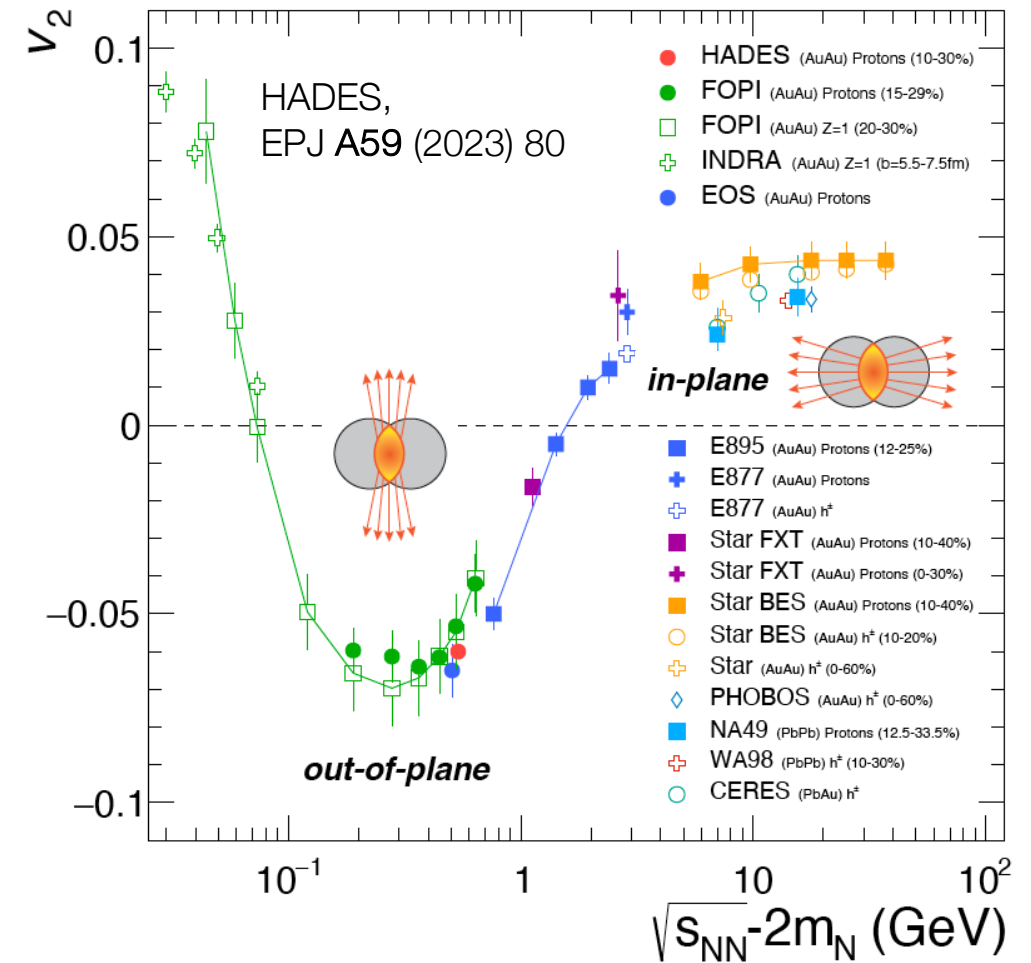
$$dv_1/dy'|_{y'=0} \text{ with } y' = y_{\text{cm}}/y_{\text{mid}}$$



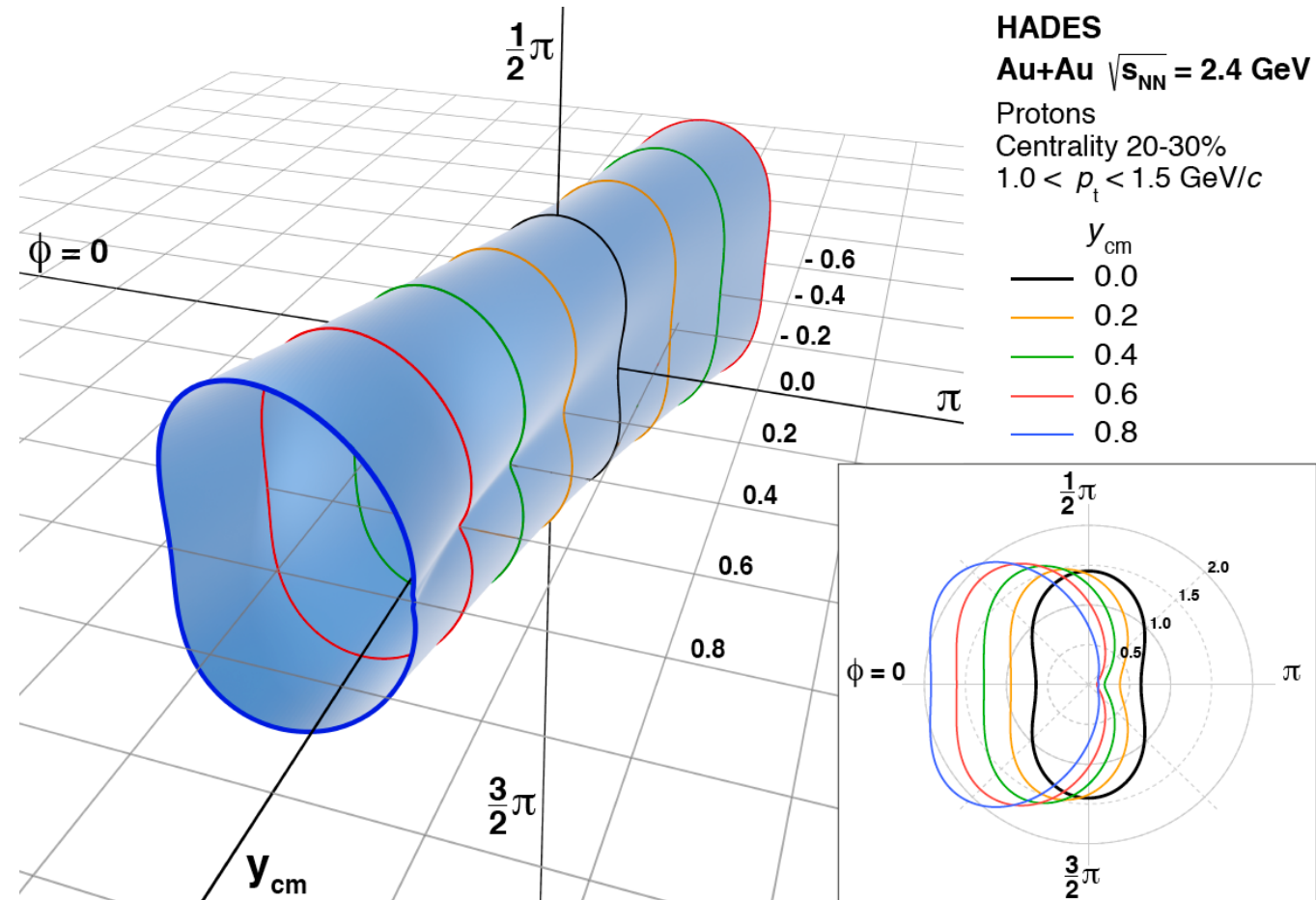
Energy Dependence of v_2

Elliptic flow (v_2) at mid-rapidity:

Evolution from
out-of-plane to in-plane flow

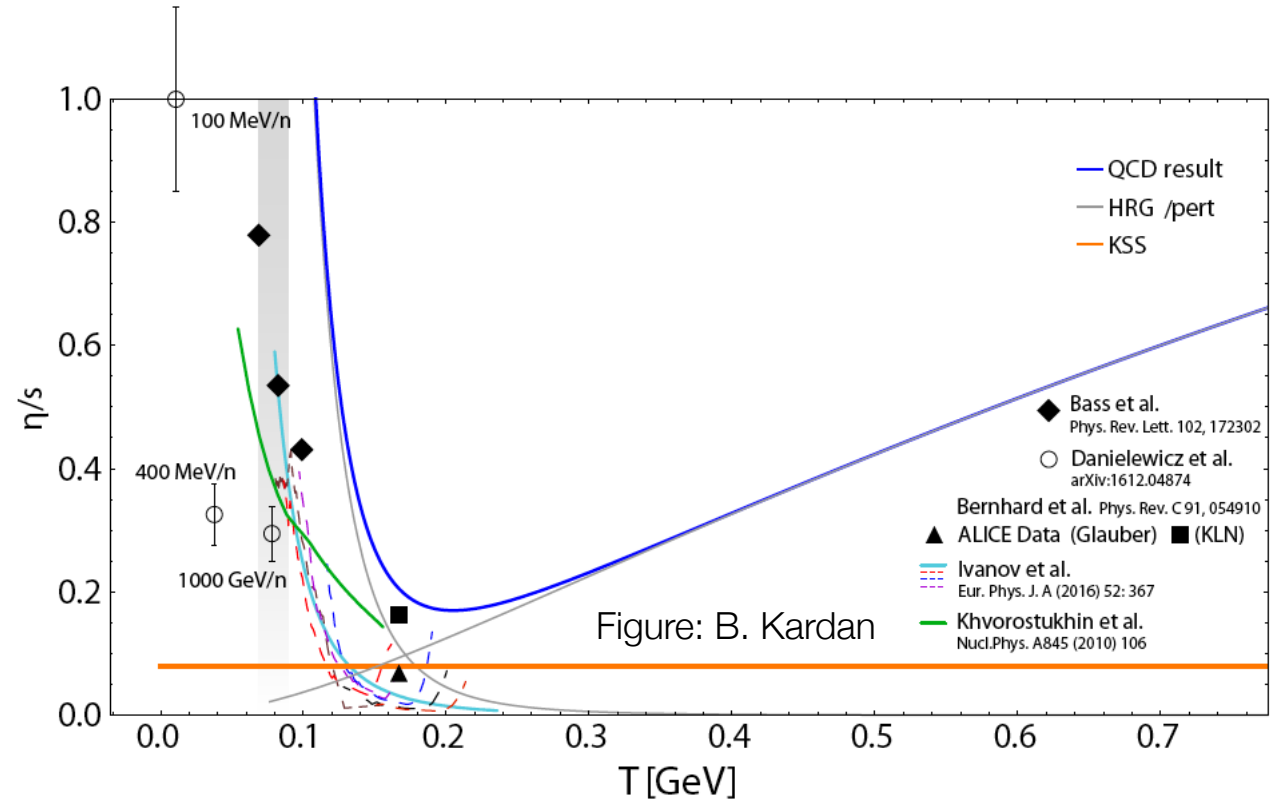
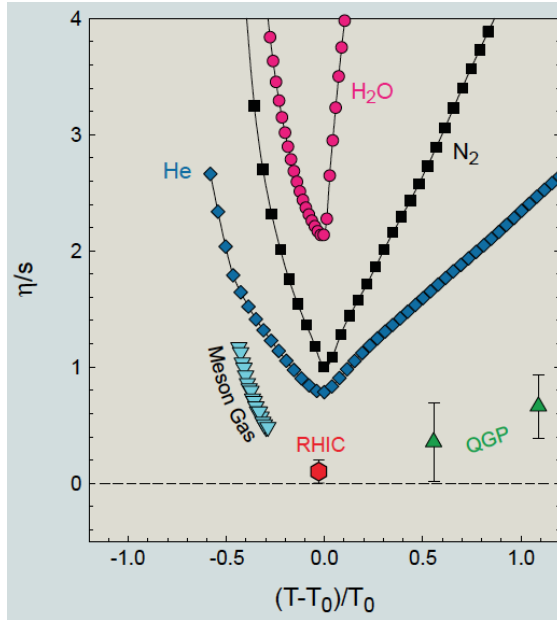


Higher Order Flow Components



HADES,
 Phys. Rev. Lett.
 125 (2020) 262301

Shear Viscosity over Entropy Ratio



Strongly coupled QGP at high energies (“perfect liquid”)

Baryonic medium at lower energies more difficult to characterize

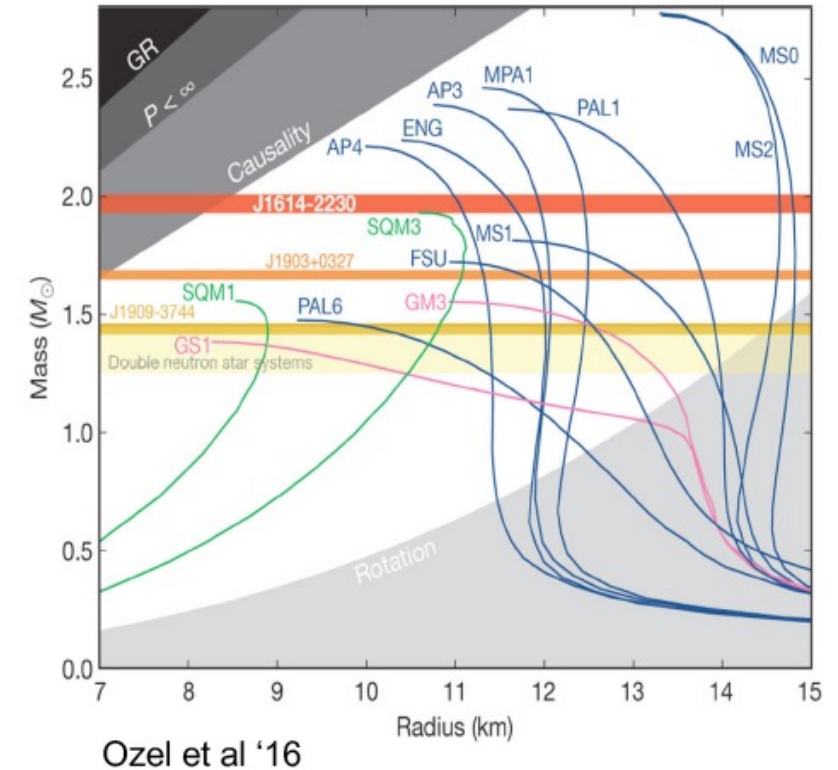
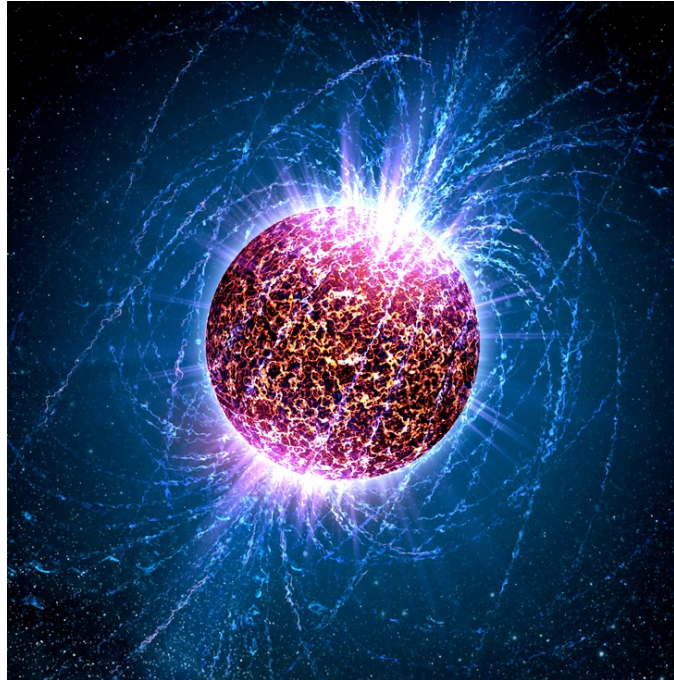
Neutron Stars: Equation-of-State

Mass-radius relation

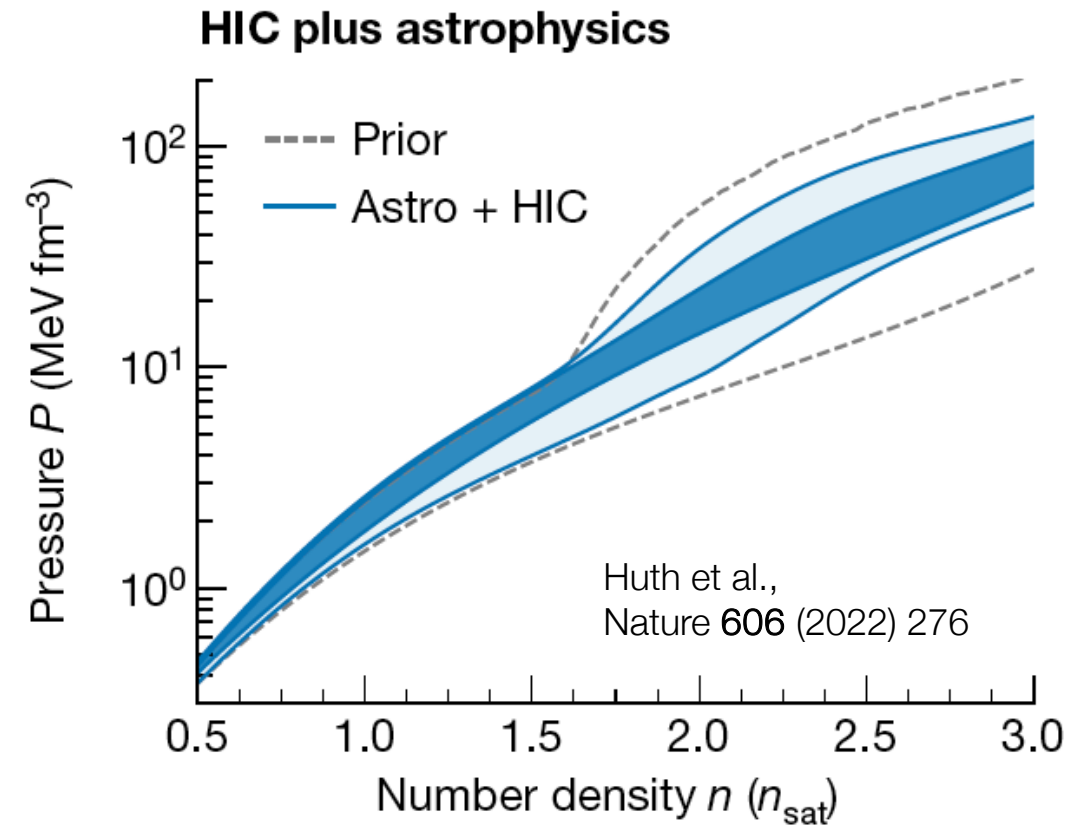
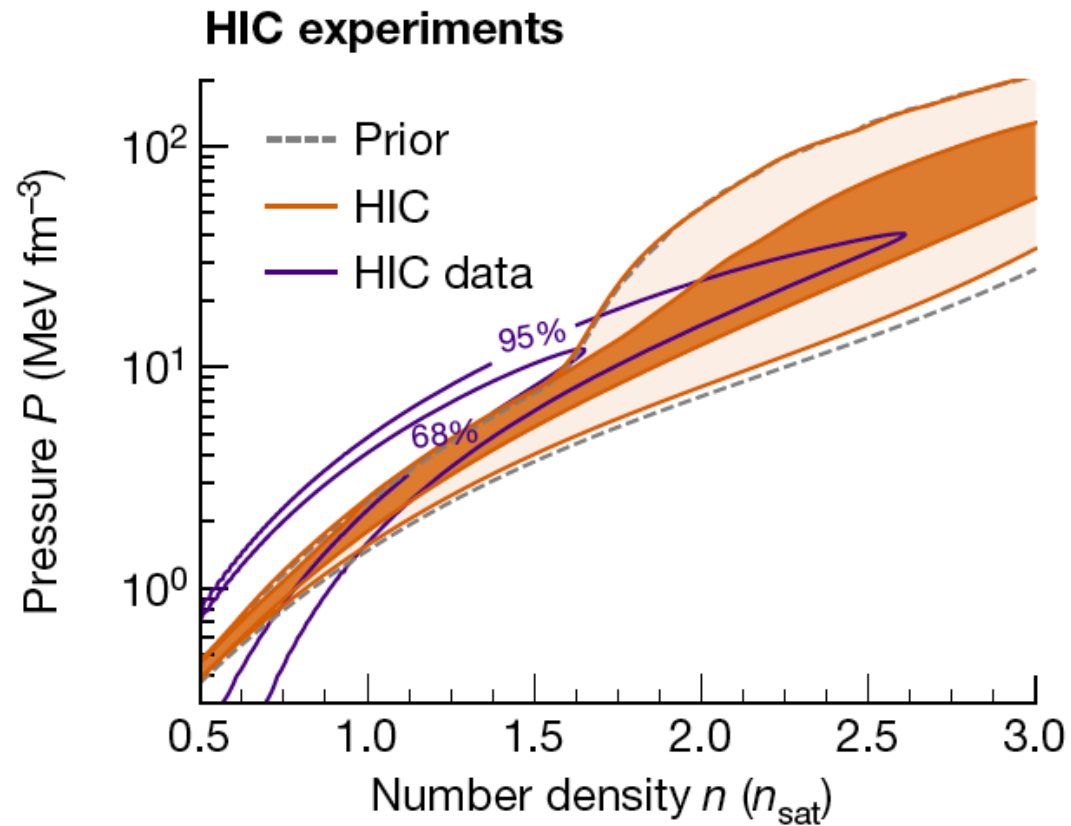
Depends on EOS of dense nuclear matter

Constraint from astrophysics:
Observation of $M_{\text{NS}} \approx 2 M_{\odot}$

Important information
from heavy-ion physics



Flow: Equation-Of-State

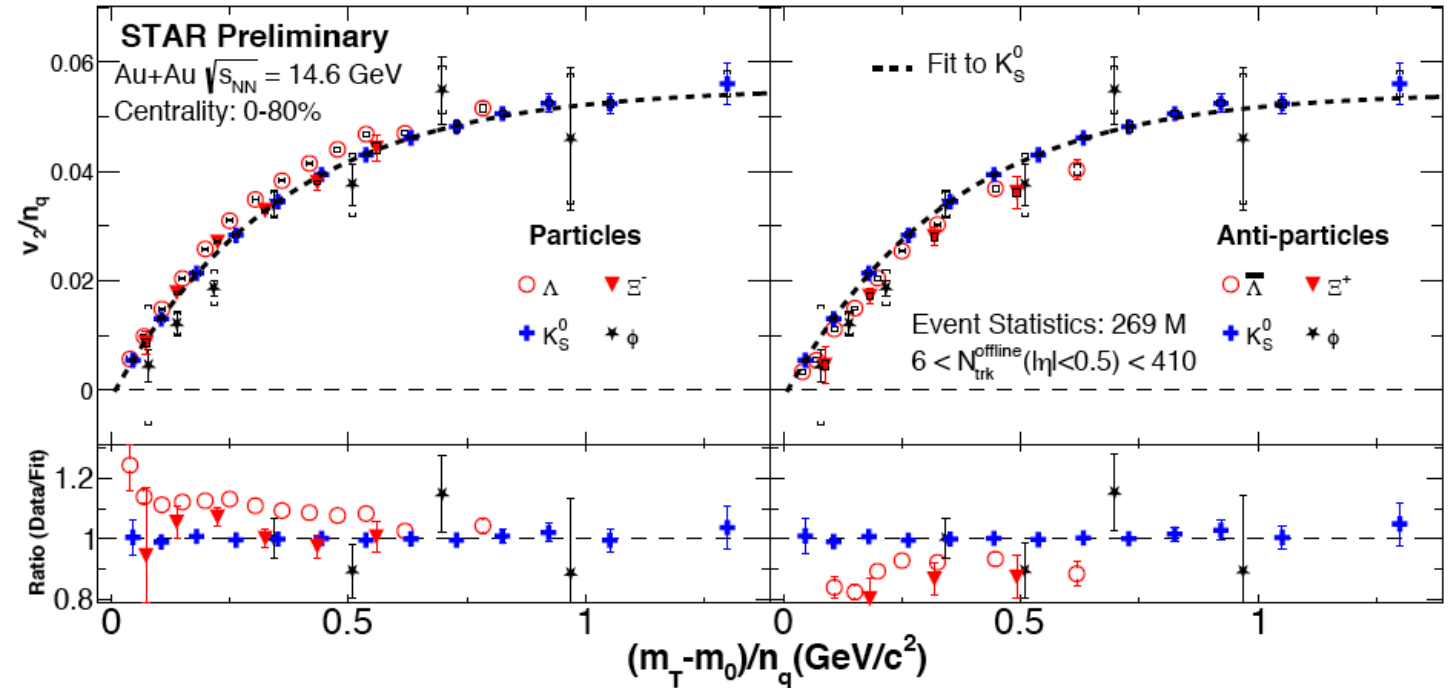


Constituent Quark Scaling

NCQ-Scaling:

v_2 divided by number
of constituent quarks n_q

Holds (within $\sim 20\%$)
at $\sqrt{s_{NN}} = 14.6$ GeV



STAR: Md. Nasim, CPOD22

Constituent Quark Scaling

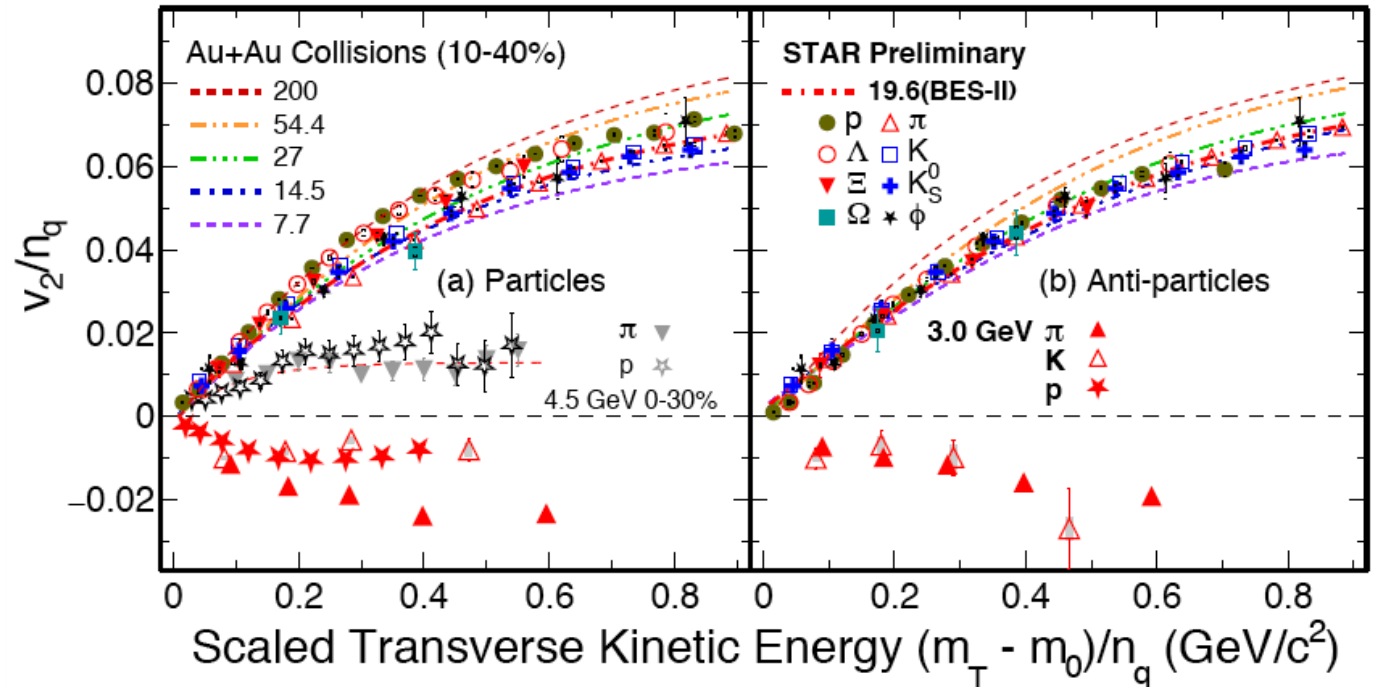
NCQ-Scaling:

v_2 divided by number
of constituent quarks n_q

Holds (within $\sim 20\%$)
at $\sqrt{s_{NN}} = 14.6$ GeV

Seems to be broken
at $\sqrt{s_{NN}} = 3.0$ GeV

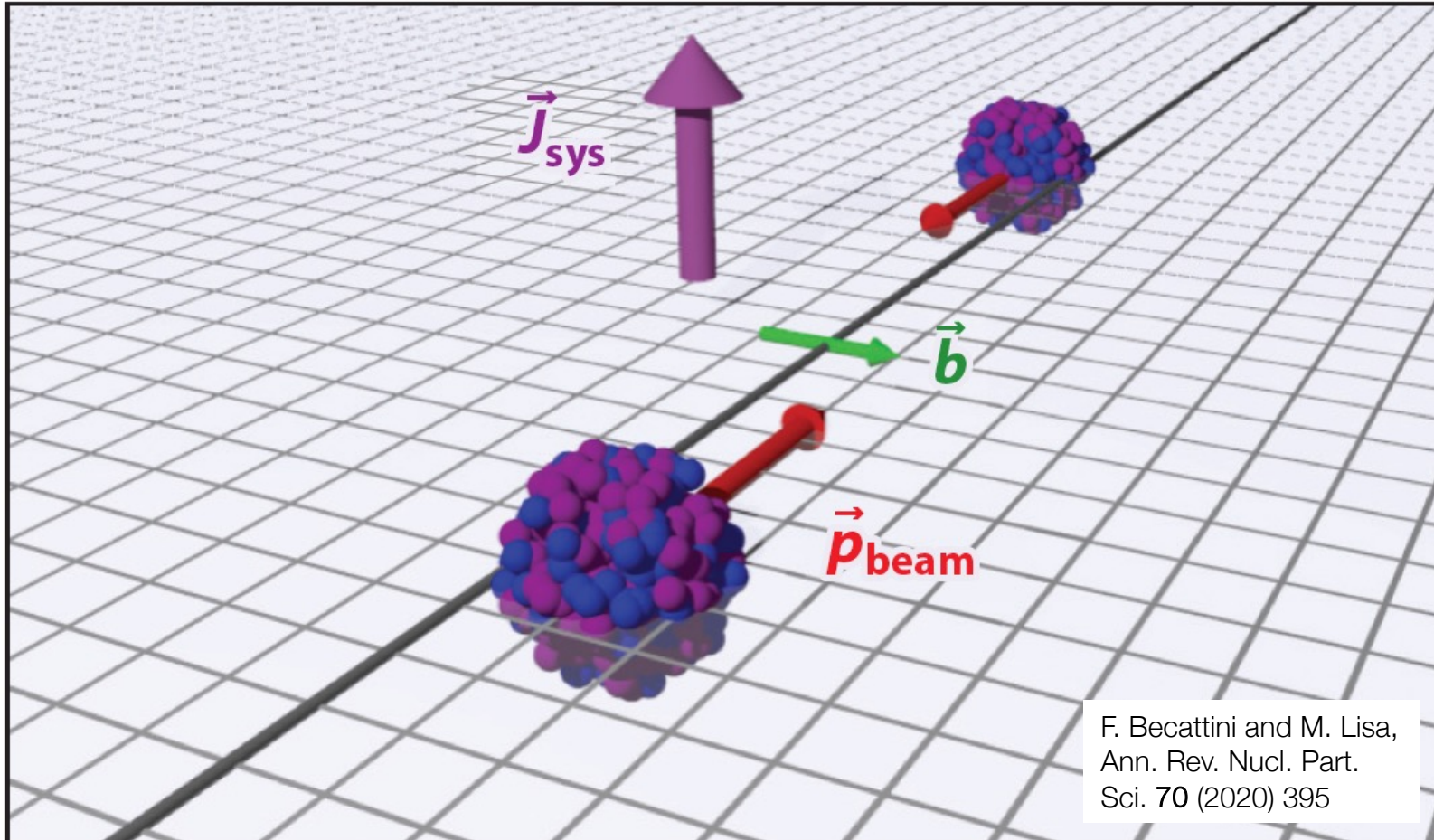
Disappearance of partonic contribution (?)



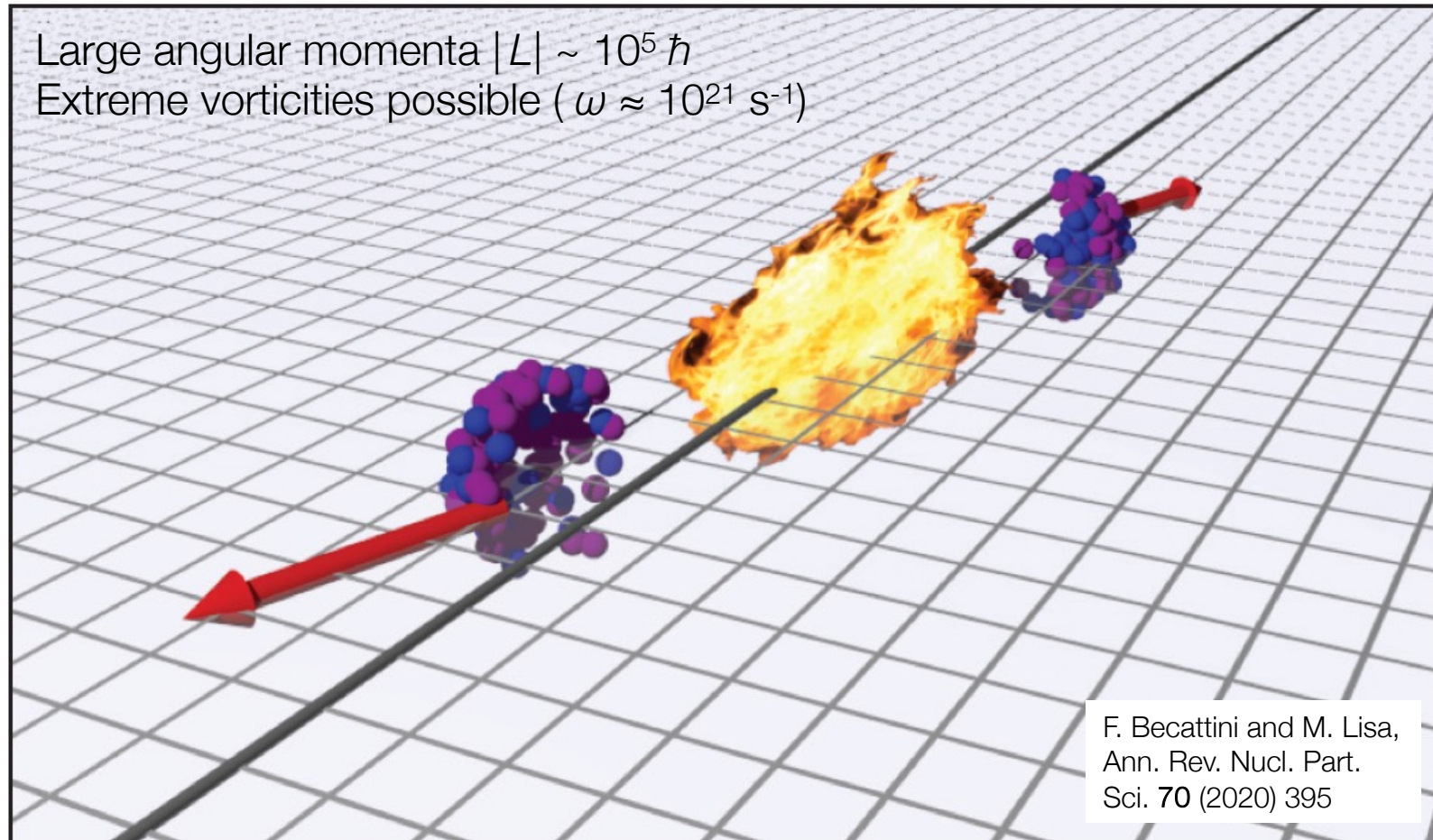
STAR: PLB 827 (2022) 137003

Vorticity

Global Polarization



Global Polarization



Global Polarization

Observable: Λ emission

Weak decay: $\Lambda \rightarrow p + \pi^-$

Proton preferentially in spin direction

$\Rightarrow$ Polarization P_Λ :

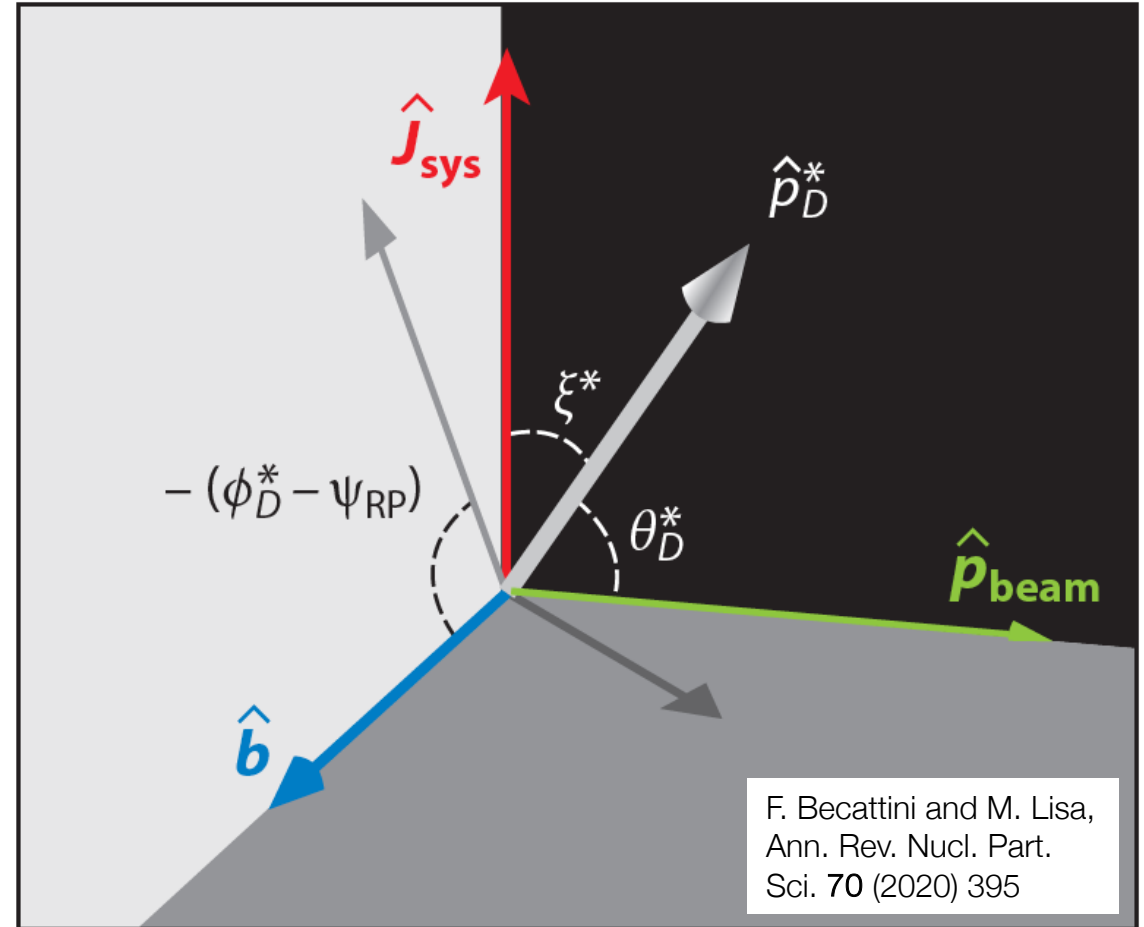
$$P_\Lambda = \frac{8}{\pi \alpha_\Lambda} \frac{\langle \Psi_{EP} - \phi_D^* \rangle}{R_{EP}}$$

Λ decay parameter: $\alpha_\Lambda = 0.732 \pm 0.014$

Ψ_{EP} = event plane angle,

R_{EP} = EP-resolution

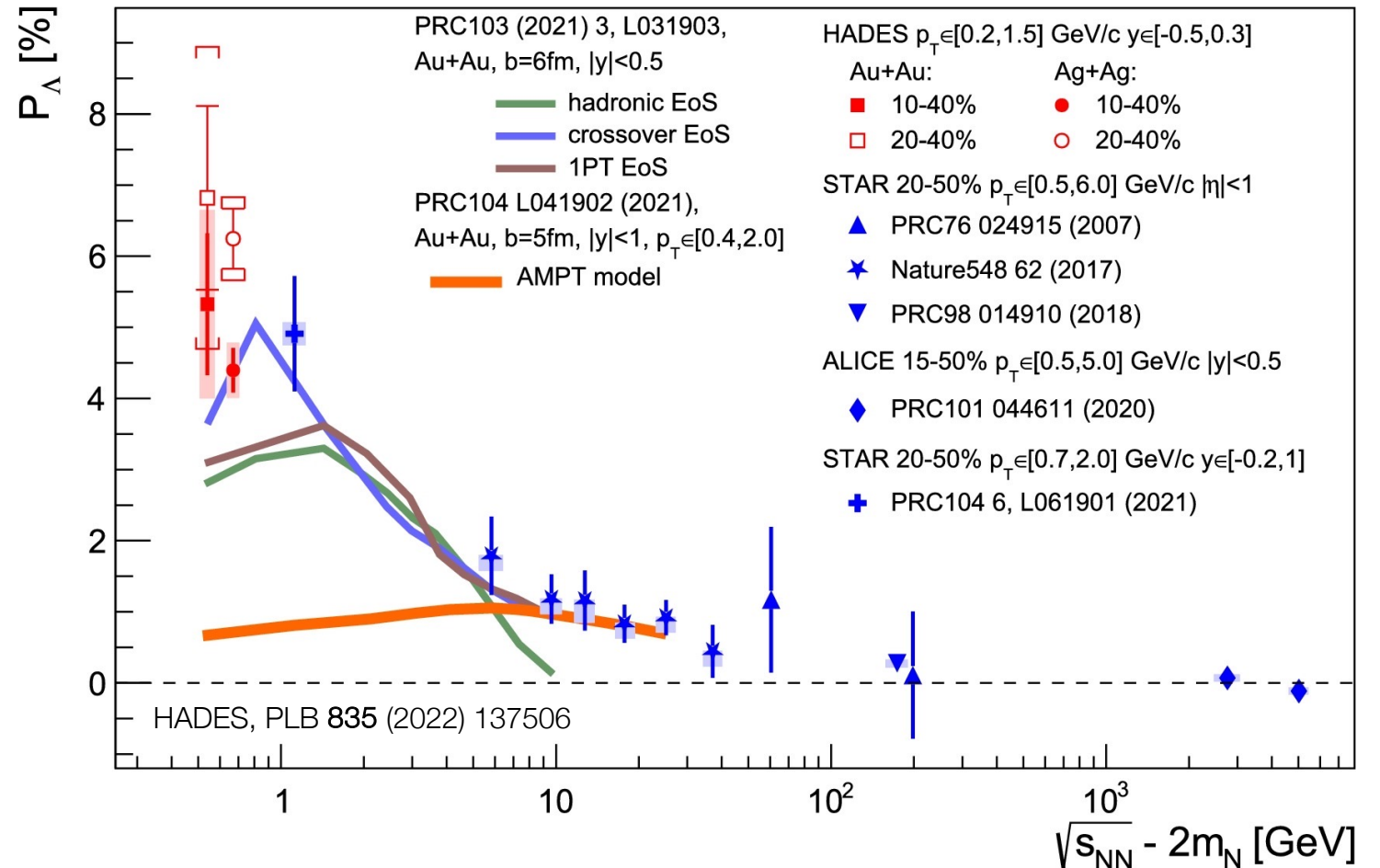
ϕ_D^* = proton azimuth angle relative to EP



Global Polarization

Strong increase of P_Λ
towards lower energies

Agreement with 3D-hydro
AMPT model disfavored



Global Polarization

Difference between $P_{\bar{\Lambda}}$ and P_{Λ}
 No evidence for $P_{\bar{\Lambda}} - P_{\Lambda} > 0$

Relation to late stage magnetic field
 (feed-down effects ignored):

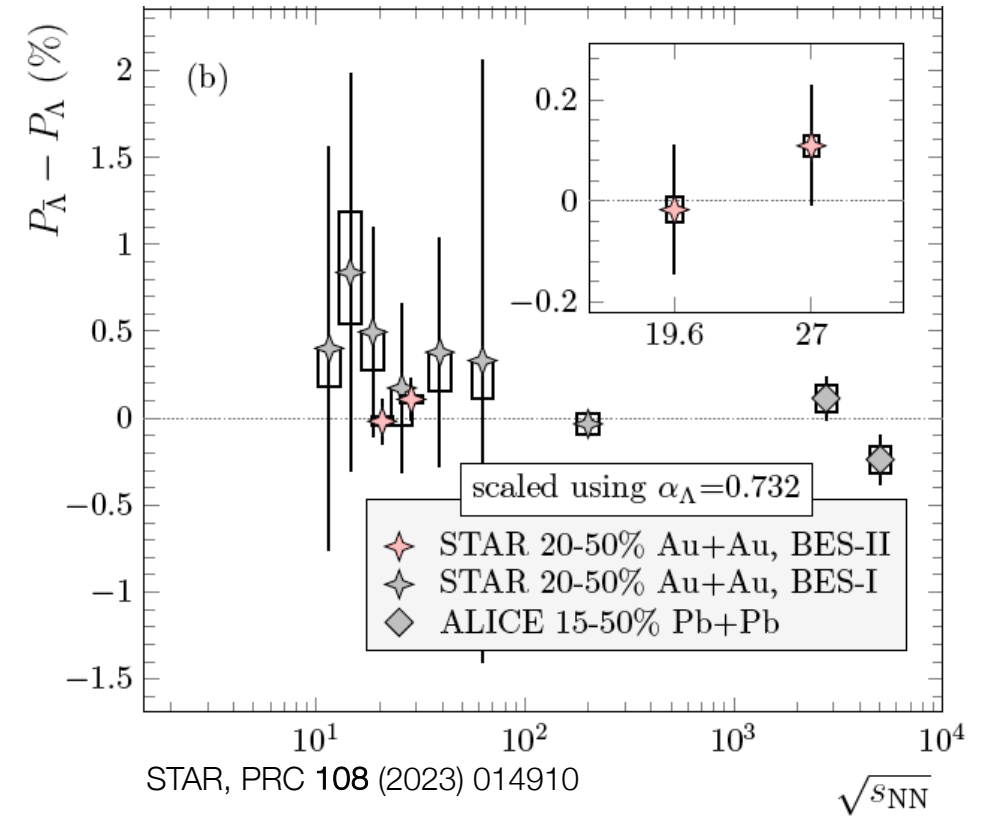
$$|B| \approx \frac{T_s |P_{\bar{\Lambda}} - P_{\Lambda}|}{2|\mu_{\Lambda}|}$$

T_s = Temperature of emitting source

μ_{Λ} = Magnetic moment of Λ

Upper limits:

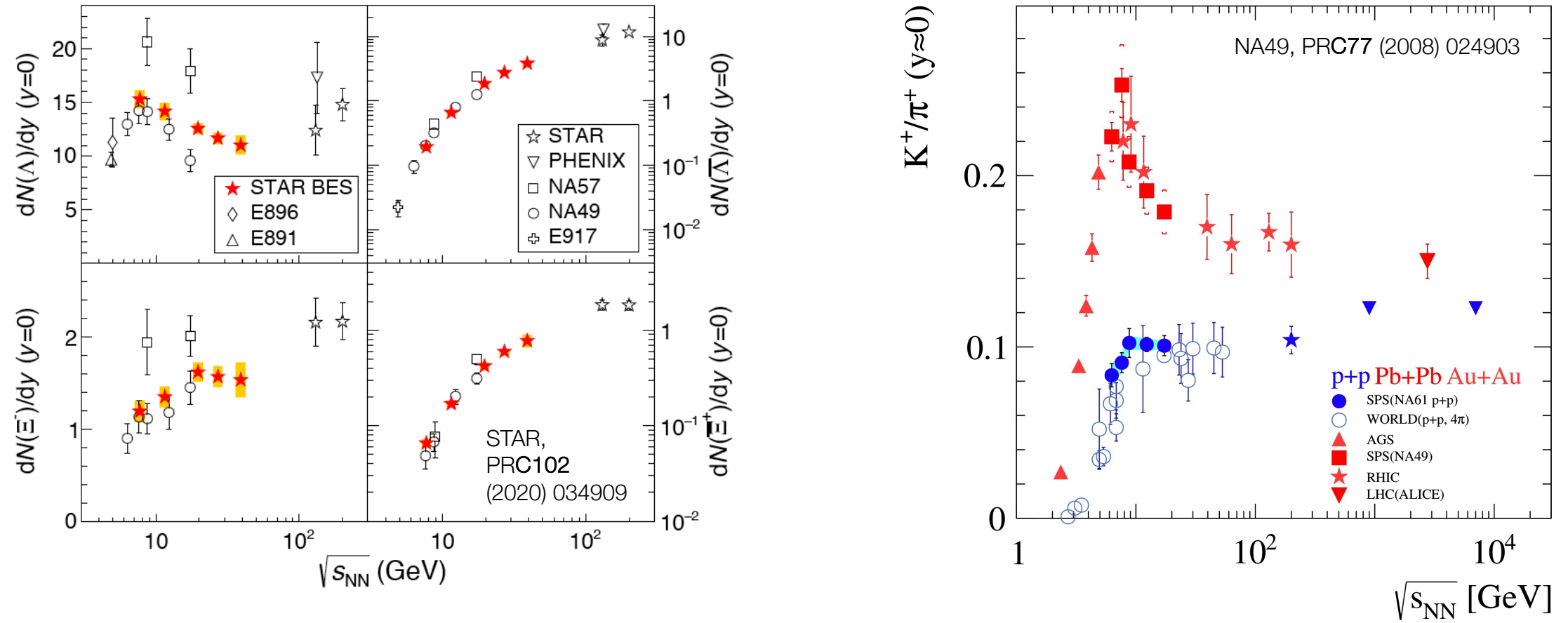
$B < 9.4 \times 10^{12}$ T at $\sqrt{s_{NN}} = 19.6$ GeV ($B < 1.4 \times 10^{13}$ T at $\sqrt{s_{NN}} = 27$ GeV)



Strangeness in Matter

Hypernuclei

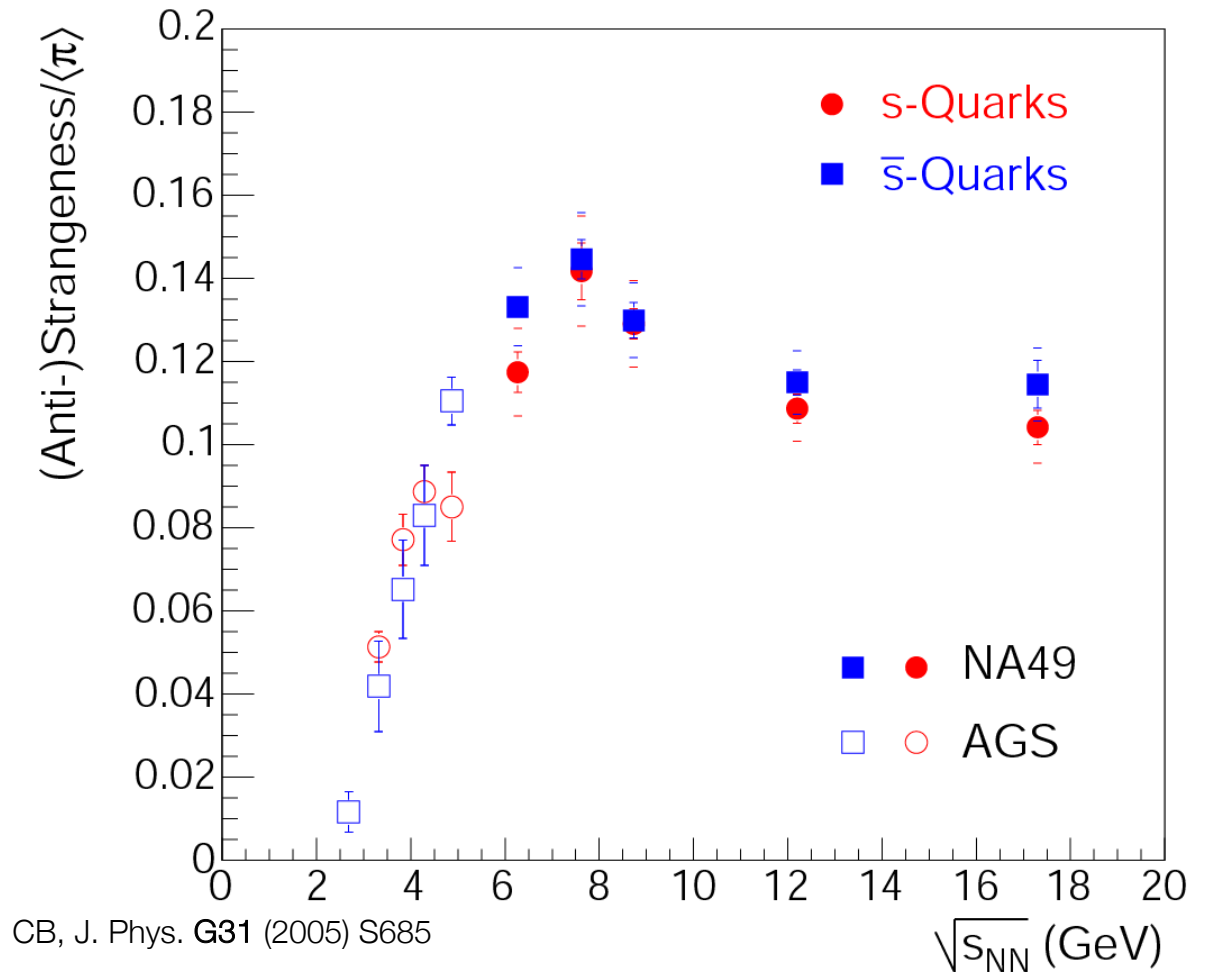
Production of Strange Particles



Structures in energy dependence (e.g. maxima for Λ , K^+/π^+)

Production of Strange Particles

Relative strangeness production is maximal around $\sqrt{s_{NN}} = 6 - 8$ GeV

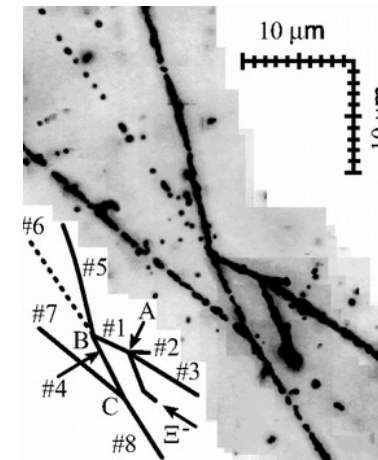
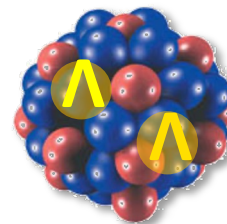
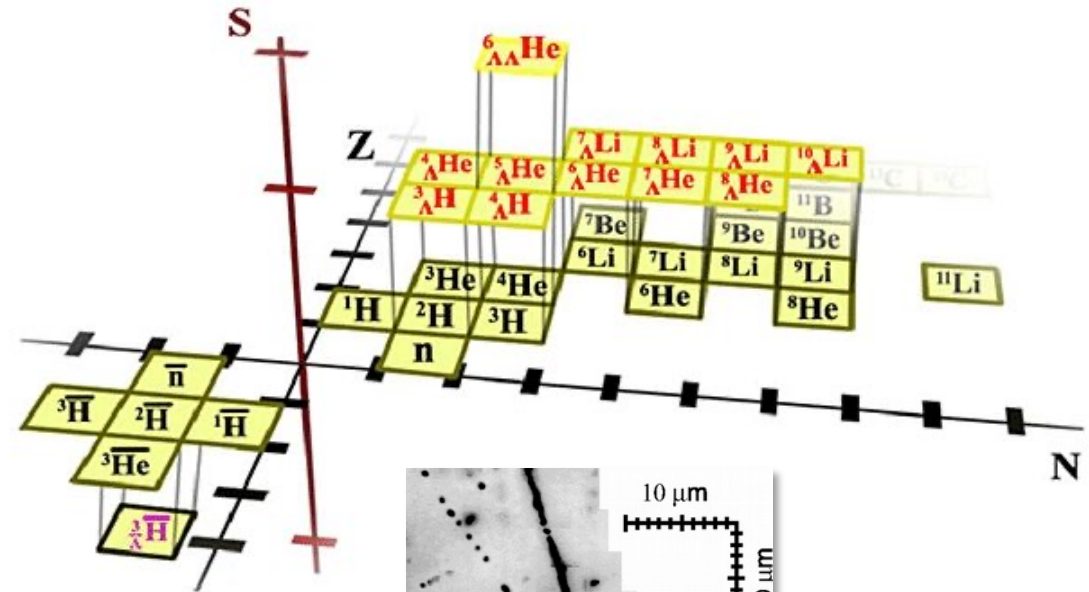


Hypernuclei

Nuclei with Λ replacing neutron(s)

Important information
hyperon-nucleon interactions
 $\Rightarrow$ change in binding energy

Double- Λ hypernuclei
particularly interesting
(so far only handful events!)



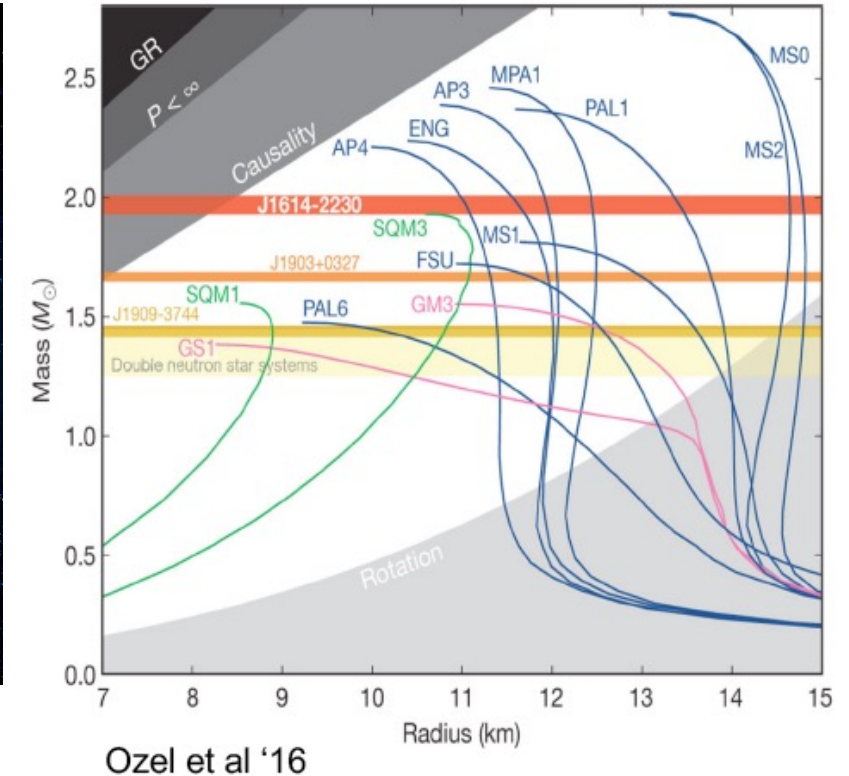
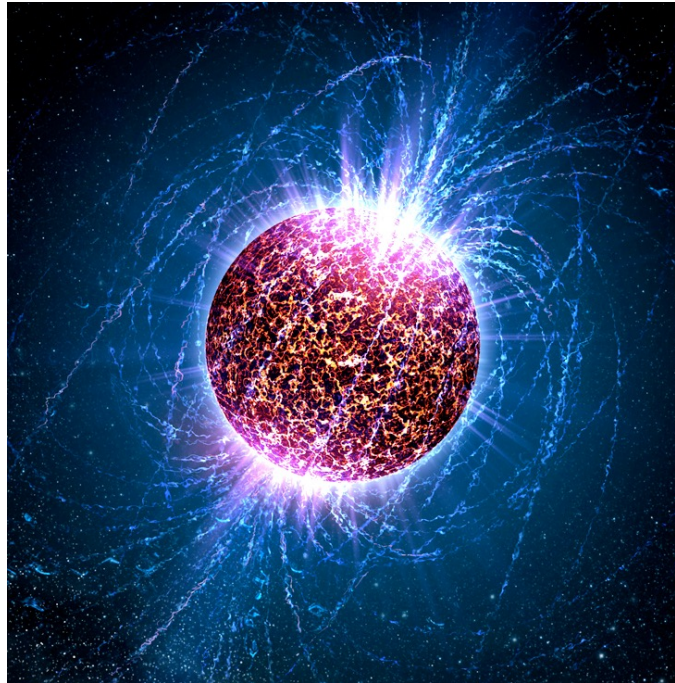
Discovery of ${}^6_{\Lambda\Lambda}\text{He}$
by Danysz
and Pniewski
in photo emulsion

Hypernuclei + Neutron Stars

Mass-radius relation:
Depends on EOS of
dense nuclear matter

Constraints from
observation of
 $M_{\text{NS}} \approx 2 M_{\odot}$

Important information
from heavy-ion physics



Hypernuclei + Neutron Stars

Hyperon-puzzle

Hyperons should appear
when density increases

$\Rightarrow$ EOS softens with hyperon matter

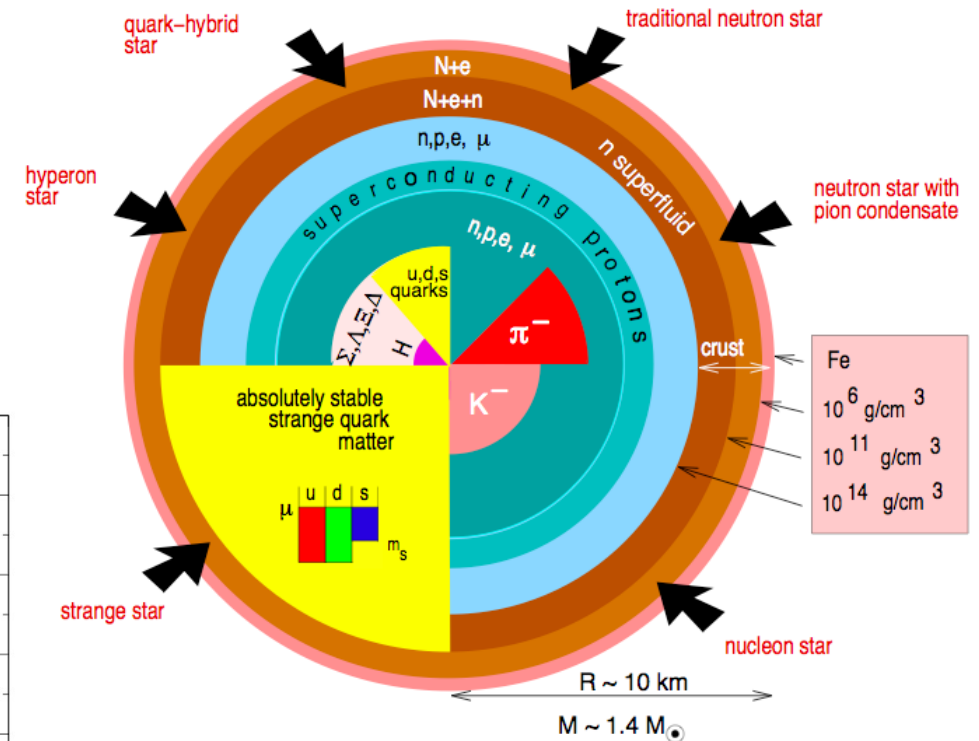
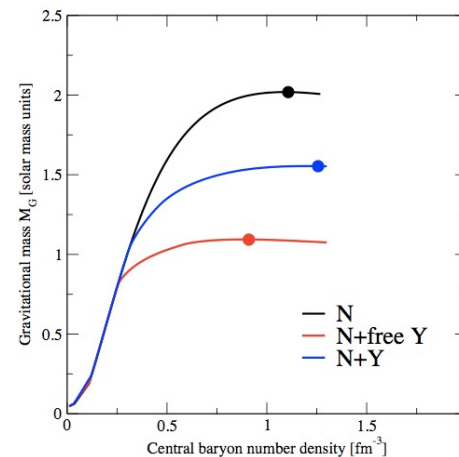
$\Rightarrow 2 M_{\odot}$ cannot be reached

YN and YY interaction

Repulsive YN and YY
interactions $\Rightarrow$ stiffer EOS

3-body forces between Ys

Important input from hypernuclei measurements



Production in Heavy-Ion Collisions

Statistical model

Based on parametrization:

$$T = T(\sqrt{s_{NN}}) \text{ and } \mu_B = \mu_B(\sqrt{s_{NN}})$$

Predictions for the CBM energy range

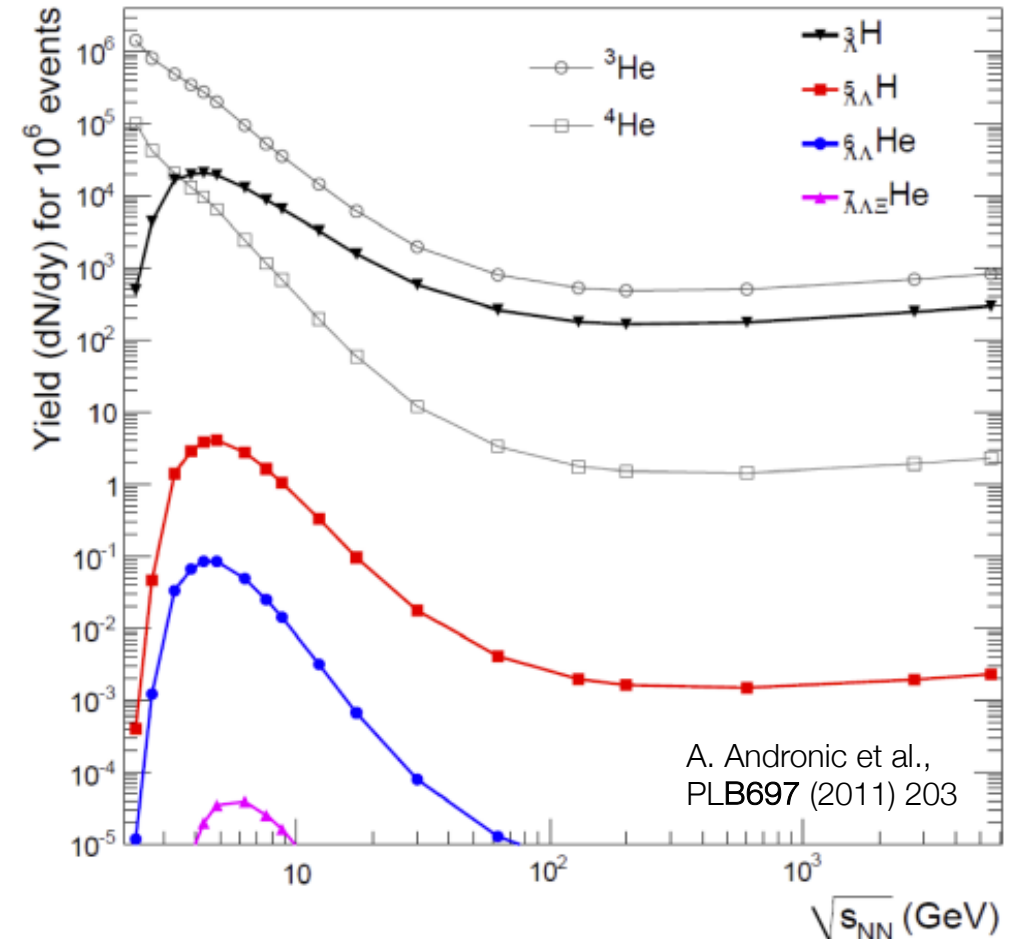
Hypernuclei production favored
at low $\sqrt{s_{NN}}$, i.e. low μ_B

Expected rates

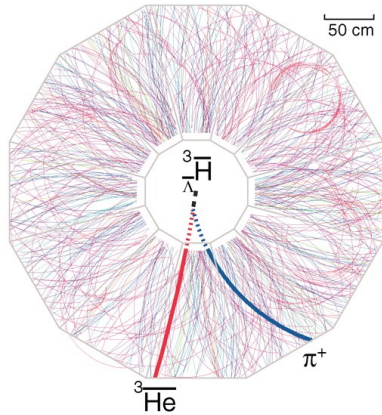
Double- Λ hypernuclei:

$\sim 10^{-6}/\text{evt.}$ — $\sim 10^{-11}/\text{evt.}$ in CBM range

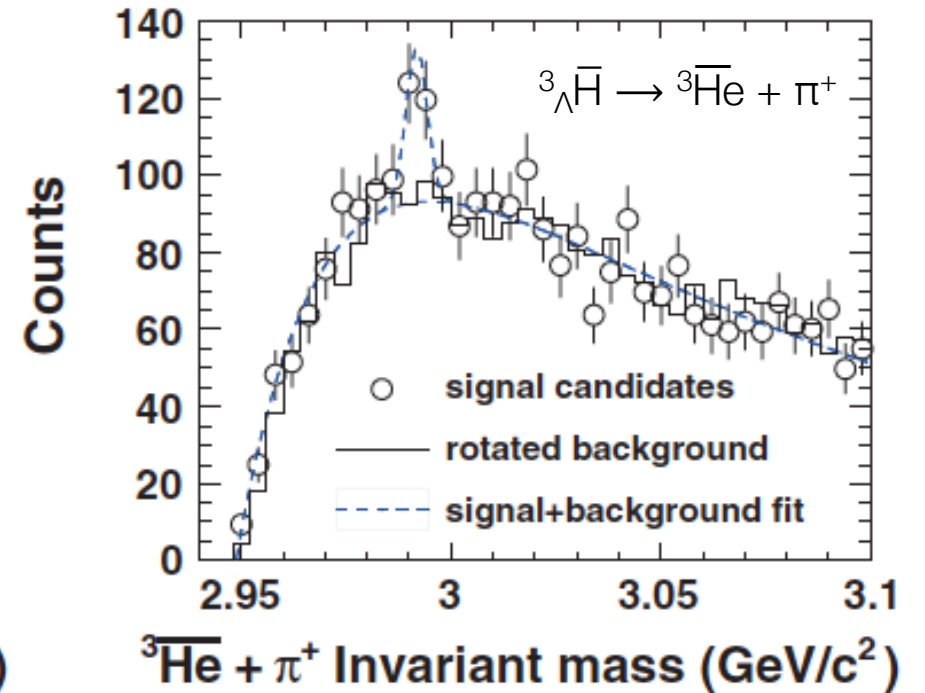
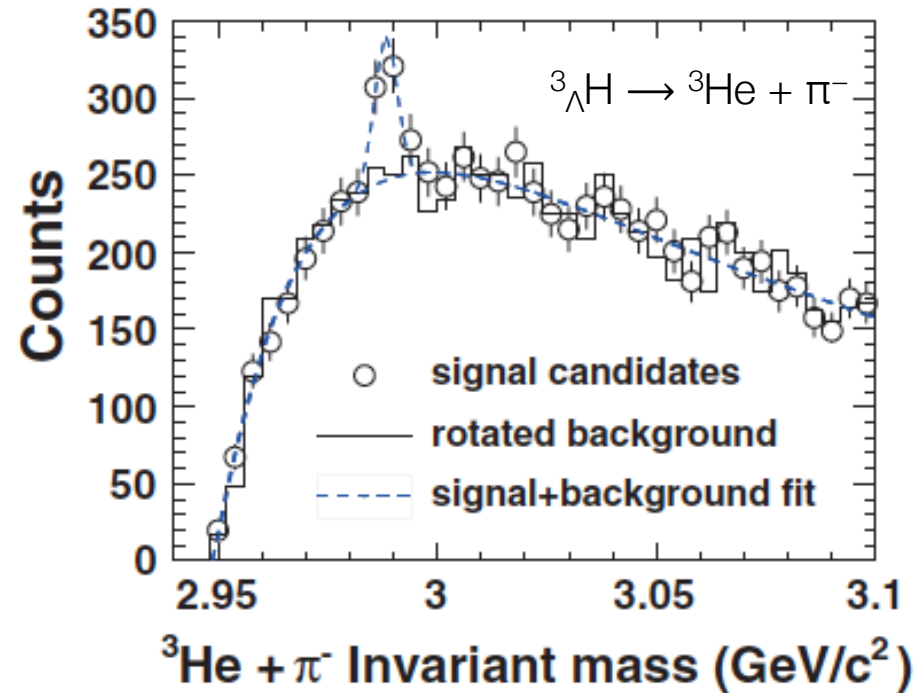
High interaction rates needed



(Anti-)Hypertriton



STAR,
Science 328 (2010) 58



First observation of an anti-hypernucleus (Au+Au at $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$)

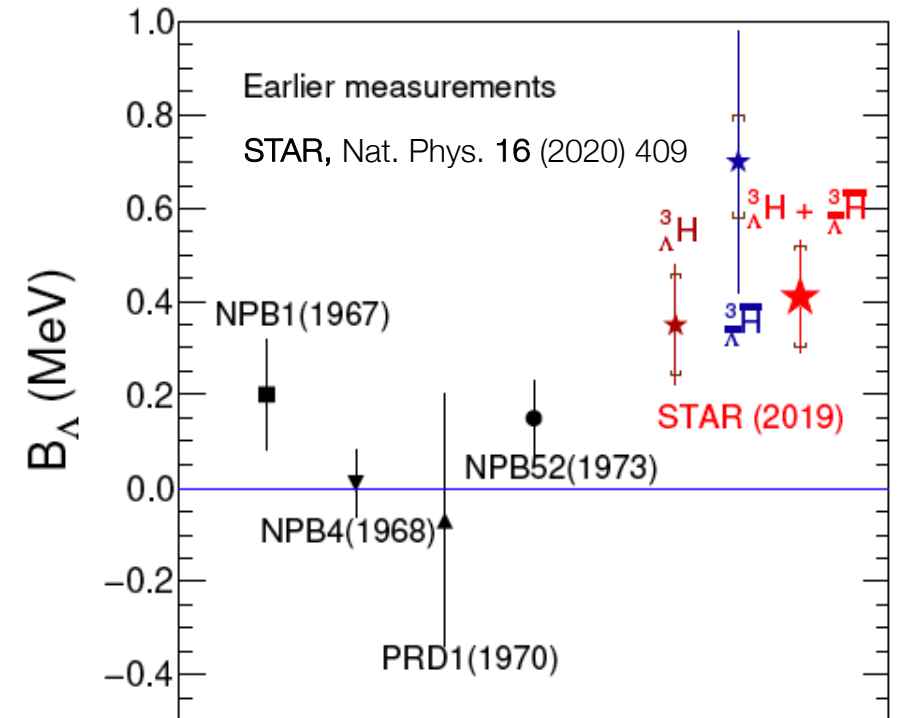
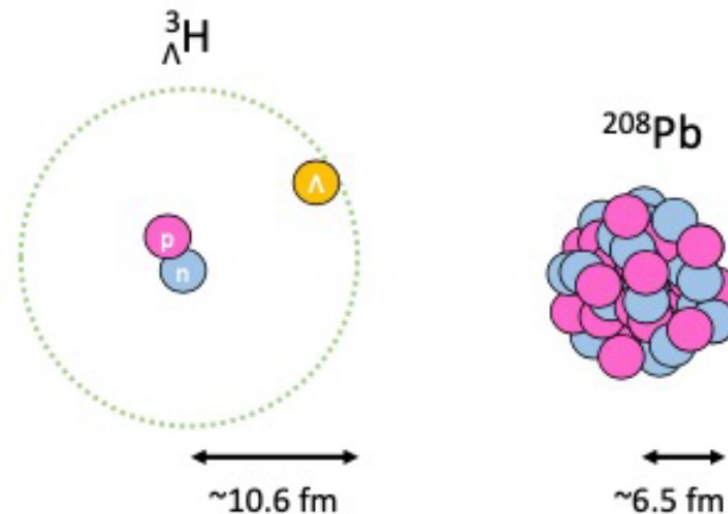
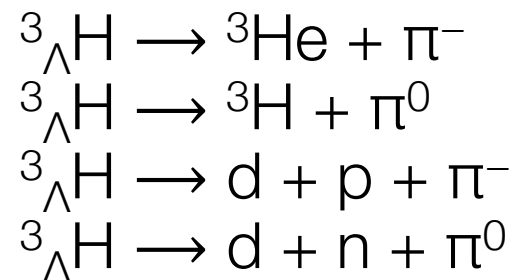
Hypertriton

Loosely bound object

Λ binding energy: $B_\Lambda \approx 400$ keV
(compare $B_d = 2.2$ MeV)

Wavefunction is larger than Pb-nucleus

Decay modes



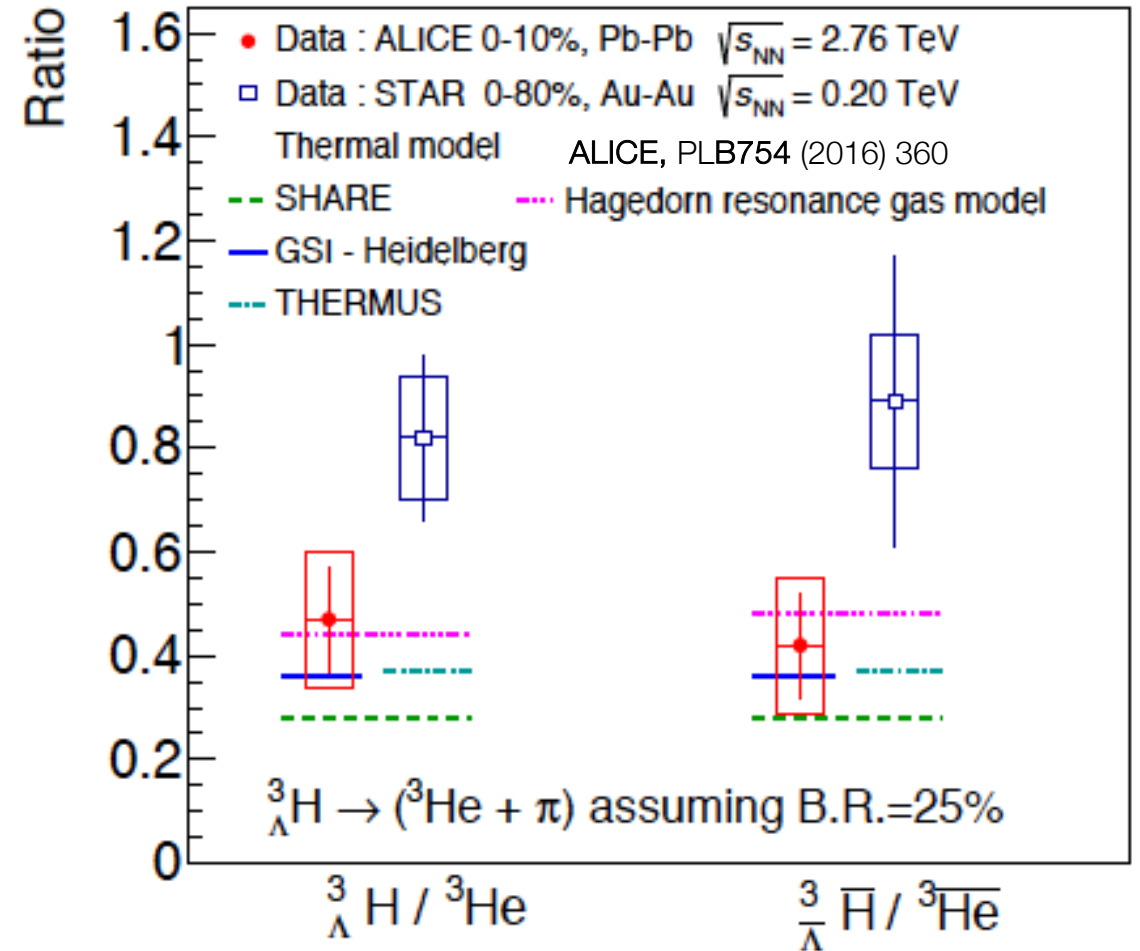
Hypertriton Yield

Ratio hypertriton/ ^3He

Good agreement with
thermal fireball prediction
for temperature $T \sim 150$ MeV

“Ice in fire” / “Snowball in hell”

How does a weakly bound object
($B_\Lambda \approx 0.4$ MeV) survive in a fireball with
freeze-out temp. of ~ 150 MeV?

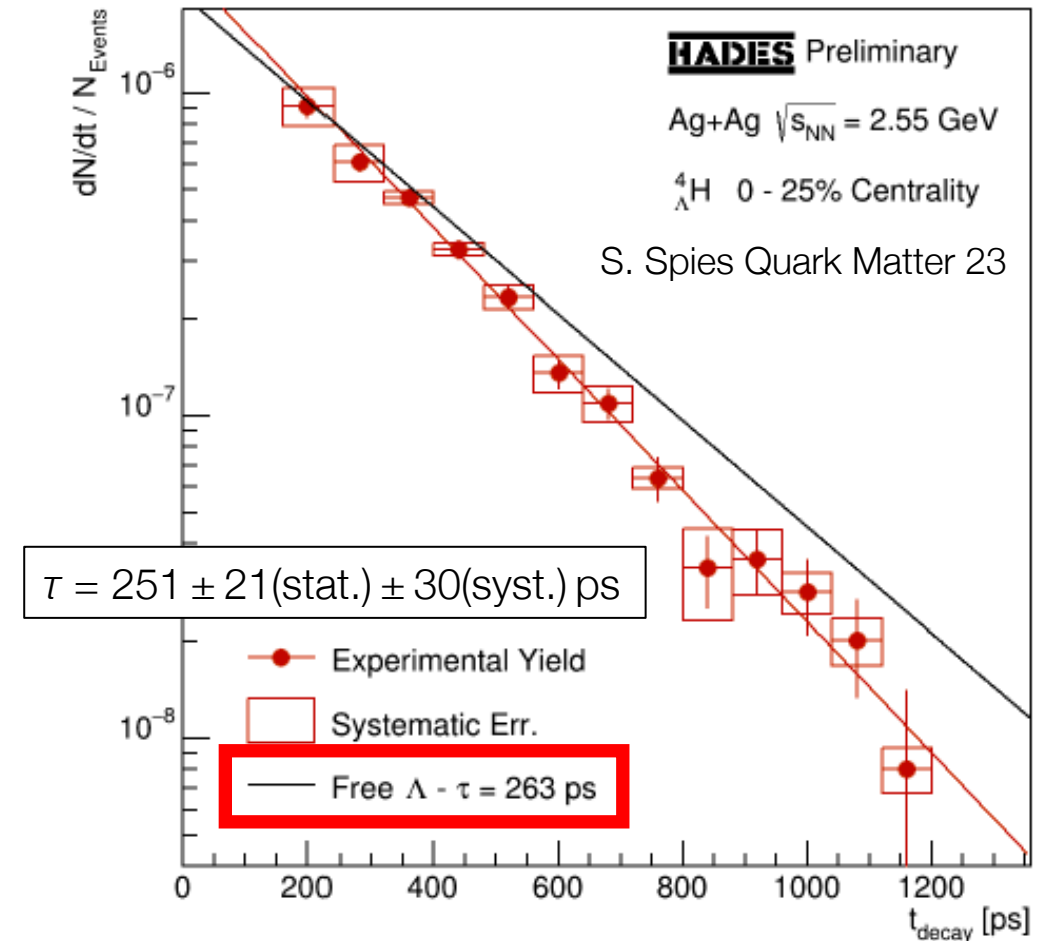
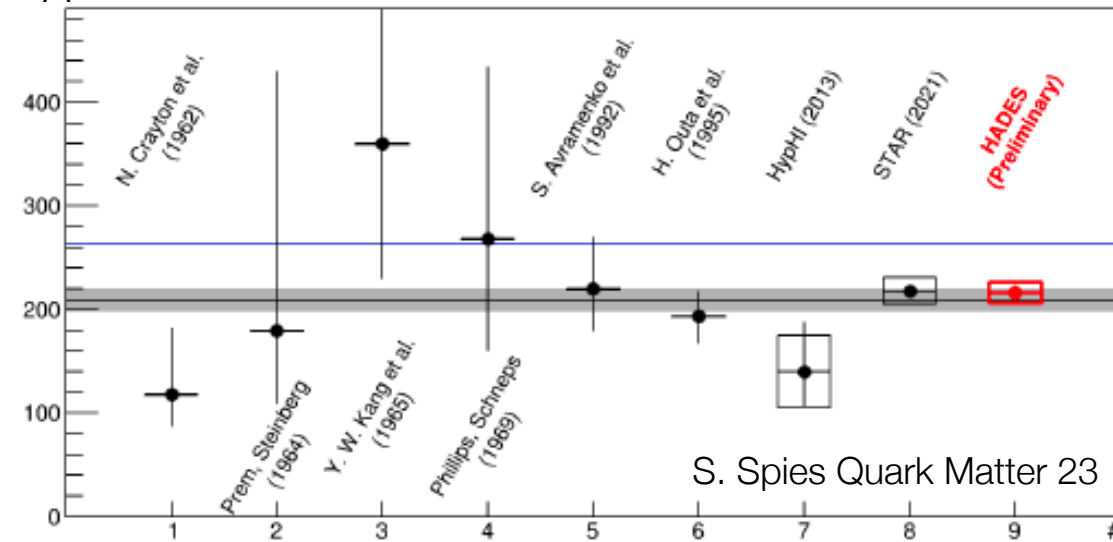


Hypertriton Lifetime

Hypertriton lifetime “puzzle”

Lifetime smaller than the one of free Λ ?
Recent data rather agree for ${}^3_\Lambda\text{H}$

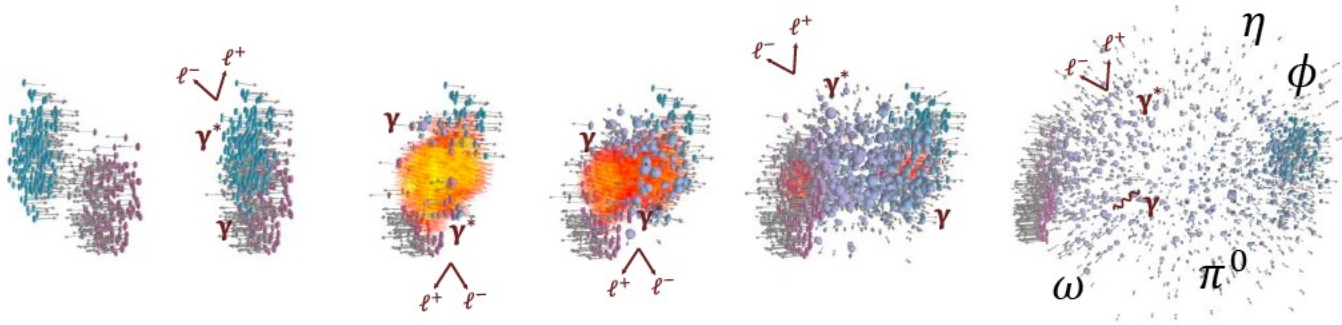
${}^4_\Lambda\text{H}$: $\sim 4.9\sigma$ deviation observed



Emissivity

Photons

Electromagnetic radiation (γ and γ^*) emitted during full fireball evolution



No strong interaction with medium $\Rightarrow$ escape unmodified

Sources of di-leptons ($\gamma^* \rightarrow e^+ e^-$, $\gamma^* \rightarrow \mu^+ \mu^-$):

Dalitz-decays ($\pi^0 / \eta \rightarrow e^+ e^- \gamma$)

Low mass range: vectormeson decays (ρ , ω , ϕ) $\Rightarrow$ medium modifications

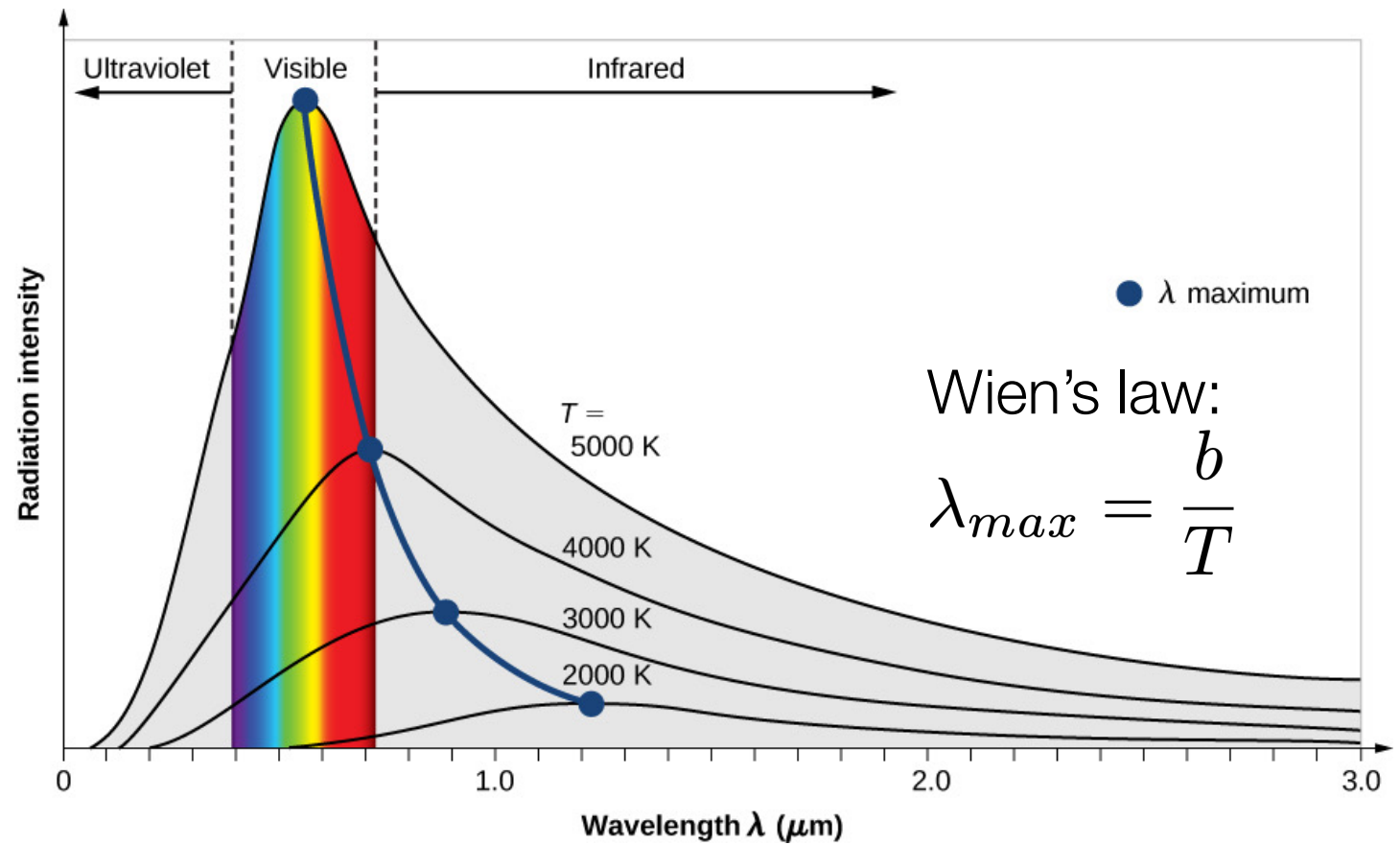
Intermediate mass range: thermal radiation (open charm)

Photons: Thermal Radiation

Black body radiation

$$B(\nu, T) = \frac{2 h \nu^3}{c^2} \frac{1}{\exp\left(\frac{h \nu}{k_B T}\right) - 1}$$

Planck's formula



Di-Electron Spectrum

Reference NN spectrum

$$\frac{dN_{\text{ref}}^{\text{NN}}}{dM_{ee}} = \left(0.54 \frac{dN^{pp}}{dM_{ee}} + 0.46 \frac{dN^{np}}{dM_{ee}} \right) \langle A_{\text{part}} \rangle$$

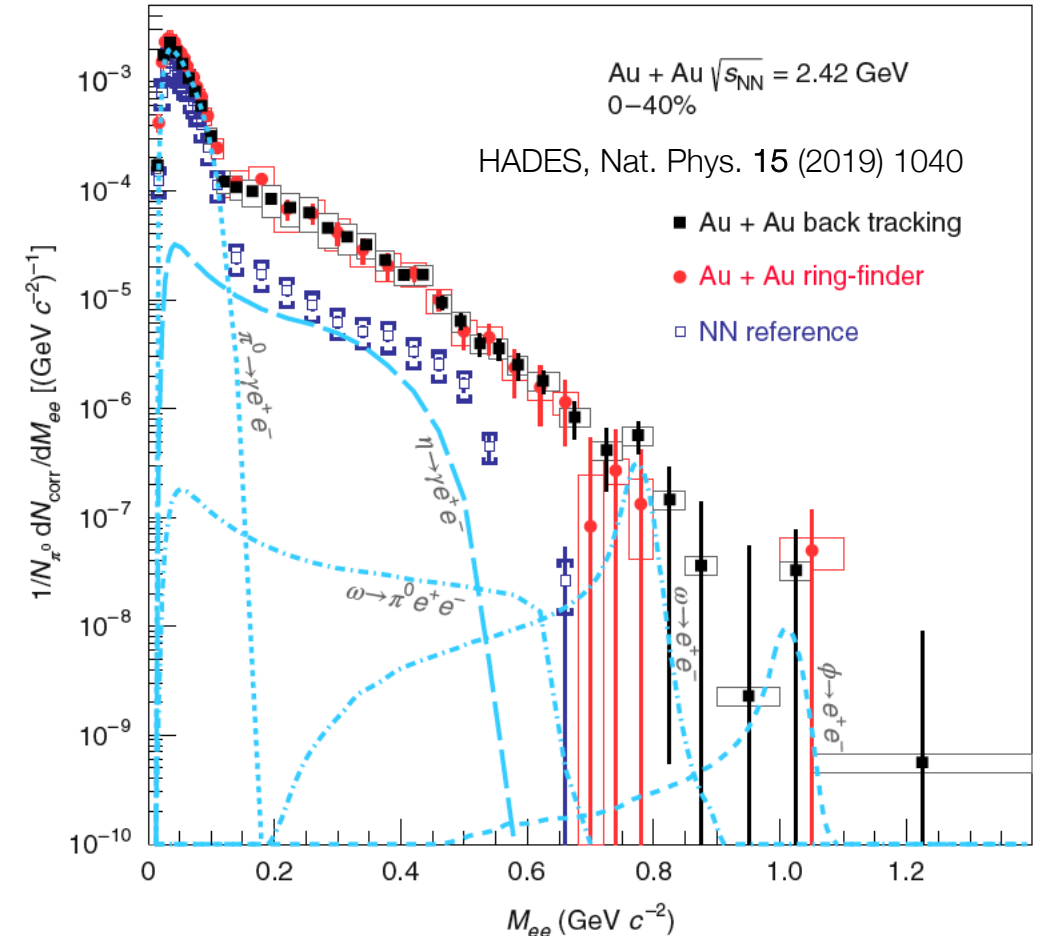
Hadronic contributions (w/o ρ)

$$\pi^0 / \eta \rightarrow e^+ e^- \gamma$$

$$\omega / \phi \rightarrow e^+ e^-$$

$$\omega \rightarrow \pi^0 e^+ e^-$$

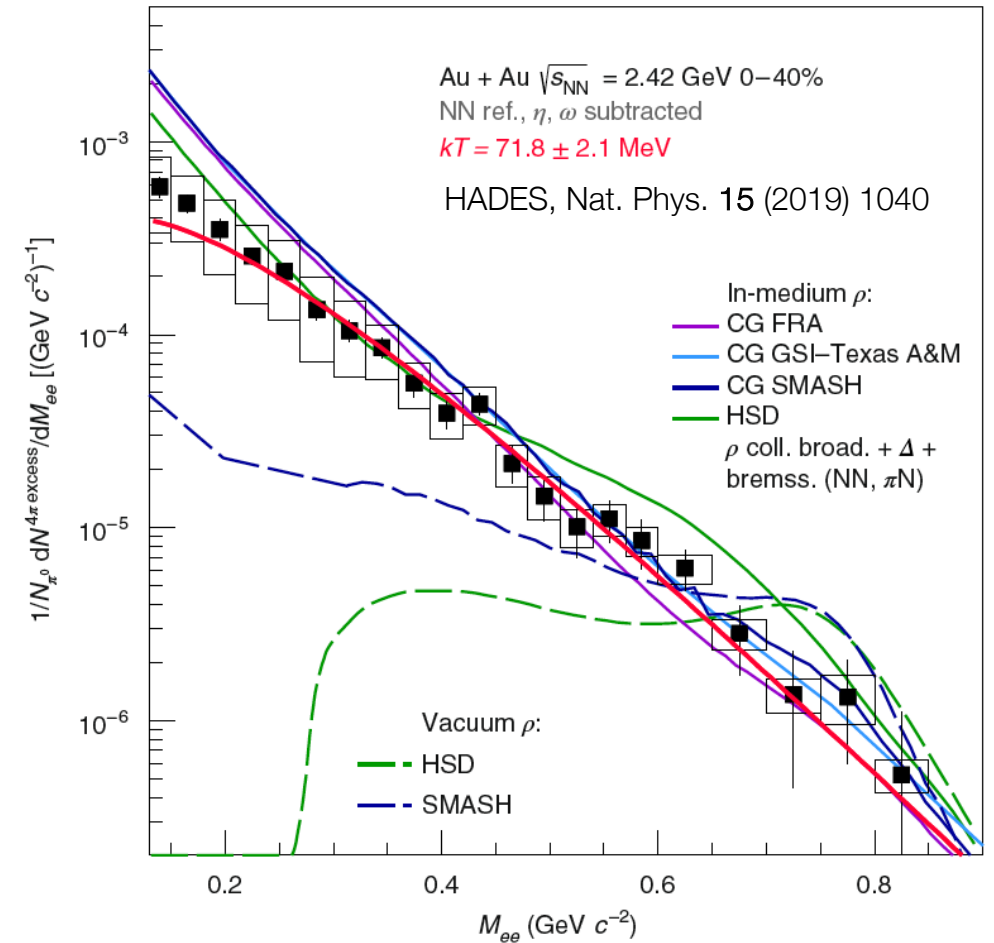
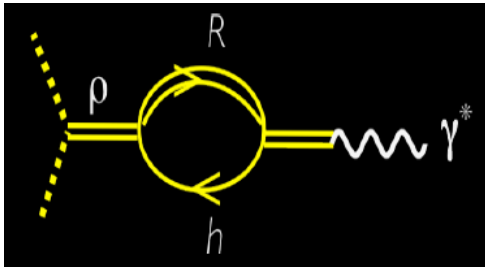
Subtraction of reference
 $\Rightarrow$ Excess radiation



Di-Electron Spectrum

Subtraction of reference
 $\Rightarrow$ **Excess radiation**

Not described by vacuum ρ
 Broadening due to ρ -baryon scattering



Di-Electron Spectrum

Subtraction of reference
⇒ **Excess radiation**

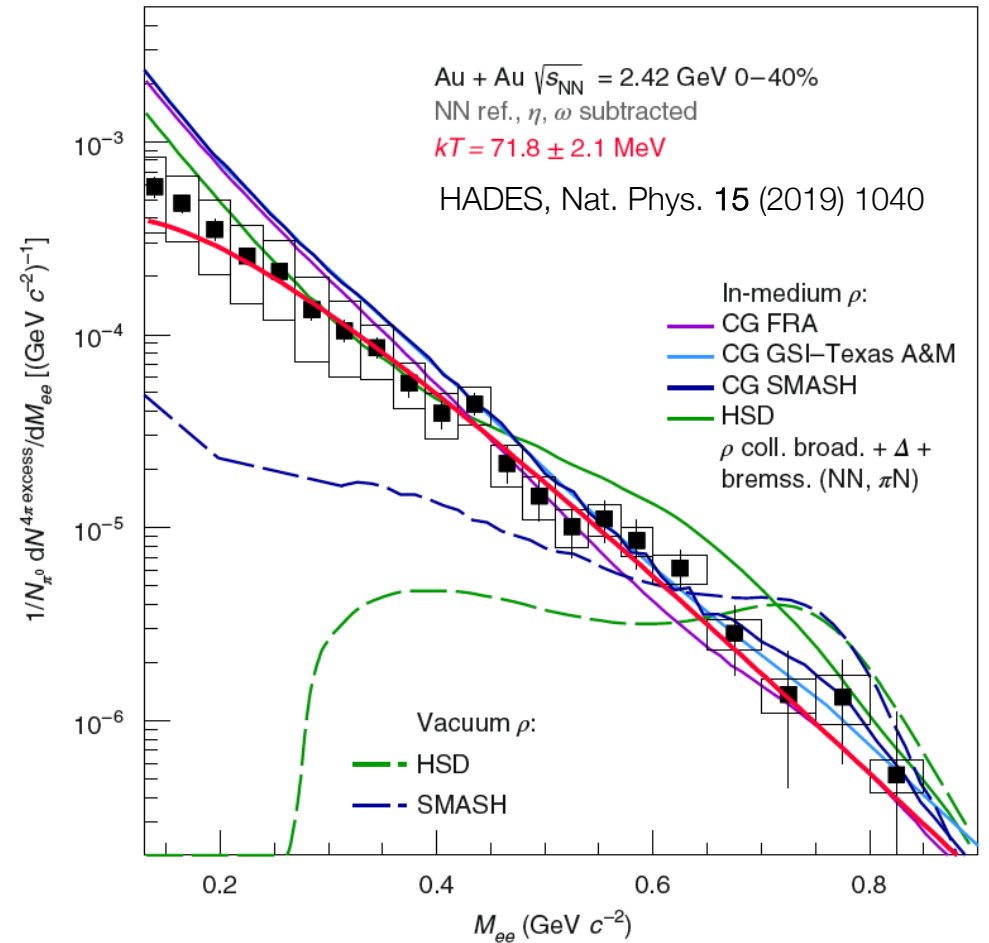
Calculations with in-medium ρ spectral functions, folded with fireball evolution from coarse-grained transport

In-medium propagator: R. Rapp and H. van Hees, PLB **753** (2016) 586
 $\rho - \omega$ chiral mixing: R. Rapp and P. Hohler, PLB **731** (2014) 103
CG FRA: S. Endres et al., PRC **92** (2015) 014911
CG GSI-TAMU: T. Galatyuk, F. Seck et al., EPJA **52** (2016) 131
CG SMASH: J. Staudenmaier et al., PRC **98** (2018) 054908.
HSD transport model: E. Bratkovskaya et al., PRC **87** (2013) 064907.

Thermal radiation of medium

Exponential spectrum $\rightarrow$ black body rad.

Fit result: $T_{\text{rad}} = 71.8 \pm 2.1 \text{ MeV}$

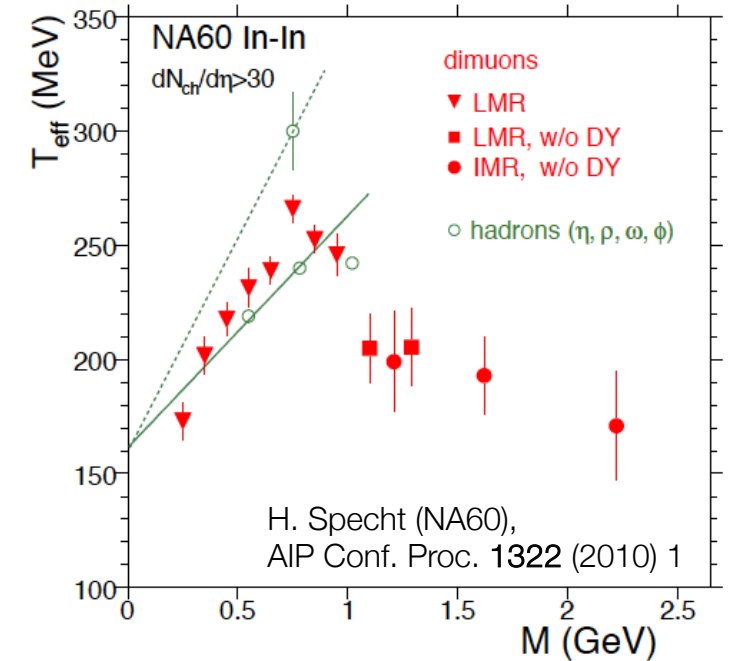
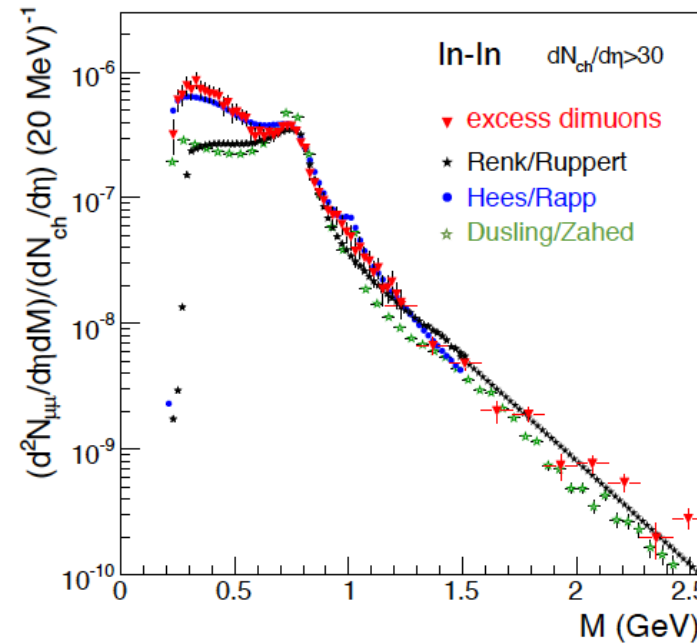


Di-Muon Spectrum

Subtraction of reference
 $\Rightarrow$ **Excess radiation**

Inverse slope parameter
 T_{eff} depends on mass M
of di-muon-pairs

Thermal radiation
at intermediate masses

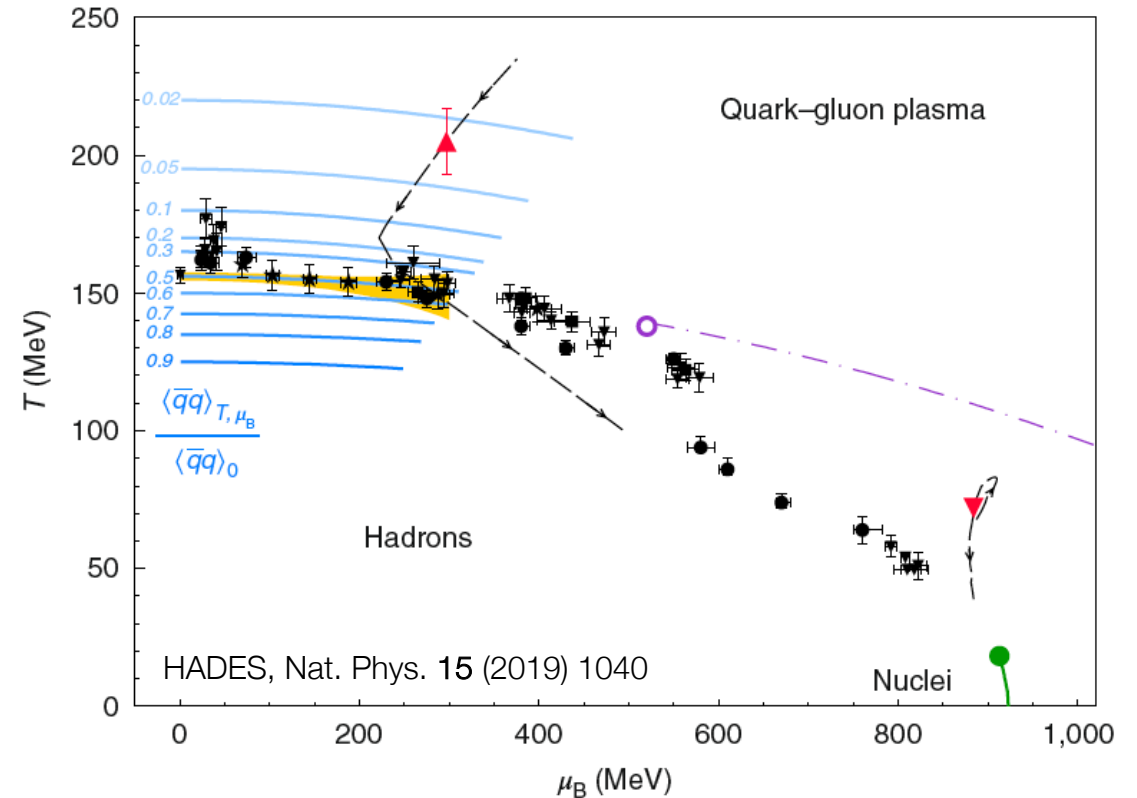


Thermal Radiation

QCD Phase diagram with
inverse slope parameters T_{eff}

Information on the early
phases of the fireball

Thermometer
Chronometer
Barometer

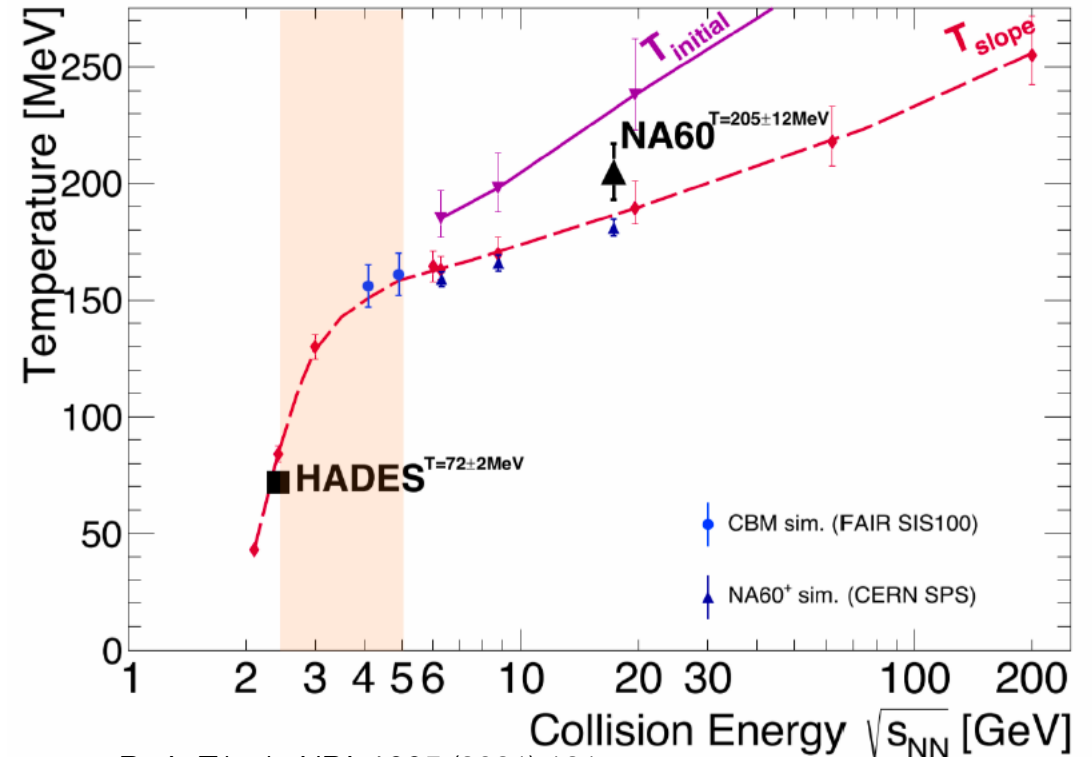


Thermal Radiation

Energy dependence

Sensitivity to the order of the phase transition?

Important physics case for CBM and NA60+



R.-A. Tripolt, NPA **1005** (2021) 121755

NA60, EPJC **61** (2009) 711

HADES, Nat. Phys. **15** (2019) 1040

$\sqrt{s_{NN}} > 6$ GeV: R. Rapp and H. v. Hess, PLB **753** (2016) 586

$\sqrt{s_{NN}} < 6$ GeV: T. Galatyuk et al.: EPJA **52** (2016) 131

Di-Leptons: Future Experiments

