

# The physics of binary neutron star mergers

## Lecture II

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# Plan of the lectures

\*Lecture I: the **math** of neutron-star mergers

\*Lecture II: the **physics** of neutron-star mergers

\*Lecture III: the **astrophysics** of neutron-star mergers

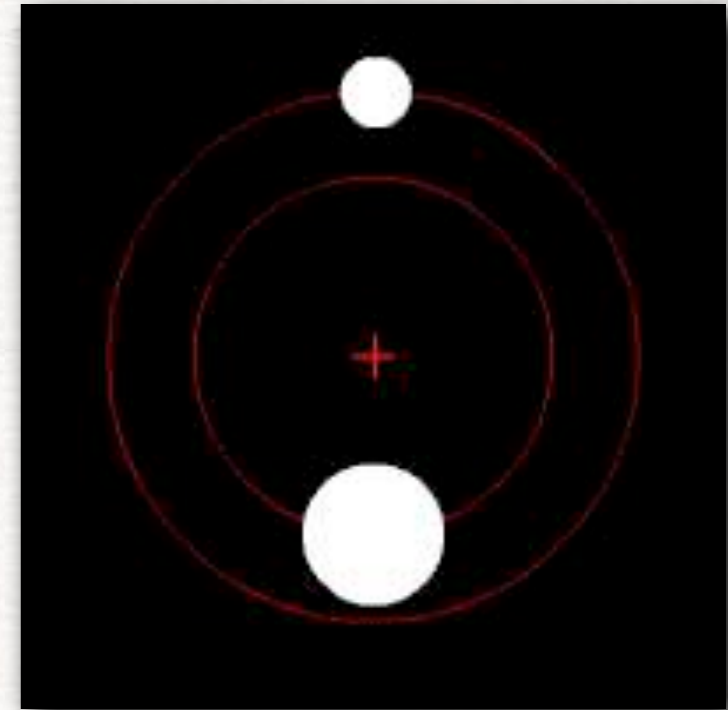
\*L. Baiotti and L. Rezzolla, Rep. Prog. Phys. 80, 096901, 2017

\*V. Paschalidis, Classical Quantum Gravity 34, 084002 2017

\*Rezzolla and Zanotti, "*Relativistic Hydrodynamics*", Oxford University Press, 2013

# The two-body problem: Newton vs Einstein

Take two objects of mass  $m_1$  and  $m_2$  interacting only gravitationally



In **Newtonian gravity** solution is analytic: there exist **closed** orbits (circular/elliptic) with

$$\ddot{\mathbf{r}} = -\frac{GM}{d_{12}^3} \mathbf{r}$$

where  $M \equiv m_1 + m_2$ ,  $\mathbf{r} \equiv \mathbf{r}_1 - \mathbf{r}_2$ ,  $d_{12} \equiv |\mathbf{r}_1 - \mathbf{r}_2|$ .

In **Einstein's gravity** no analytic solution! **No closed** orbits: the system loses energy/angular momentum via gravitational waves.

# The two-body problem in GR

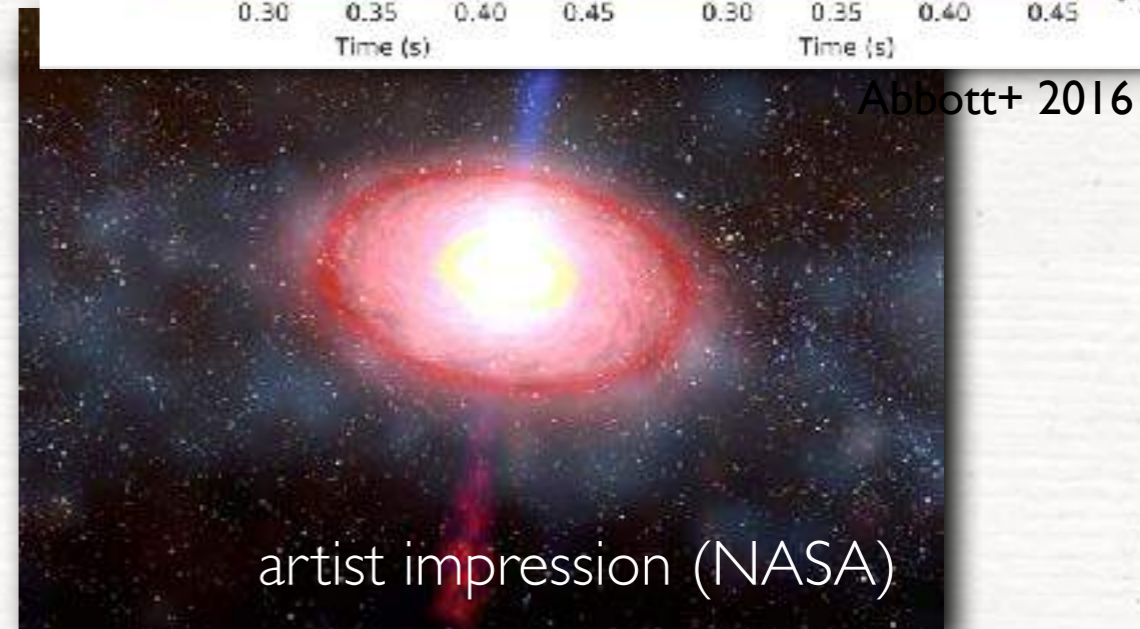
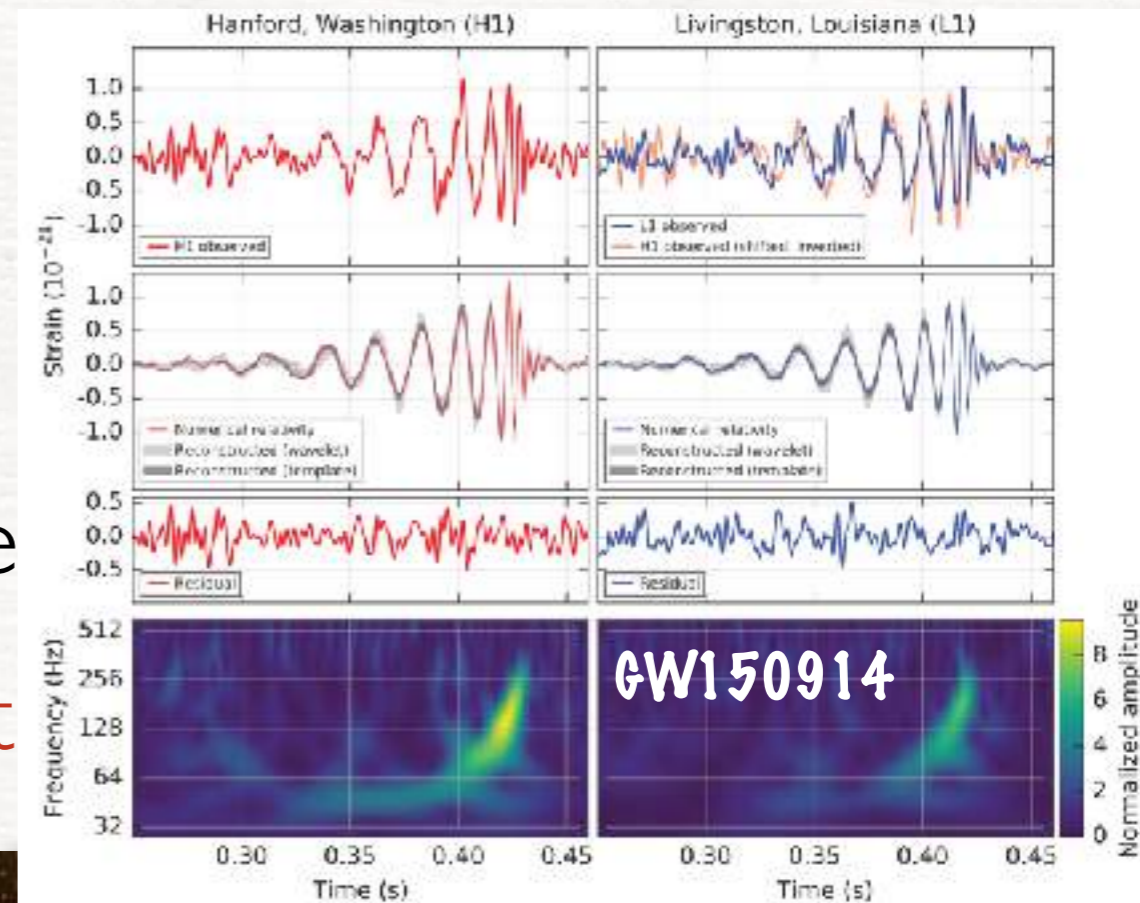
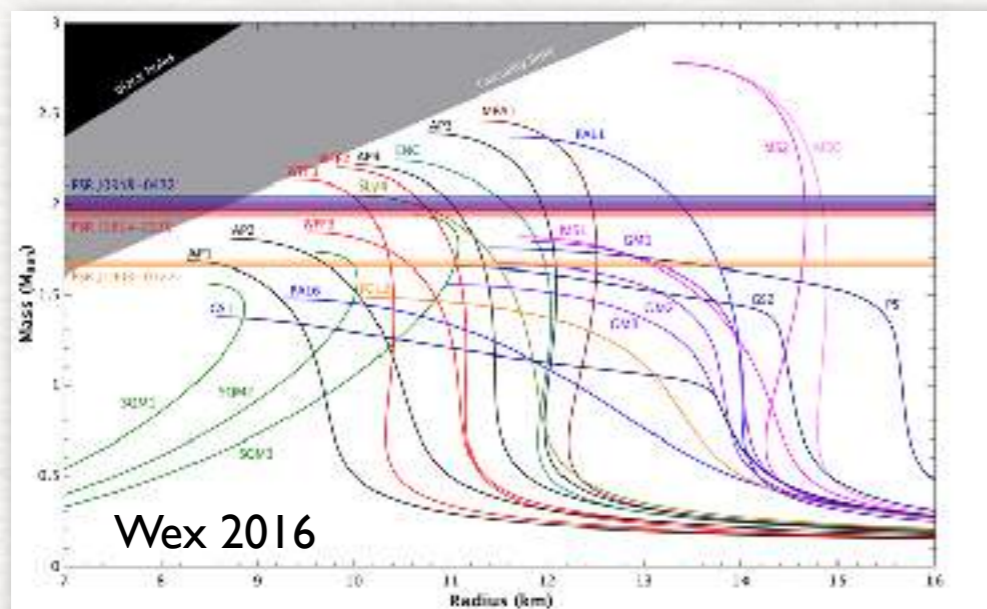
- For BHs we know what to **expect**:

$$\text{BH} + \text{BH} \longrightarrow \text{BH} + \text{GWs}$$

- For NSs the question is more **subtle**: hyper-massive neutron star (HMNS), ie

$$\text{NS} + \text{NS} \longrightarrow \text{HMNS} + \dots ? \longrightarrow \text{BH} + \text{t}$$

- **HMNS** phase can provide clear information on **EOS**



- **BH+torus** system may tell us on the central engine of **GRBs**

# The two-body problem in GR

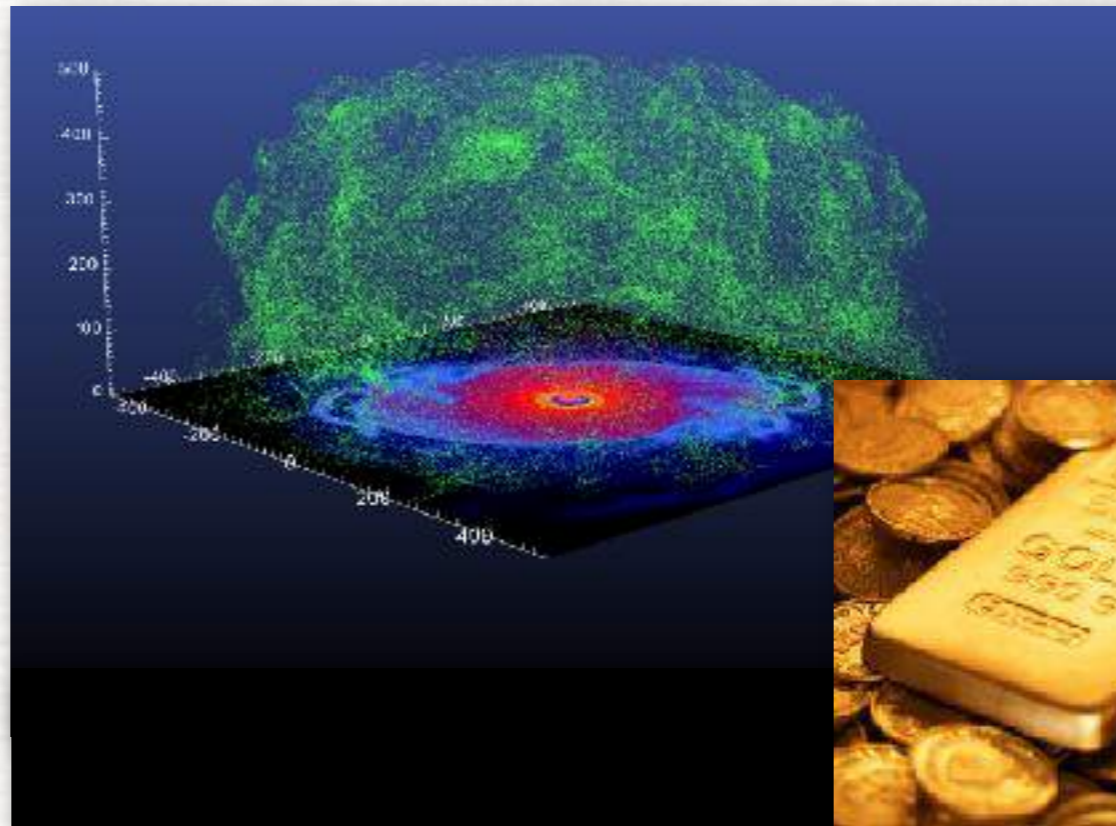
- For BHs we know what to **expect**:



- For NSs the question is more **subtle**: the merger leads to an hyper-massive neutron star (HMNS), ie a metastable equilibrium:



- **ejected matter** undergoes nucleosynthesis of heavy elements



# The equations of numerical relativity

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu}, \quad (\text{field equations})$$

$$\nabla_{\mu}T^{\mu\nu} = 0, \quad (\text{cons. energy/momentum})$$

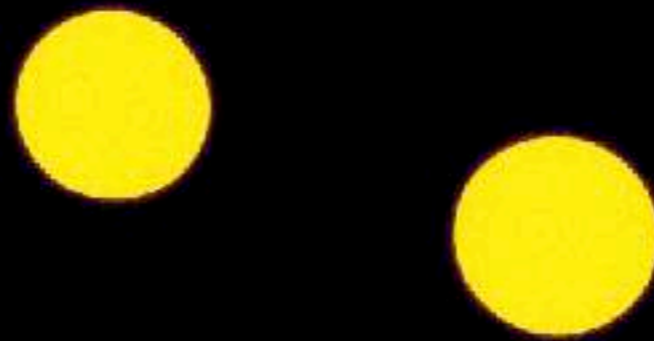
$$\nabla_{\mu}(\rho u^{\mu}) = 0, \quad (\text{cons. rest mass})$$

$$p = p(\rho, \epsilon, Y_e, \dots), \quad (\text{equation of state})$$

$$\nabla_{\nu}F^{\mu\nu} = I^{\mu}, \quad \nabla_{\nu}^*F^{\mu\nu} = 0, \quad (\text{Maxwell equations})$$

$$T_{\mu\nu} = T_{\mu\nu}^{\text{fluid}} + T_{\mu\nu}^{\text{EM}} + \dots \quad (\text{energy - momentum tensor})$$

In GR these equations do not possess an analytic solution in the regimes we are interested in



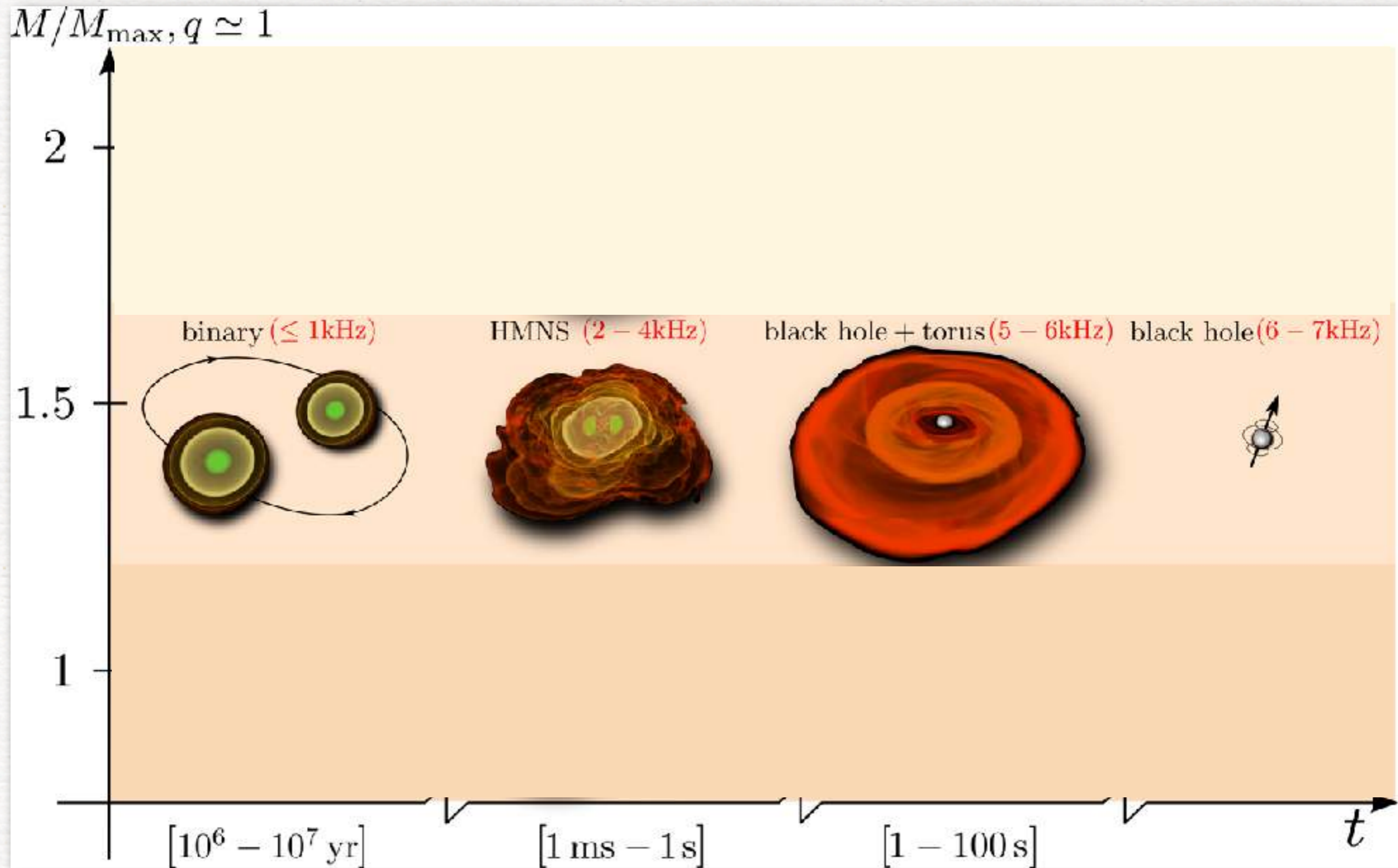
merger → HMNS → BH + torus

Quantitative differences are produced by:

- **total mass** (prompt vs delayed collapse)



# Broadbrush picture



merger → HMNS → BH + torus

Quantitative differences are produced by:

- total **mass** (prompt vs delayed collapse)
- mass **asymmetries** (HMNS and torus)



Total mass :  $3.37 M_{\odot}$ ; mass ratio :0.80;



- \* the torii are generically **more massive**
- \* the torii are generically **more extended**
- \* the torii tend to stable **quasi-Keplerian** configurations
- \* overall unequal-mass systems have all the ingredients needed to create a GRB



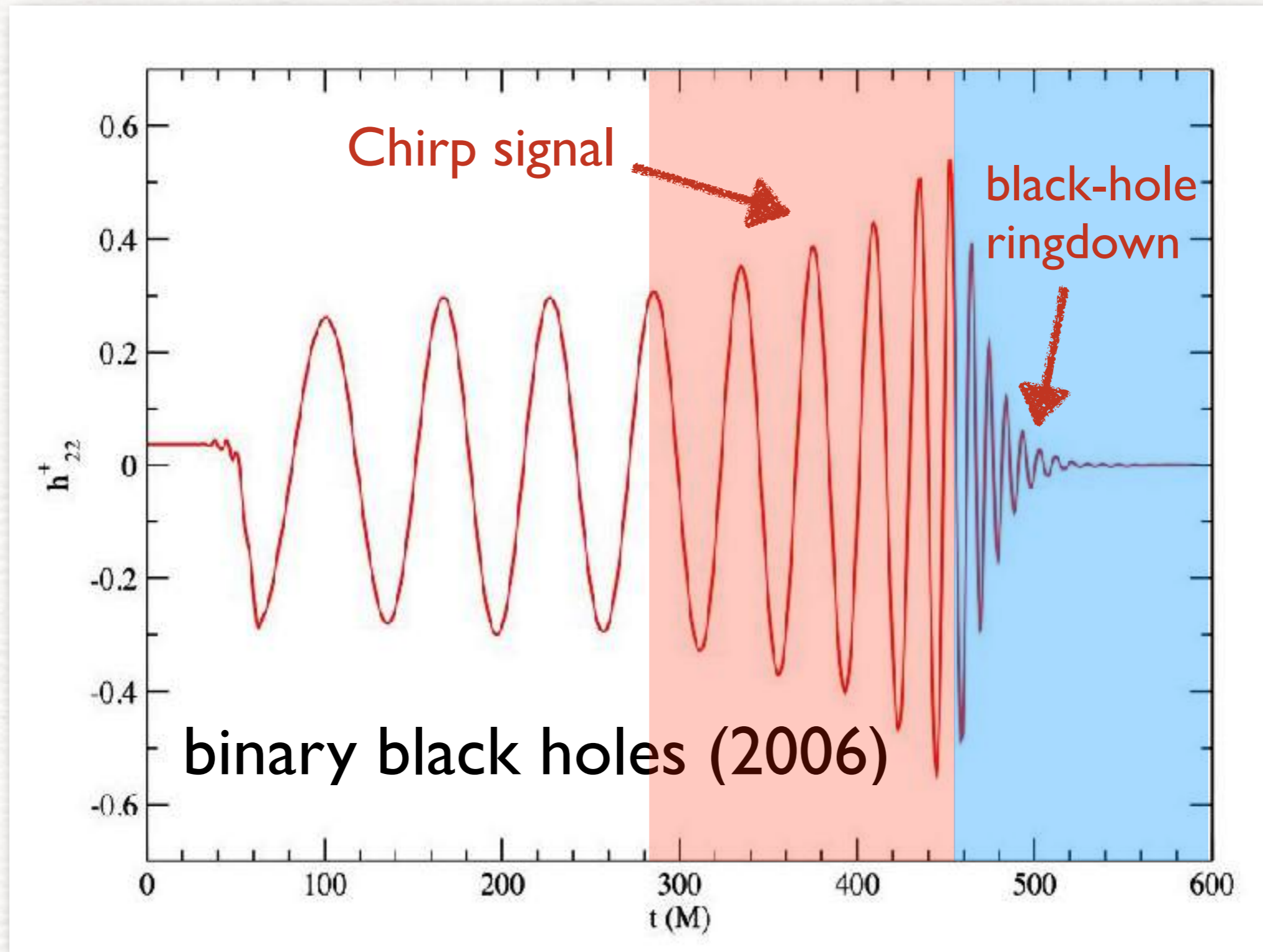
merger → HMNS → BH + torus

Quantitative differences are produced by:

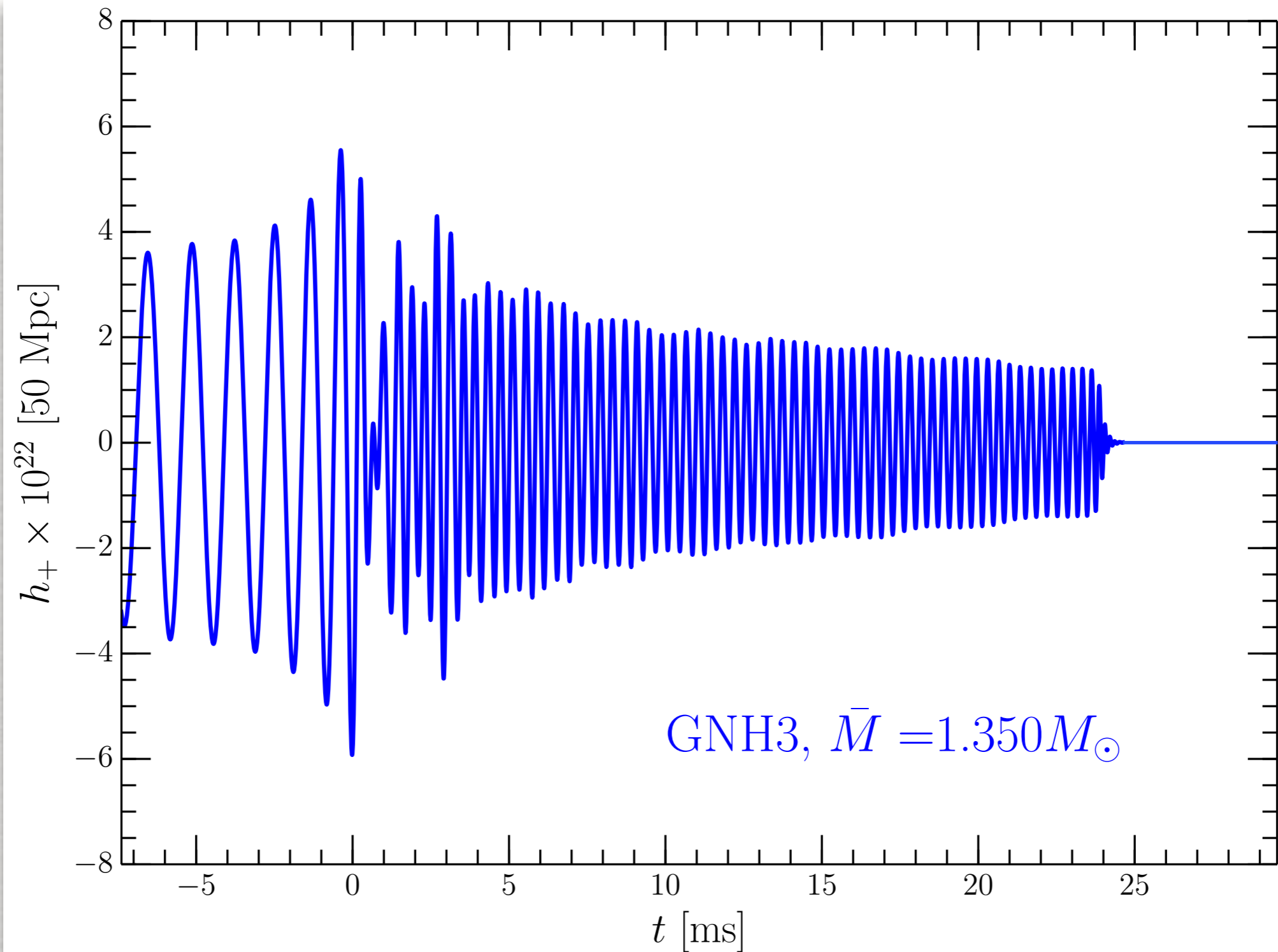
- total **mass** (prompt vs delayed collapse)
- mass **asymmetries** (HMNS and torus)
- soft/stiff **EOS** (inspiral and post-merger)
- **magnetic fields** (equil. and EM emission)
- **radiative** losses (equil. and nucleosynthesis)



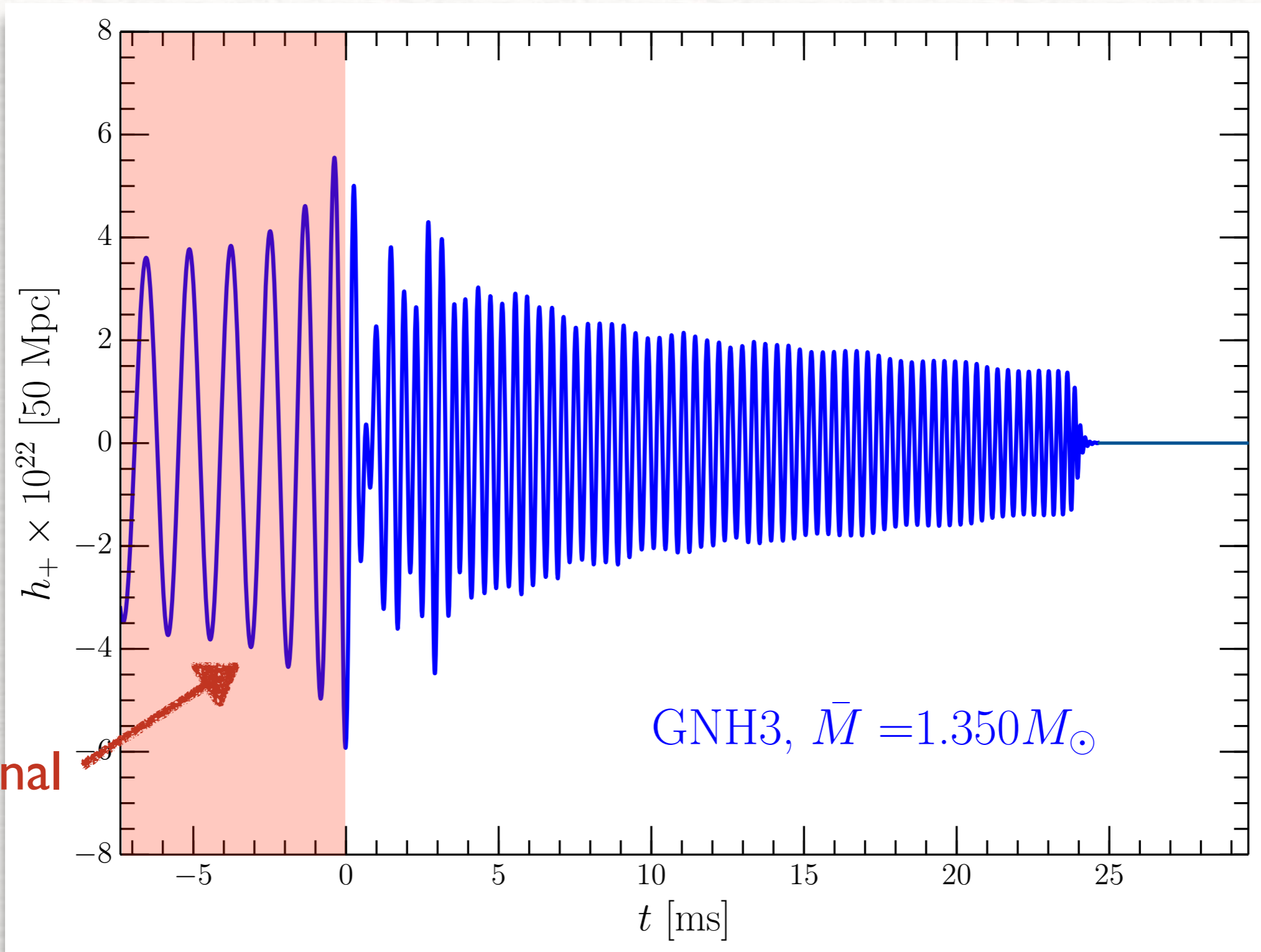
# Anatomy of the GW signal



# Anatomy of the GW signal



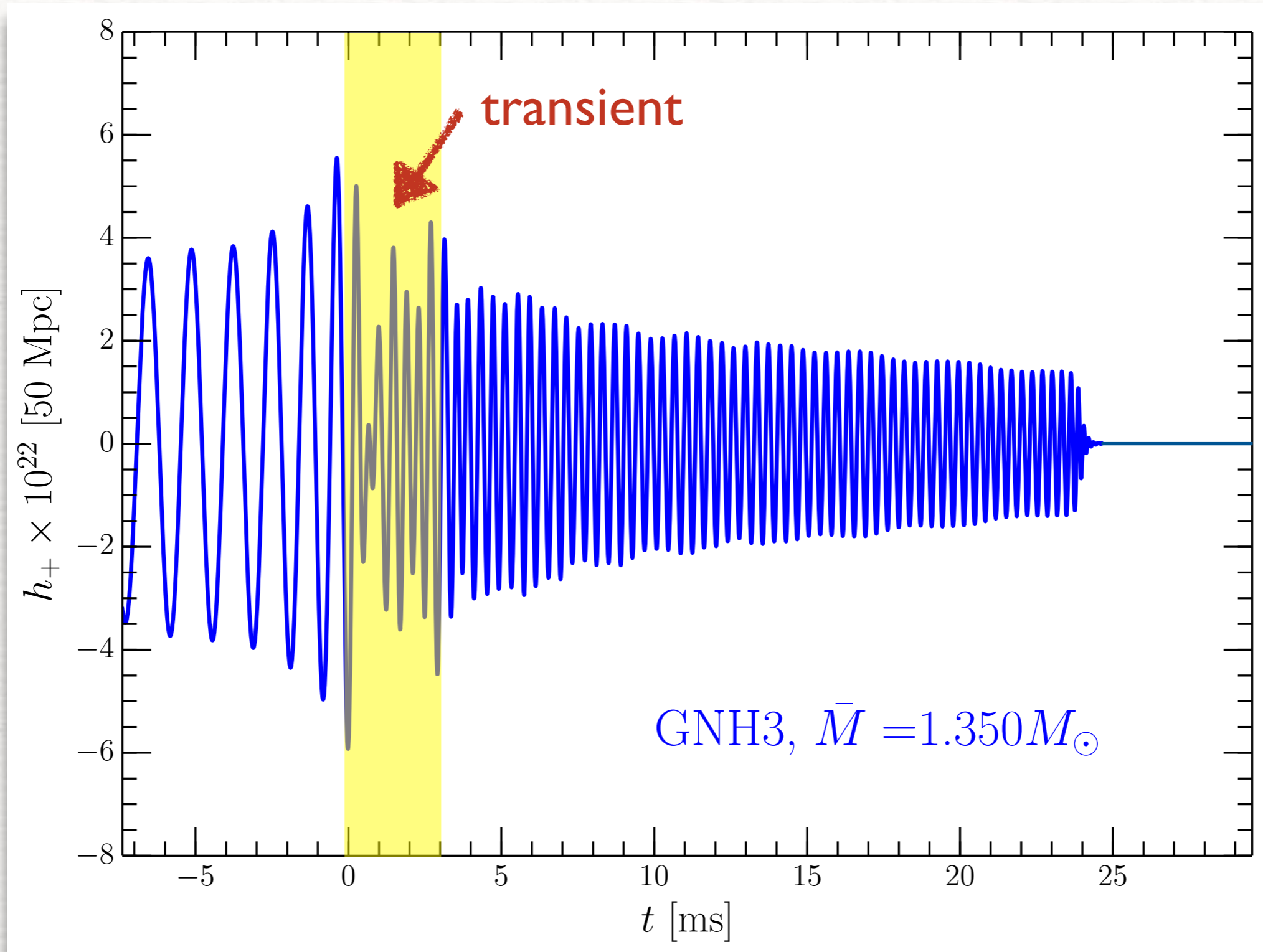
# Anatomy of the GW signal



**Inspiral:** well approximated by PN/EOB; tidal effects important

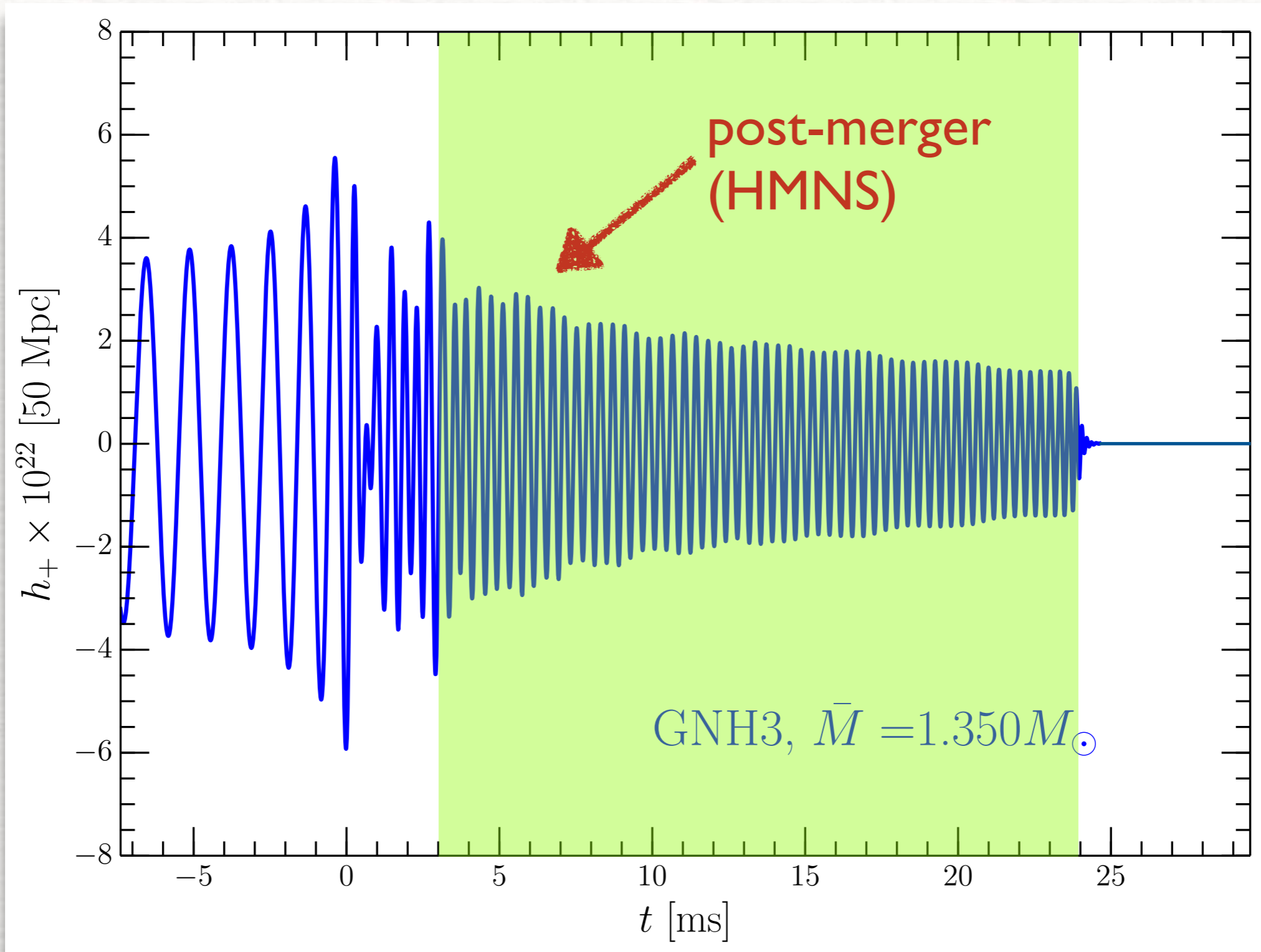


# Anatomy of the GW signal



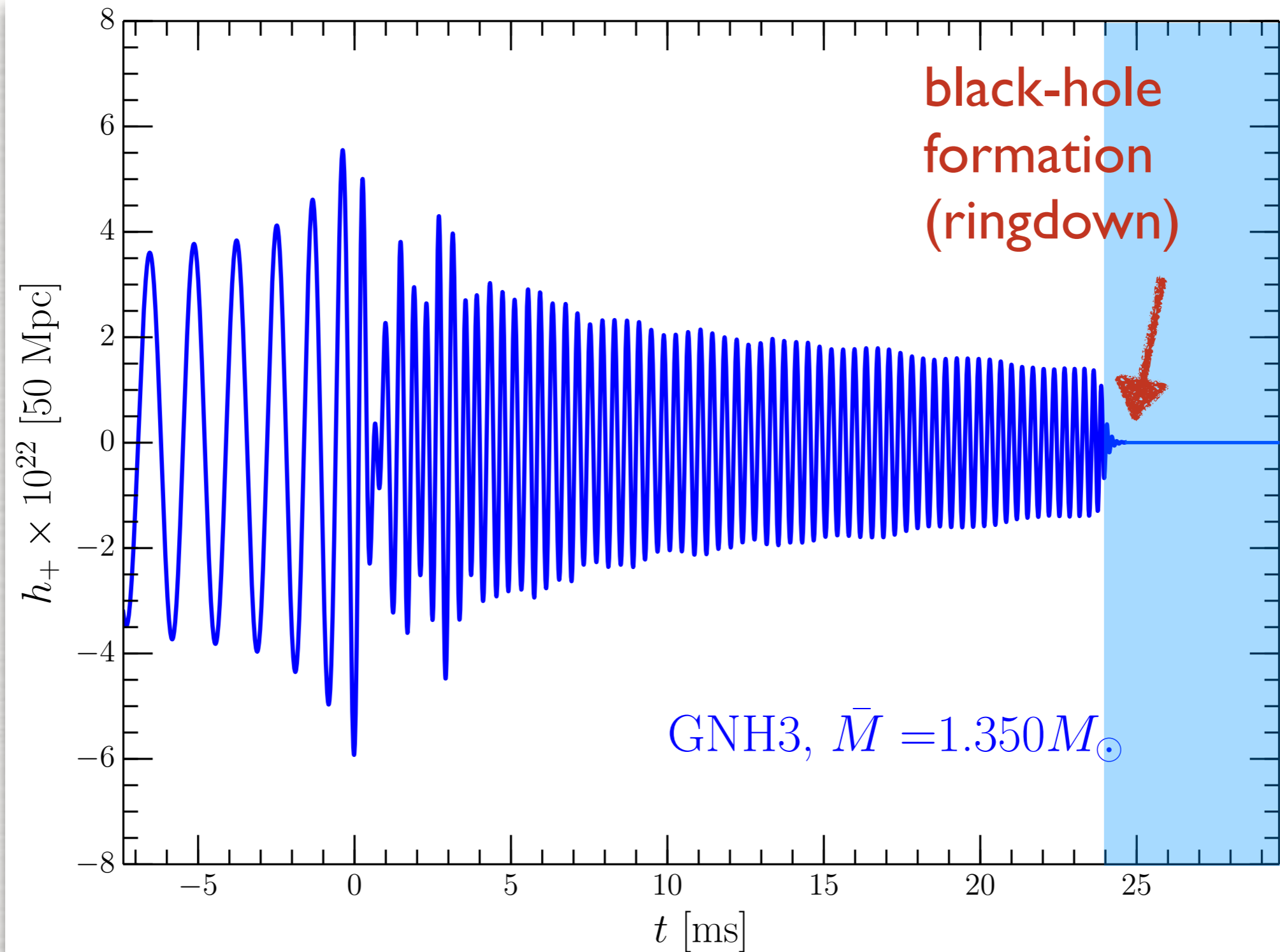
**Merger:** highly nonlinear but analytic description possible

# Anatomy of the GW signal



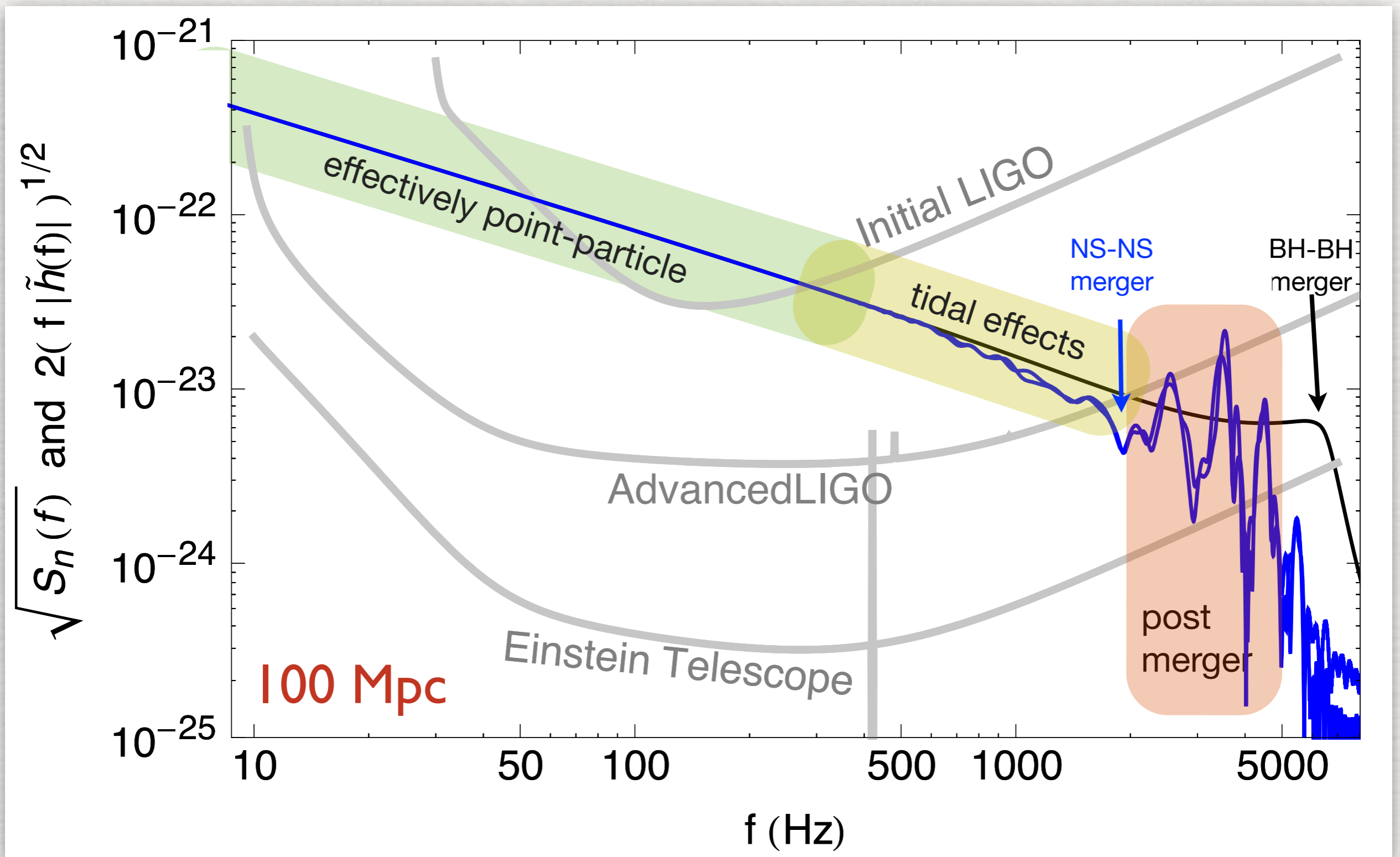
**post-merger:** quasi-periodic emission of bar-deformed HMNS

# Anatomy of the GW signal



**Collapse-ringdown:** signal essentially shuts off.

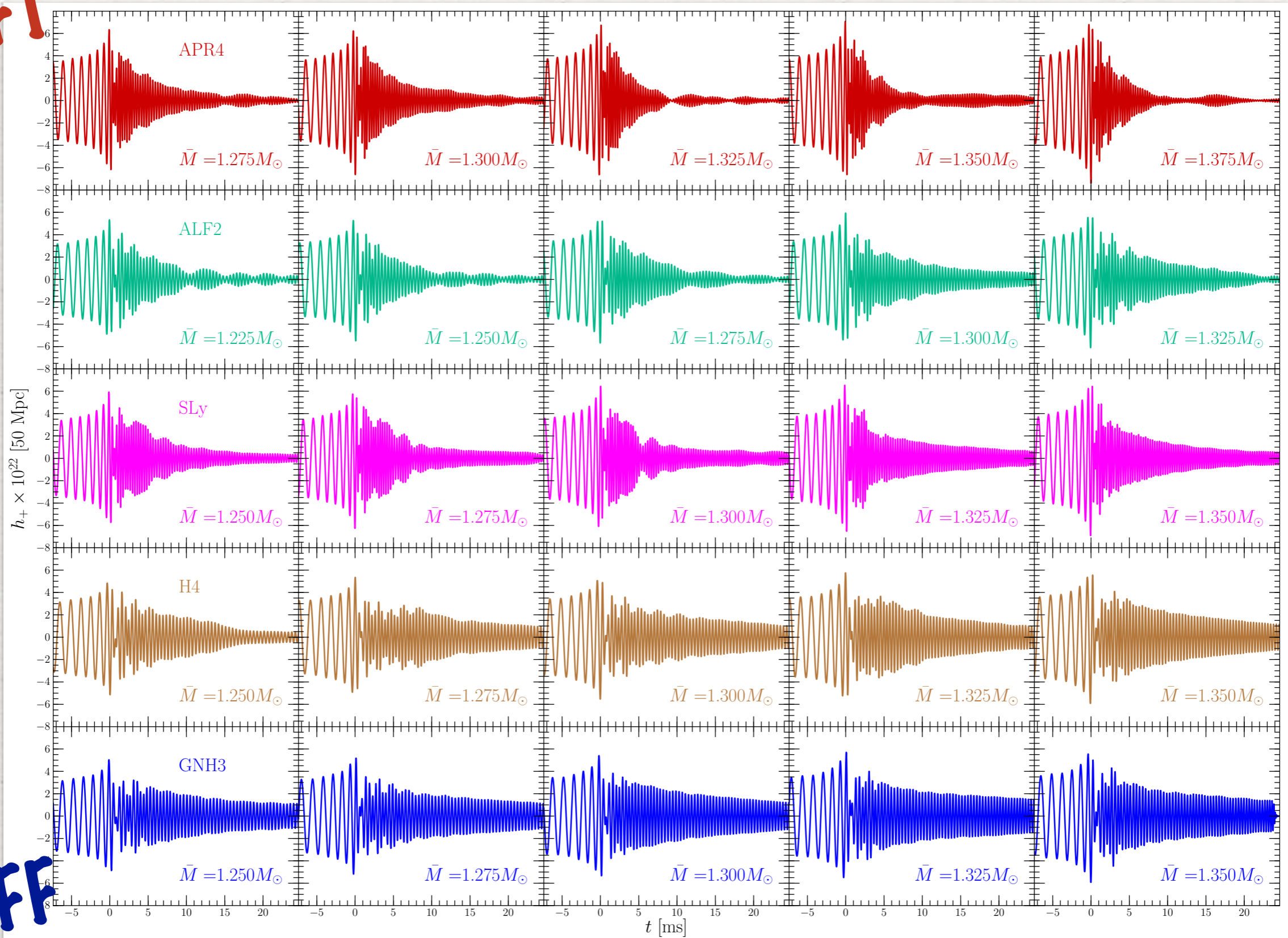
# In frequency space



# What we can do nowadays

Takami, LR, Baiotti (2014, 2015), LR+ (2016)

SOFT

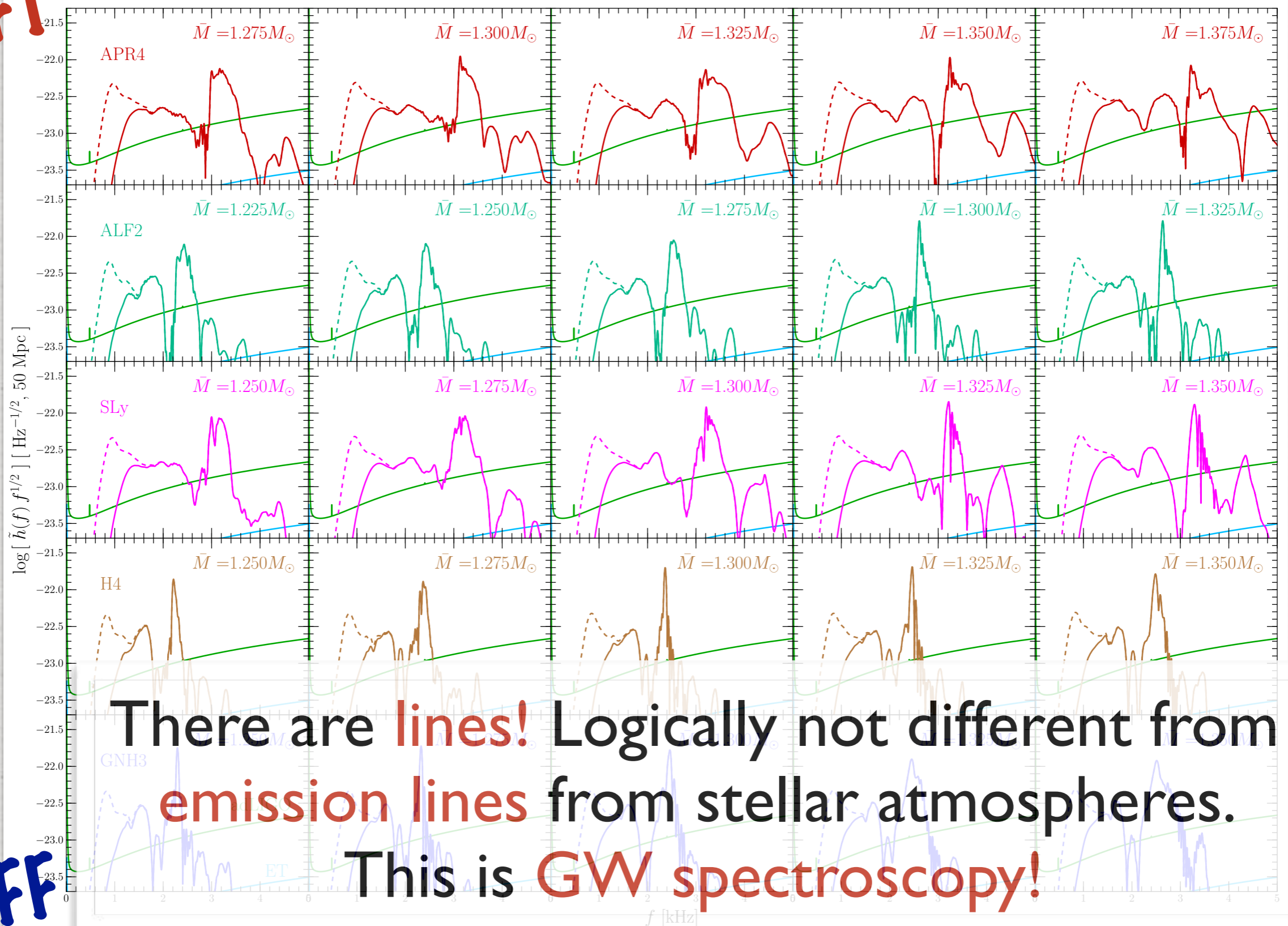


STIFF

# Extracting information from the EOS

Takami, LR, Baiotti (2014, 2015), LR+ (2016)

SOFT



There are **lines!** Logically not different from **emission lines** from stellar atmospheres.

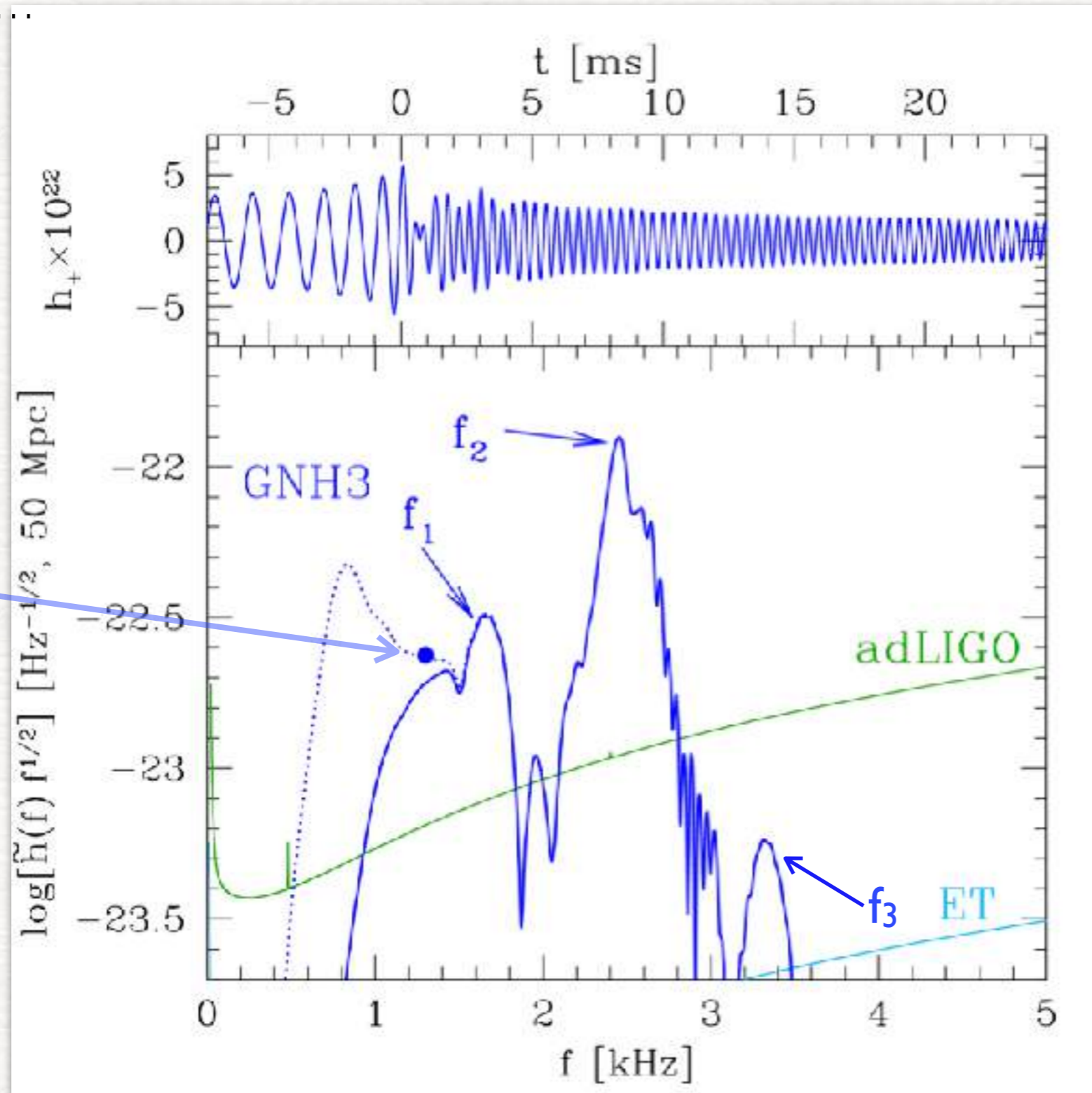
This is **GW spectroscopy!**

STIFF

# A new approach to constrain the EOS

Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, Clark+ 2016, LR+2016, de Pietri+ 2016, Feo+ 2017, Bose+ 2017 ...

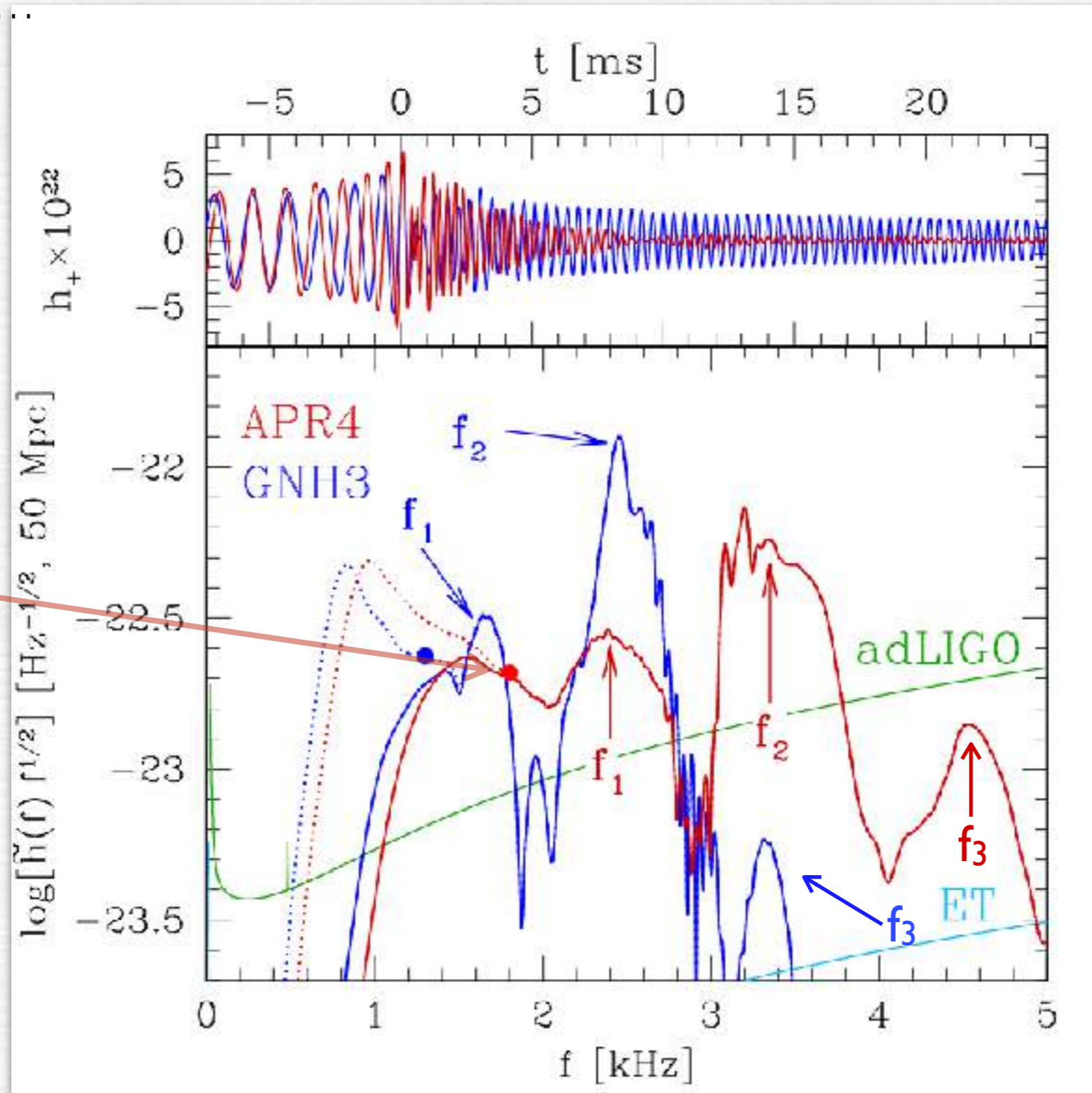
merger  
frequency



# A spectroscopic approach to the EOS

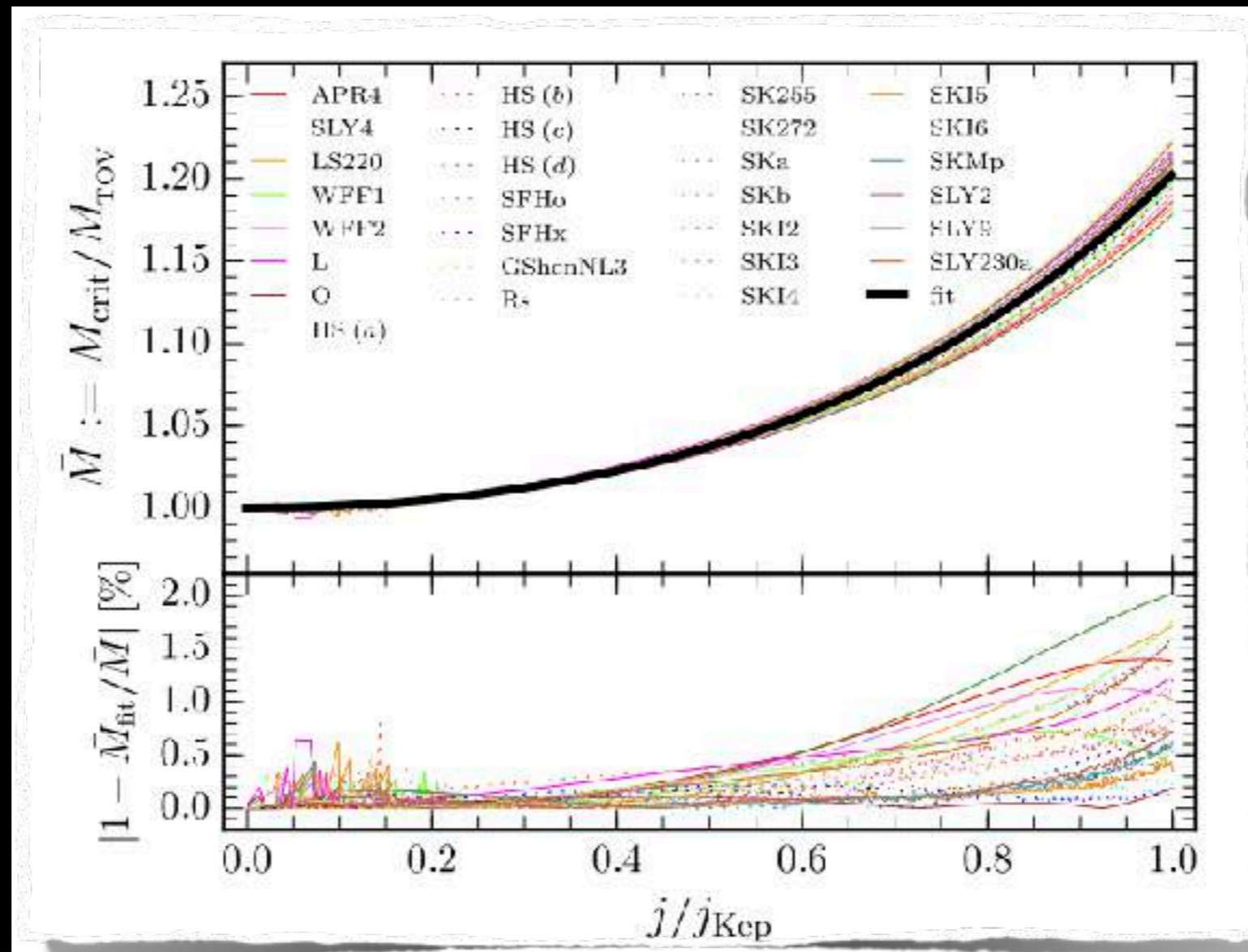
Oechslin+2007, Baiotti+2008, Bauswein+ 2011, 2012, Stergioulas+ 2011, Hotokezaka+ 2013, Takami 2014, 2015, Bernuzzi 2014, 2015, Bauswein+ 2015, Clark+ 2016, LR+2016, de Pietri+ 2016, Feo+ 2017, Bose+ 2017 ...

merger  
frequency

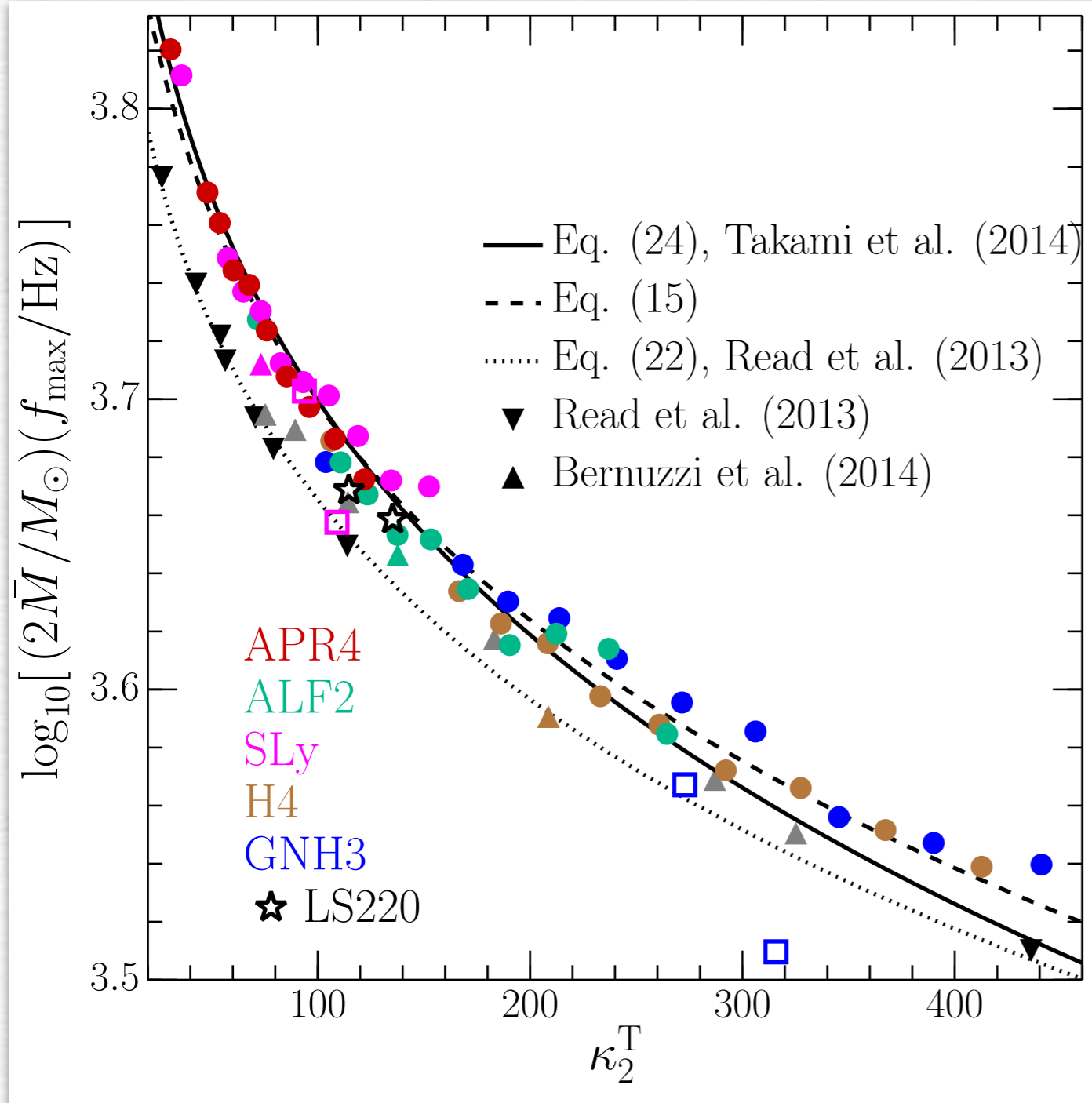




# Quasi-universal behaviour



# Quasi-universal behaviour: **inspiral**



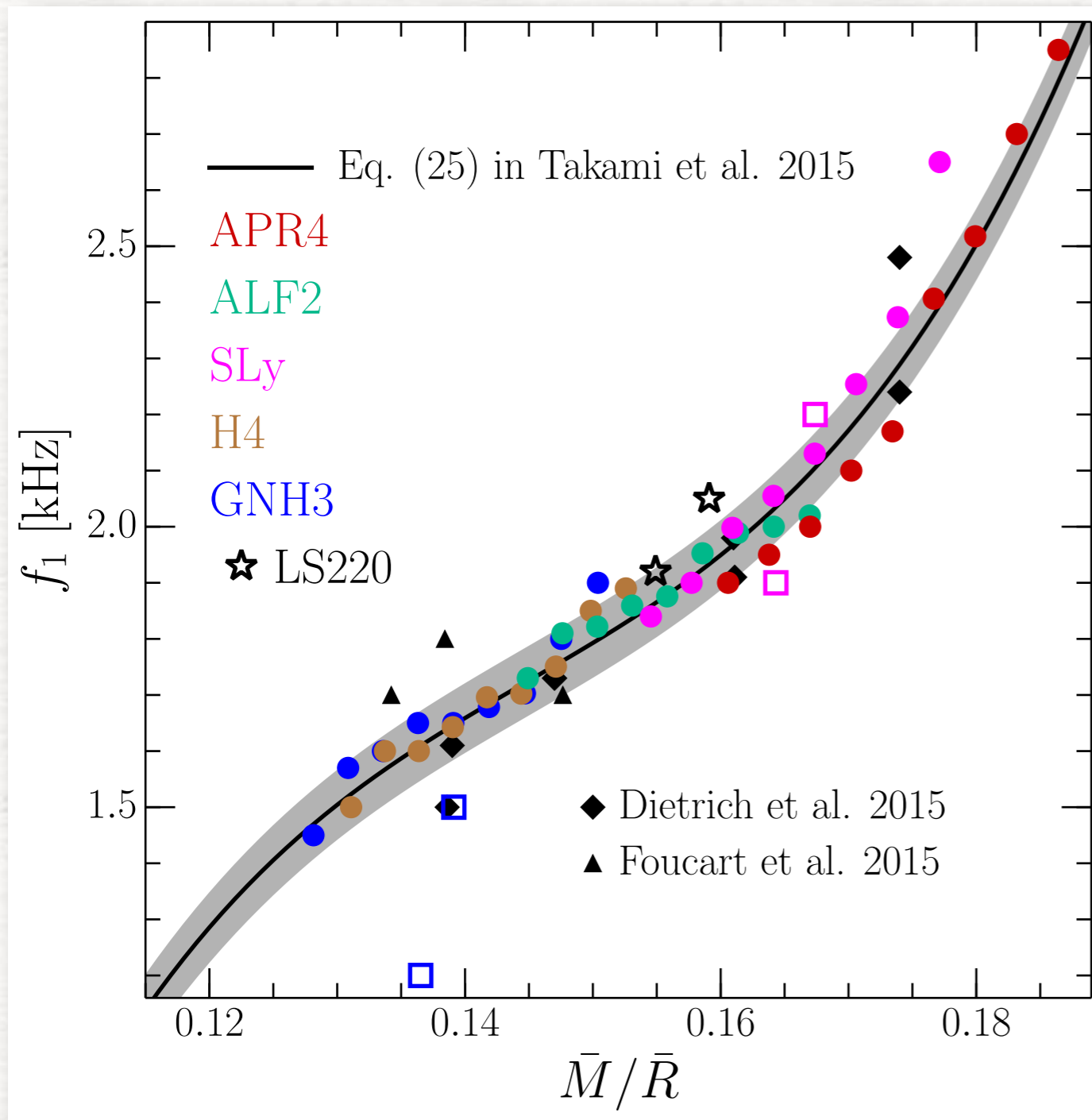
“surprising” result: **quasi-universal** behaviour of GW frequency at amplitude peak (Read+2013)

Many other simulations have confirmed this (Bernuzzi+ 2014, Takami+ 2015, LR+2016).

**Quasi-universal** behaviour in the **inspiral** implies that once  **$f_{\max}$**  is measured, so is tidal deformability, hence  $I, Q, M/R$

$$\Lambda = \frac{\lambda}{\bar{M}^5} = \frac{16}{3} \kappa_2^T \quad \text{tidal deformability or Love number}$$

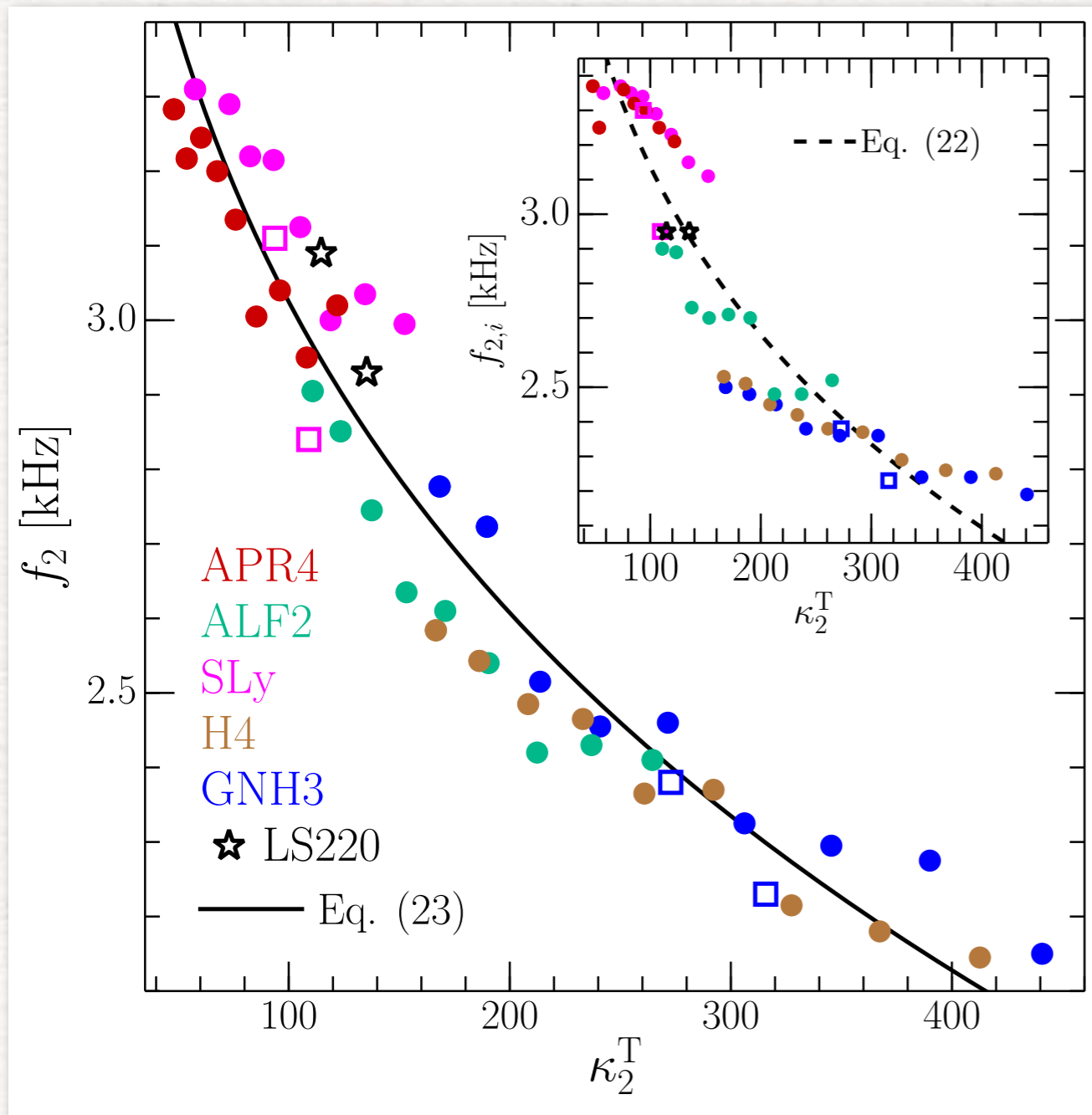
# Quasi-universal behaviour: post-merger



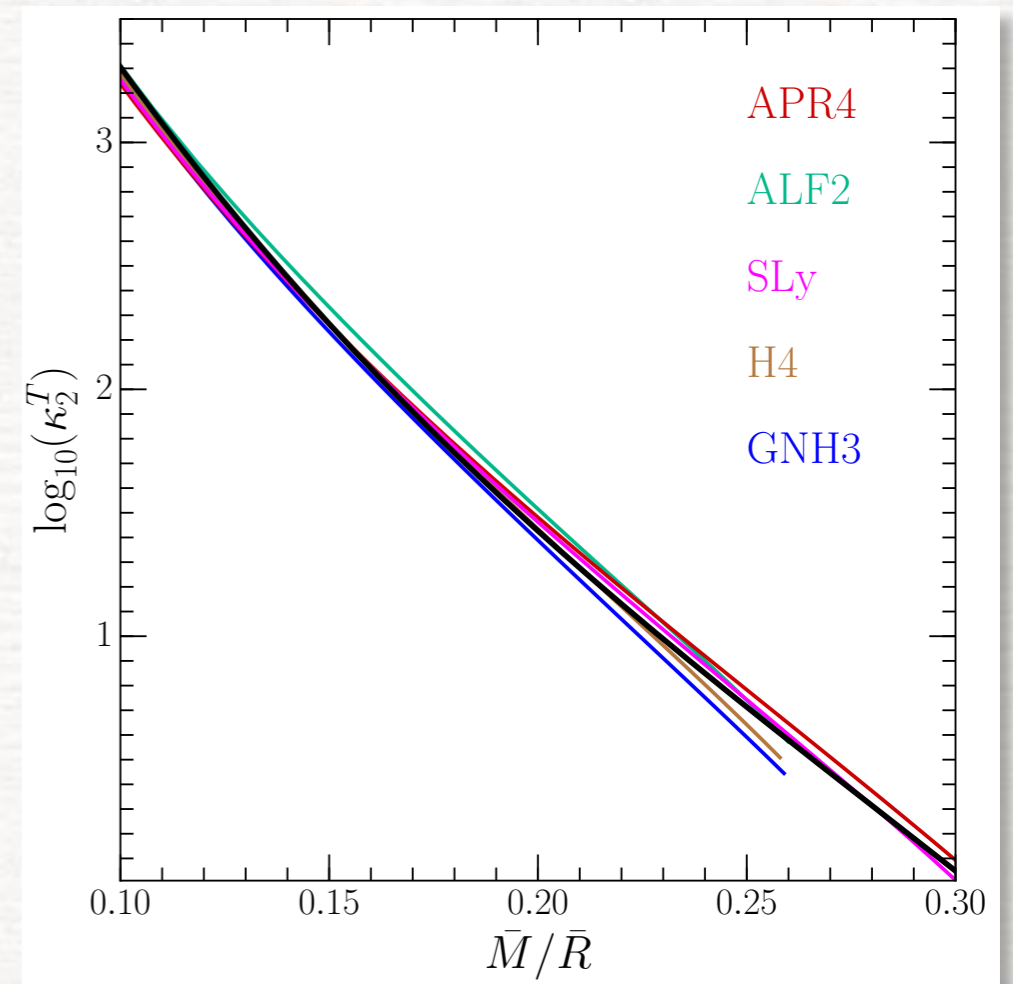
We have found **quasi-universal behaviour**: i.e., the properties of the spectra are only weakly dependent on the EOS.

This has profound implications for the analytical modelling of the GW emission: “what we do for one EOS can be extended to all EOSs.”

# Quasi-universal behaviour: post-merger



- Correlations with Love number found also for high frequency peak  $f_2$ .
- This and other correlations are **weaker** but equally useful.

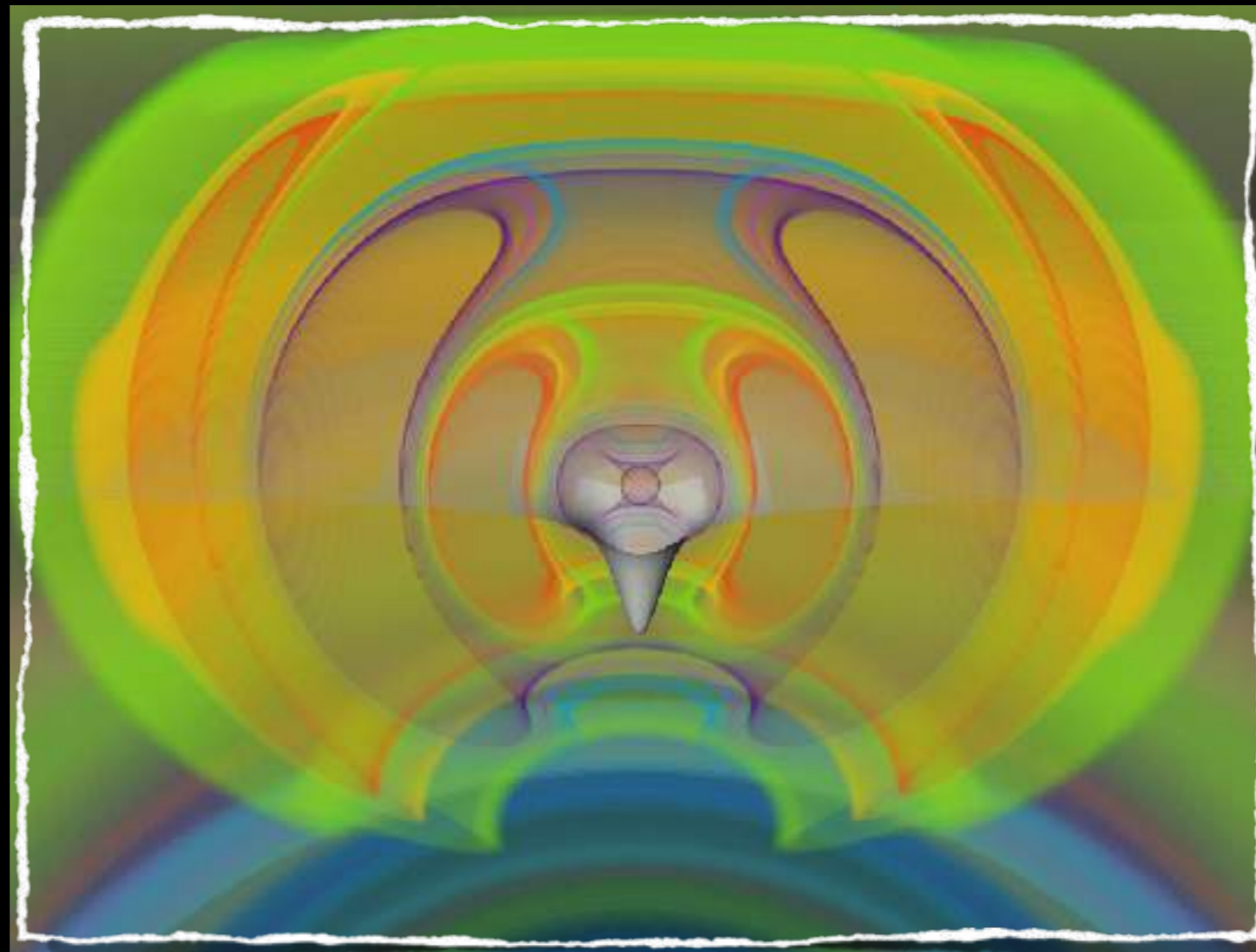


- Important correlation also between **compactness** and **deformability**

# GW170817, maximum mass, radii and tidal deformabilities

LR, Most, Weih (2018)

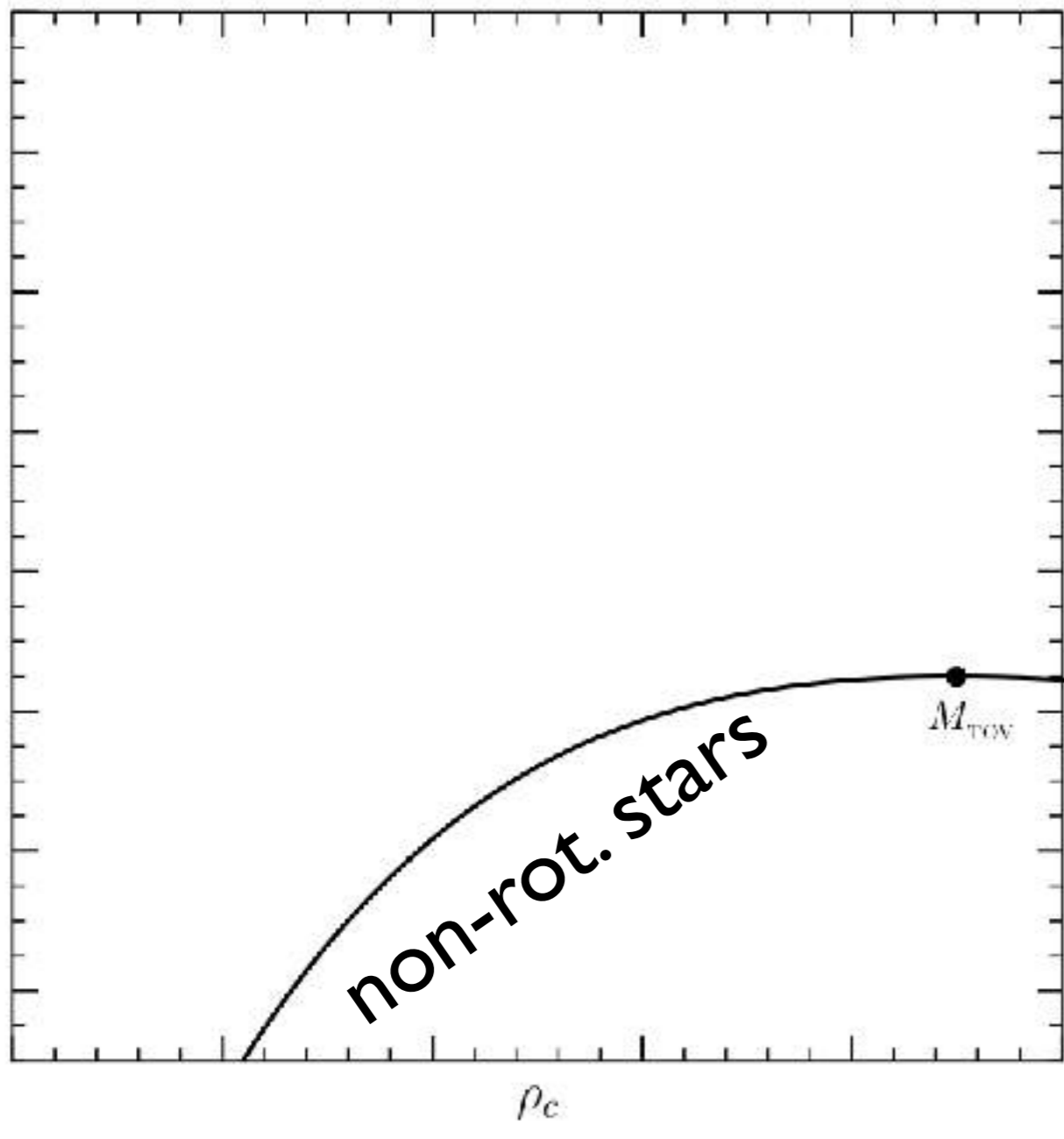
Most, Weih, LR, Schaffner-Bielich (2018)



# The outcome of GW170817

- The remnant of GW170817 was a hypermassive star, i.e. a differentially rotating object with initial **gravitational** mass

$$M_1 + M_2 = 2.74_{-0.01}^{+0.04} M_{\odot}$$

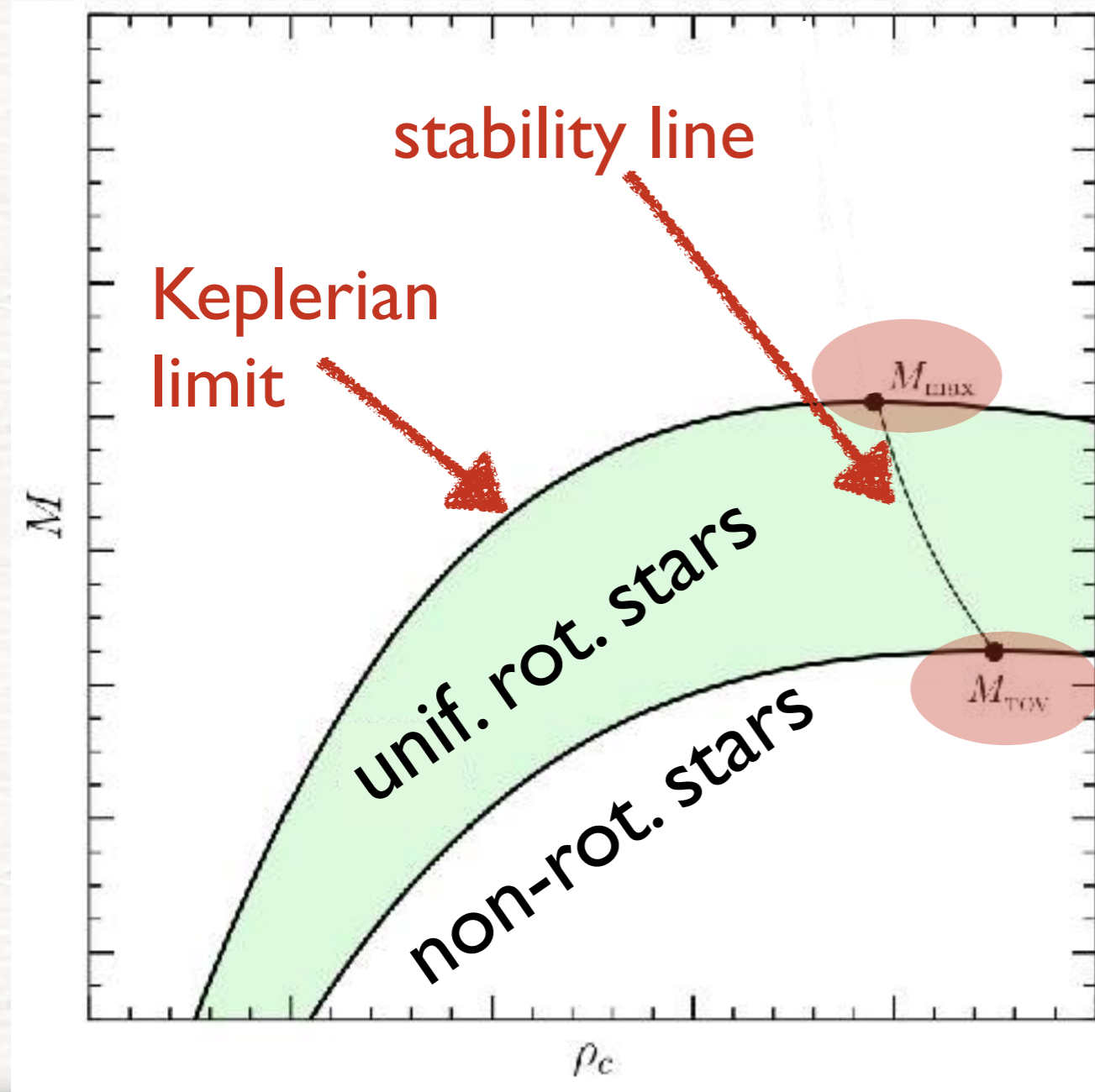


- Sequences of equilibrium models of **nonrotating** stars will have a maximum mass:  $M_{\text{TOV}}$

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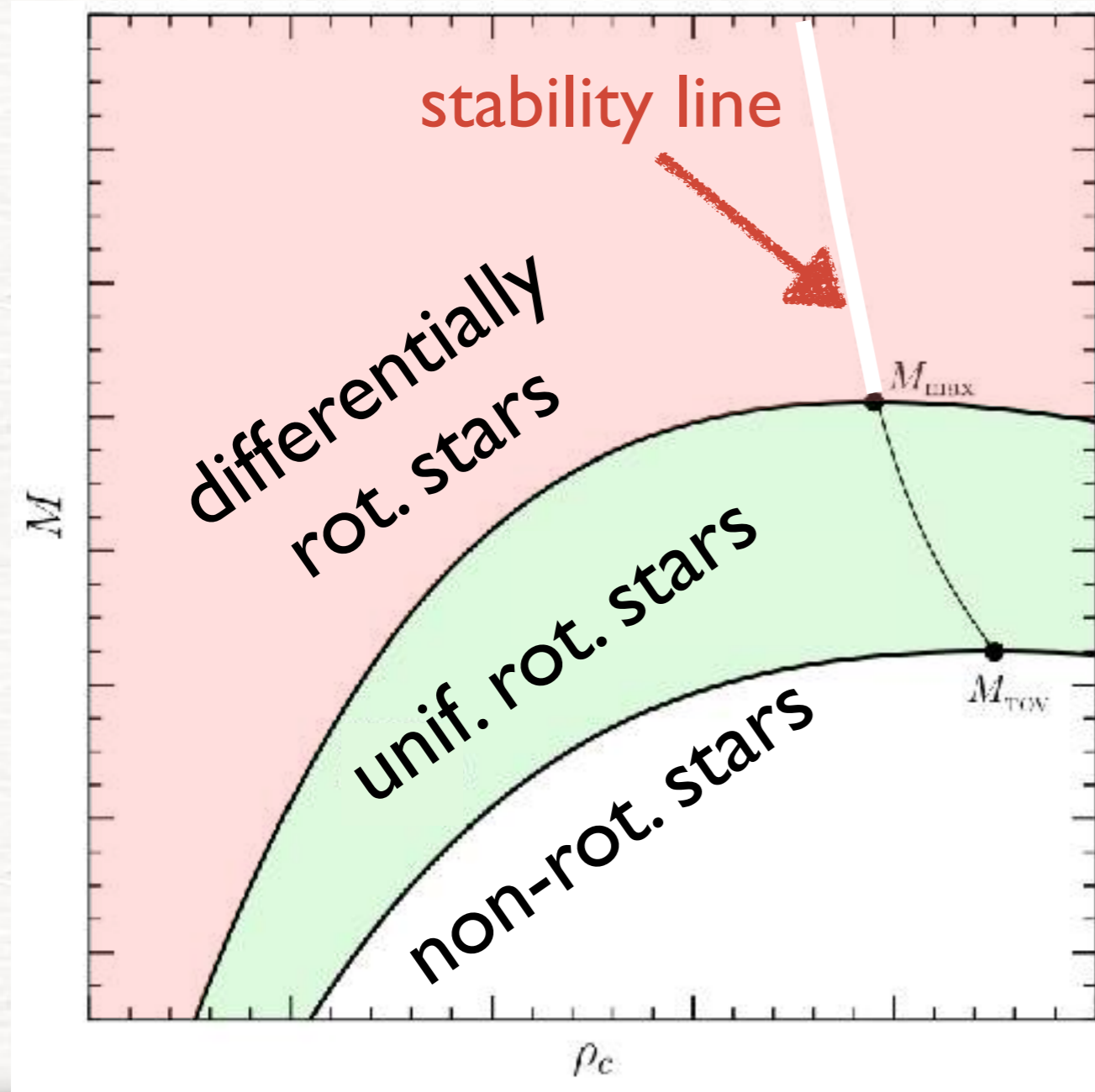
- Sequences of equilibrium models of **nonrotating** stars will have a maximum mass:  $M_{TOV}$
- This is true also for **uniformly** rotating stars at mass shedding limit:  $M_{max}$
- $M_{max}$  simple and **quasi-universal** function of  $M_{TOV}$  (Breu & LR 2016)

$$M_{max} = (1.20_{-0.05}^{+0.02}) M_{TOV}$$

# The outcome of GW170817

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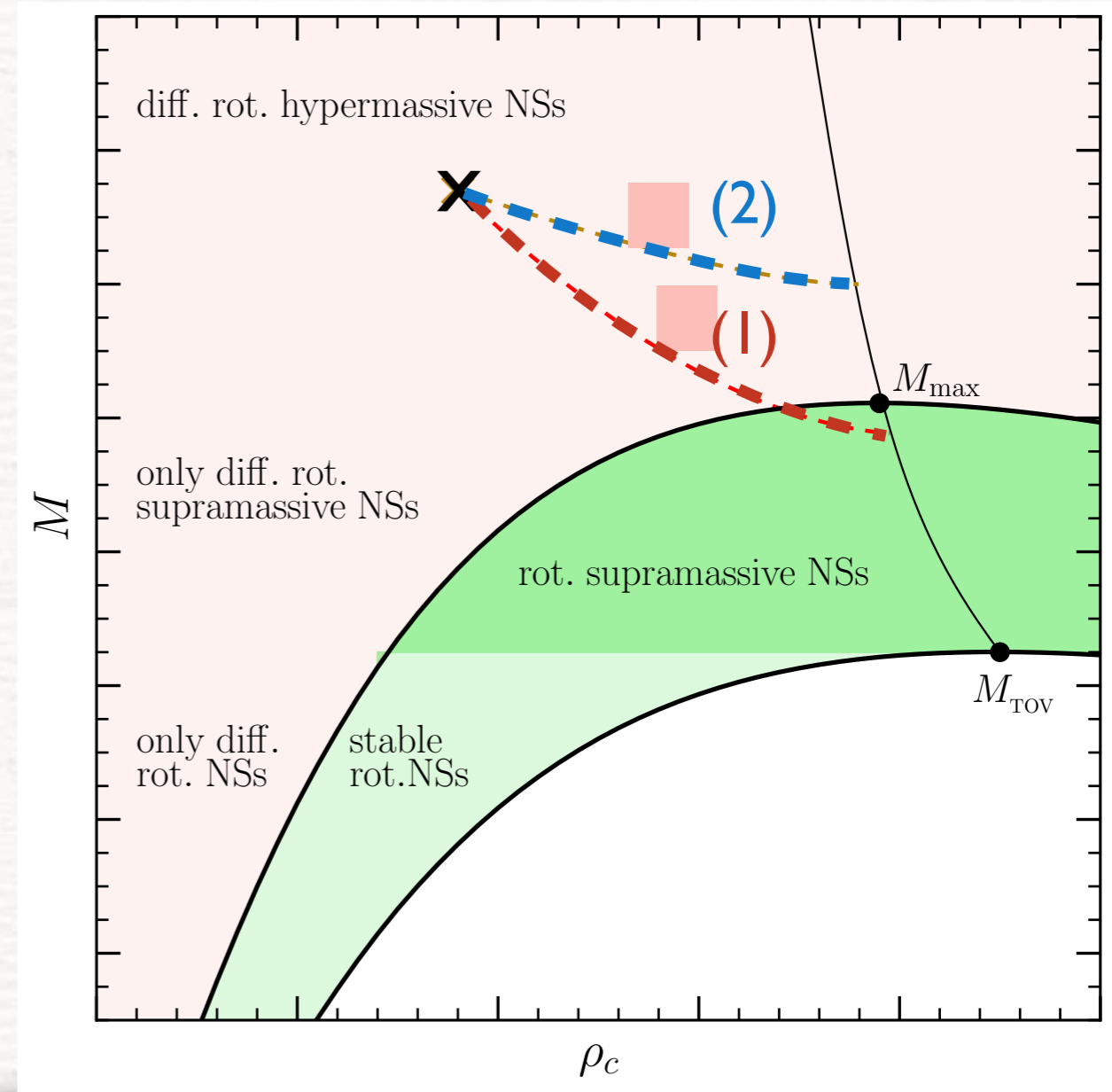


- Green** region is for **uniformly** rotating equilibrium models.
- Salmon** region is for **differentially** rotating equilibrium models.
- Stability line is simply extended (Weih+18)



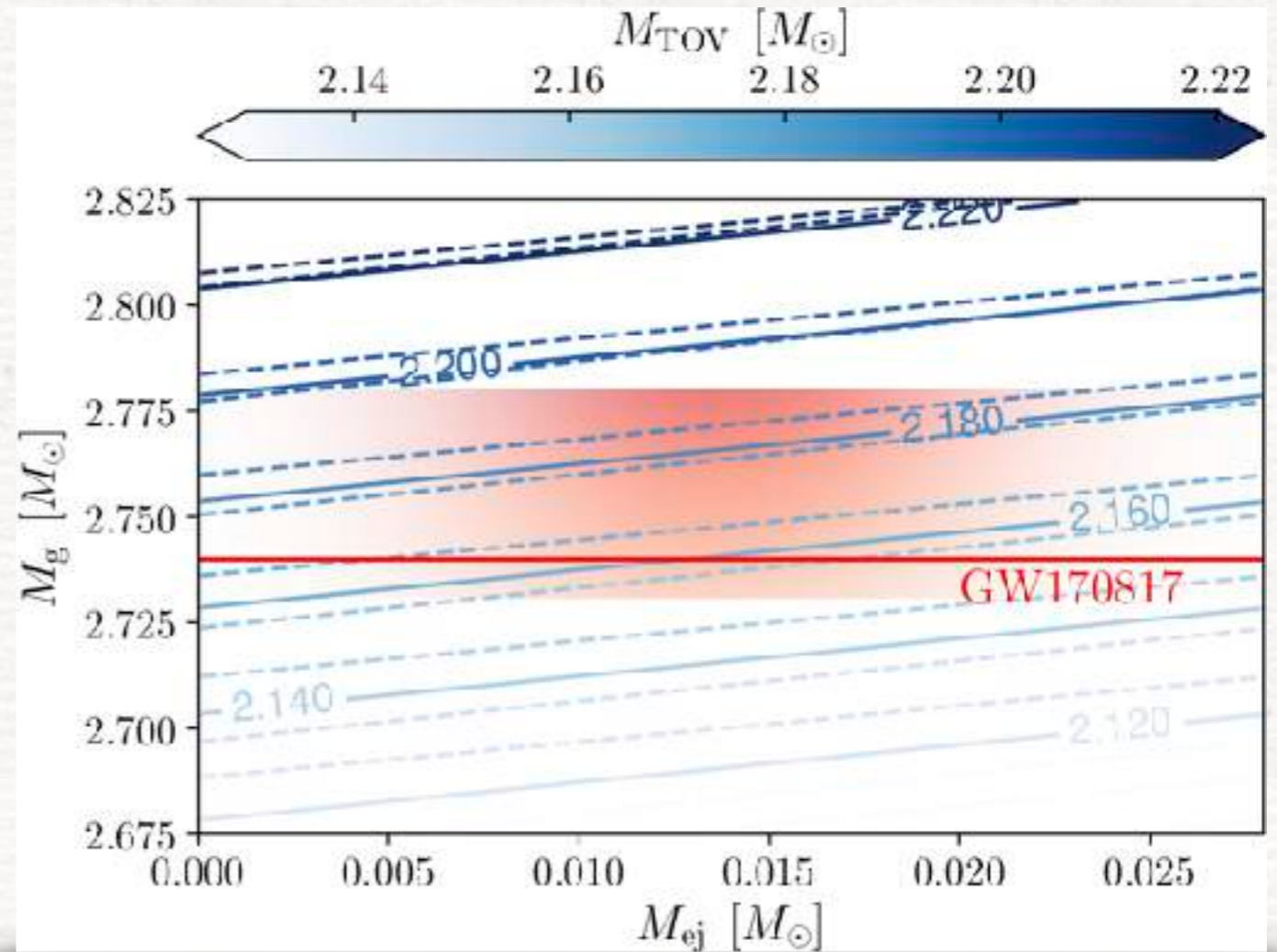
# The outcome of GW170817

- GW170817 produced object as "x"; GRB implies a BH has been formed: "x" followed two possible tracks: **fast (2)** and **slow (1)**
- It rapidly produced a BH when still **differentially** rotating **(2)**
- It lost differential rotation leading to a **uniformly** rotating core **(1)**.
- **(1)** is much more likely because of large ejected mass (long lived).
- Final mass is near  $M_{\max}$  and we know this is universal!



## let's recap...

- The merger product of GW170817 was initially **differentially** rotating but collapsed as **uniformly** rotating object.
- Use measured **gravitational** mass of GW170817
- Remove **rest mass** deduced from kilonova emission
- Use **universal relations** and account errors to obtain



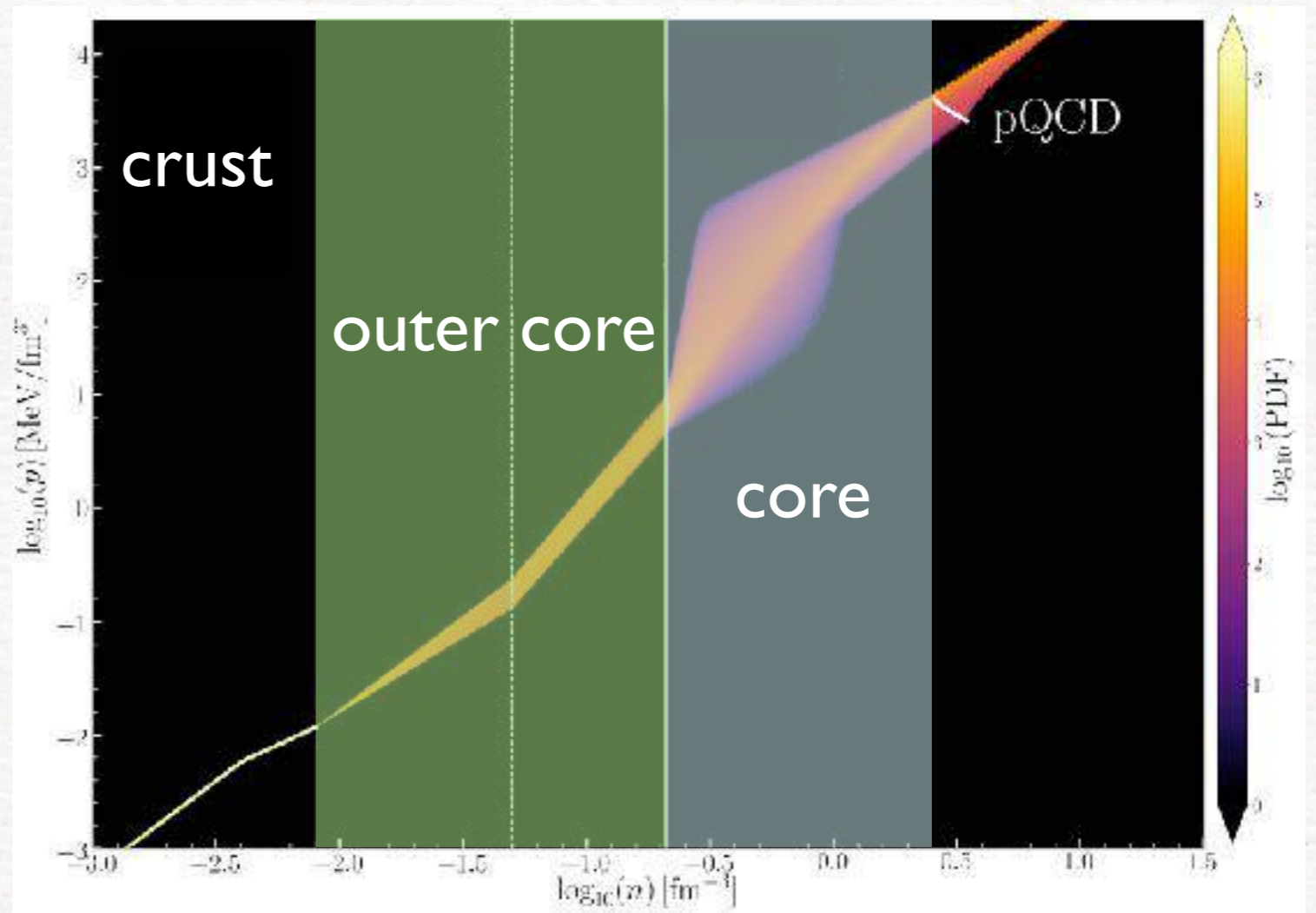
pulsar  
timing

$$2.01^{+0.04}_{-0.04} \leq M_{\text{TOV}}/M_\odot \lesssim 2.16^{+0.17}_{-0.15}$$

universal relations  
and GW170817;  
similar estimates  
by other groups

# Limits on radii and deformabilities

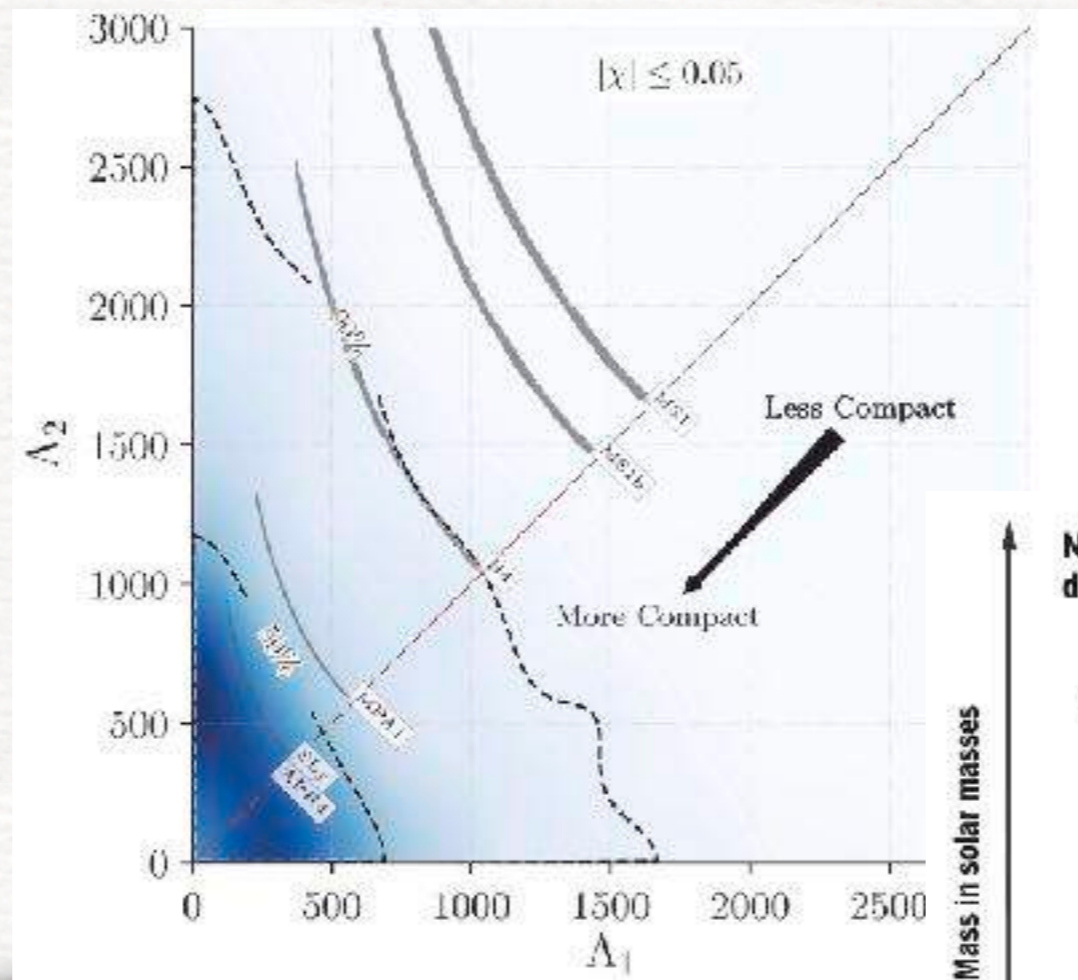
- Constraining NS radii of neutron stars is an effort with thousands of papers published over the last 40 years.
- Question is deeply related with EOS of nuclear matter.
- Can new constraints be set by GW170817?
- Ignorance can be parameterised and EOSs can be built arbitrarily as long as they satisfy specific **constraints** on **low** and **high** densities.



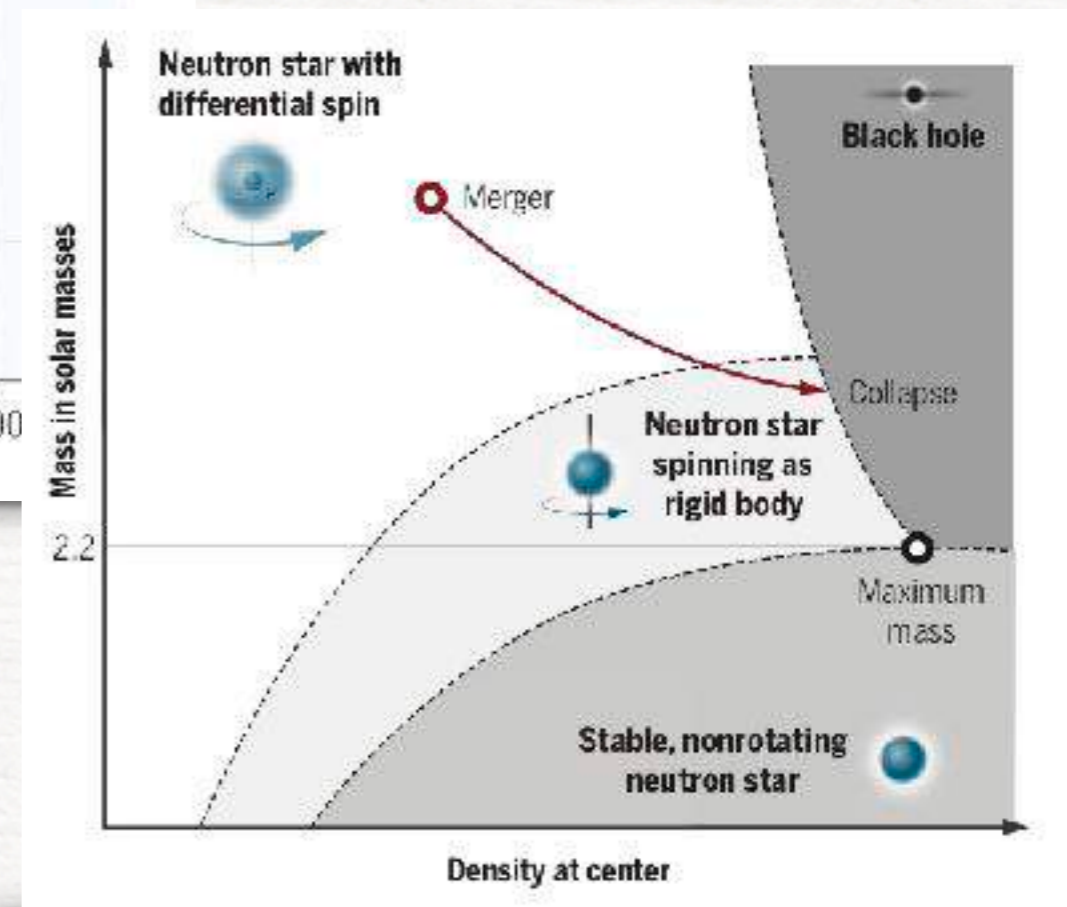
# Limits on radii and deformabilities

- We have produced  $10^6$  EOSs with about  $10^9$  stellar models.

- Can impose differential constraints from the **maximum mass** and from the **tidal deformability** from **GW170817**?



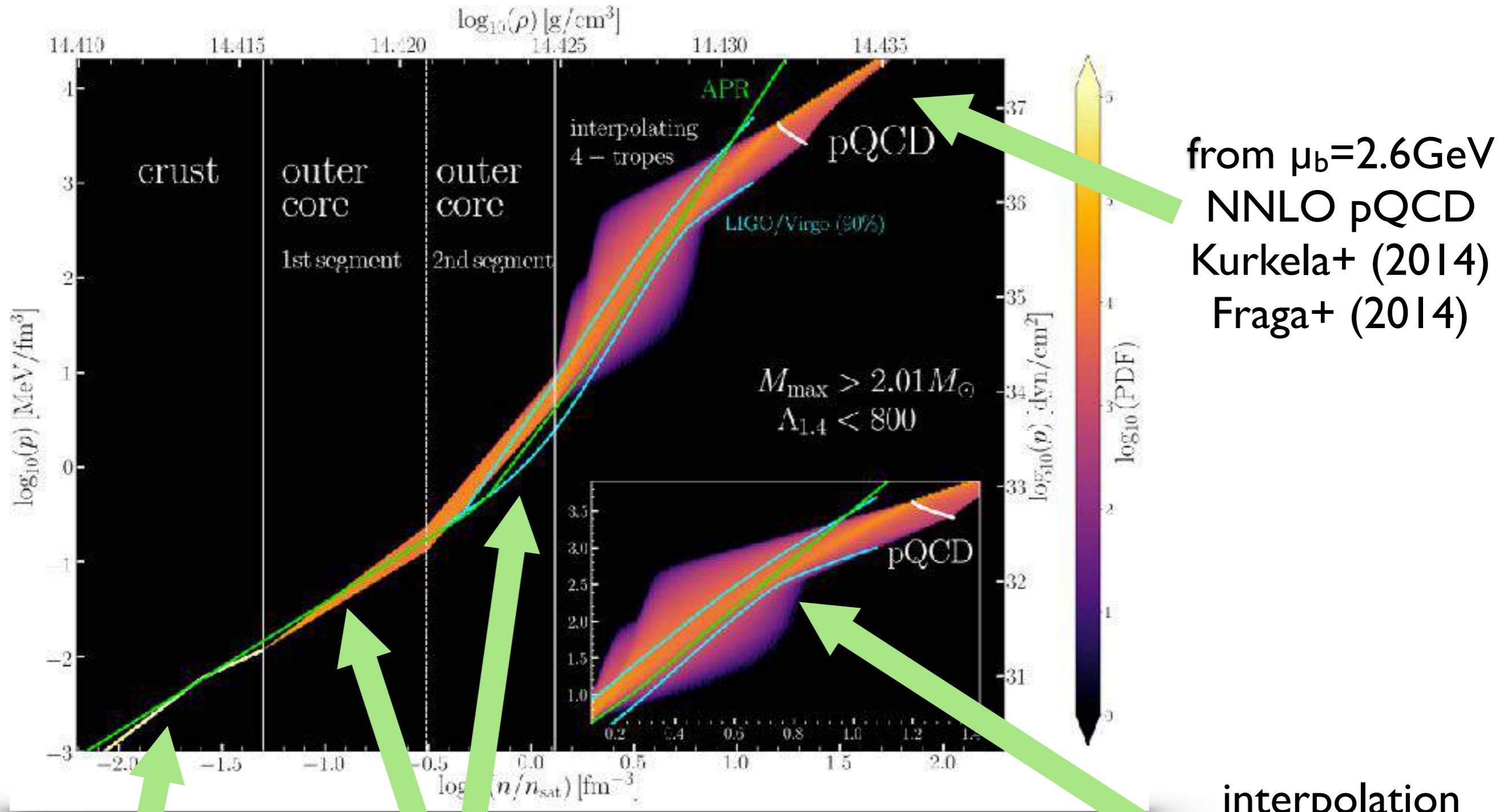
Abbott+ 2017



LR+ 2017

# parametrising our ignorance

- Construct most generic family of NS-matter EOs



from  $\mu_b=2.6\text{GeV}$   
NNLO pQCD  
Kurkela+ (2014)  
Fraga+ (2014)

BPS

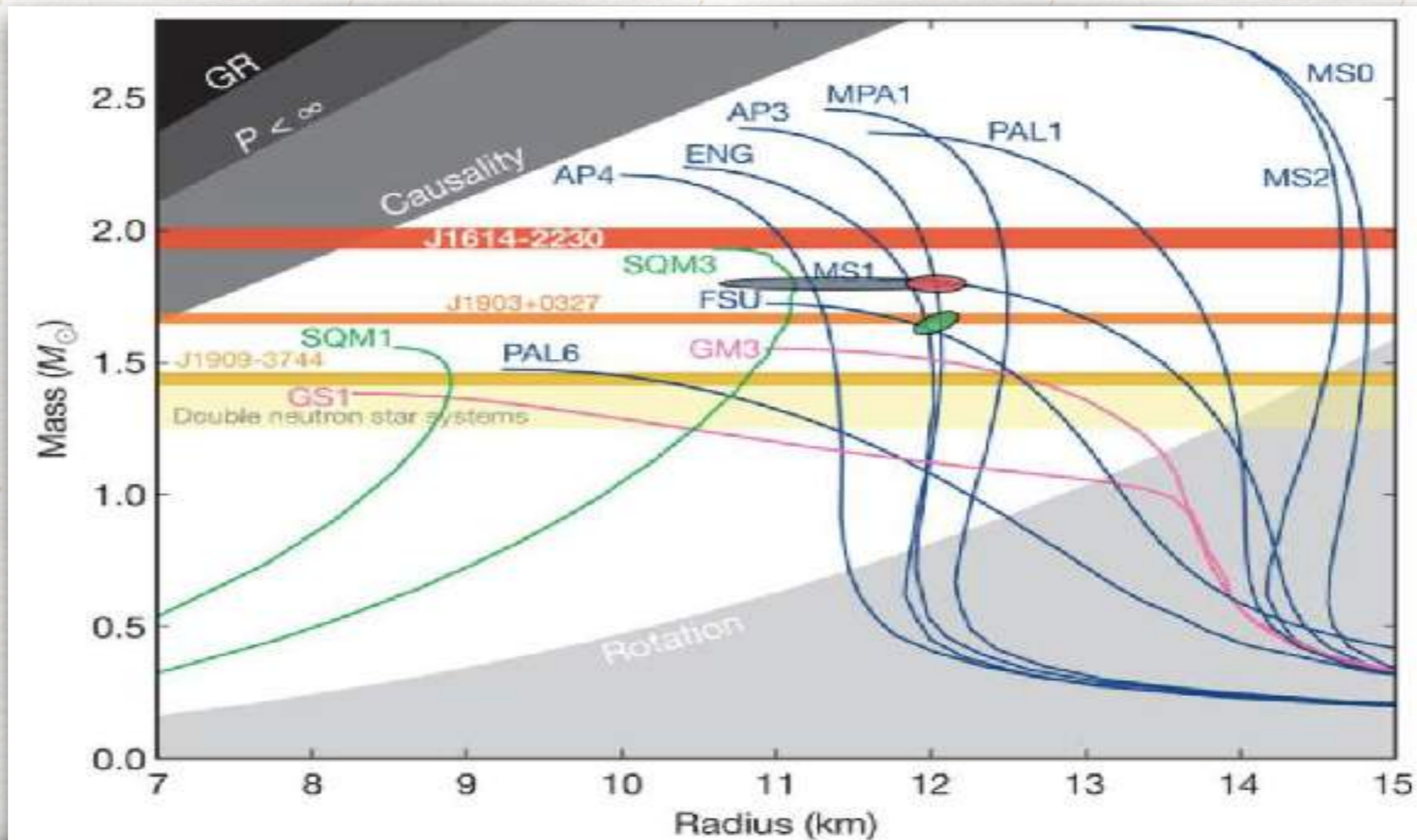
polytropic fit of Drischler+ (2016)  
(large impact on results)

interpolation  
by matching 4  
polytropes

# Mass-radius relations

- We have produced  $10^6$  EOSs with about  $10^9$  stellar models.

- Can impose differential constraints from the **maximum mass** and from the **tidal deformability** from **GW170817**

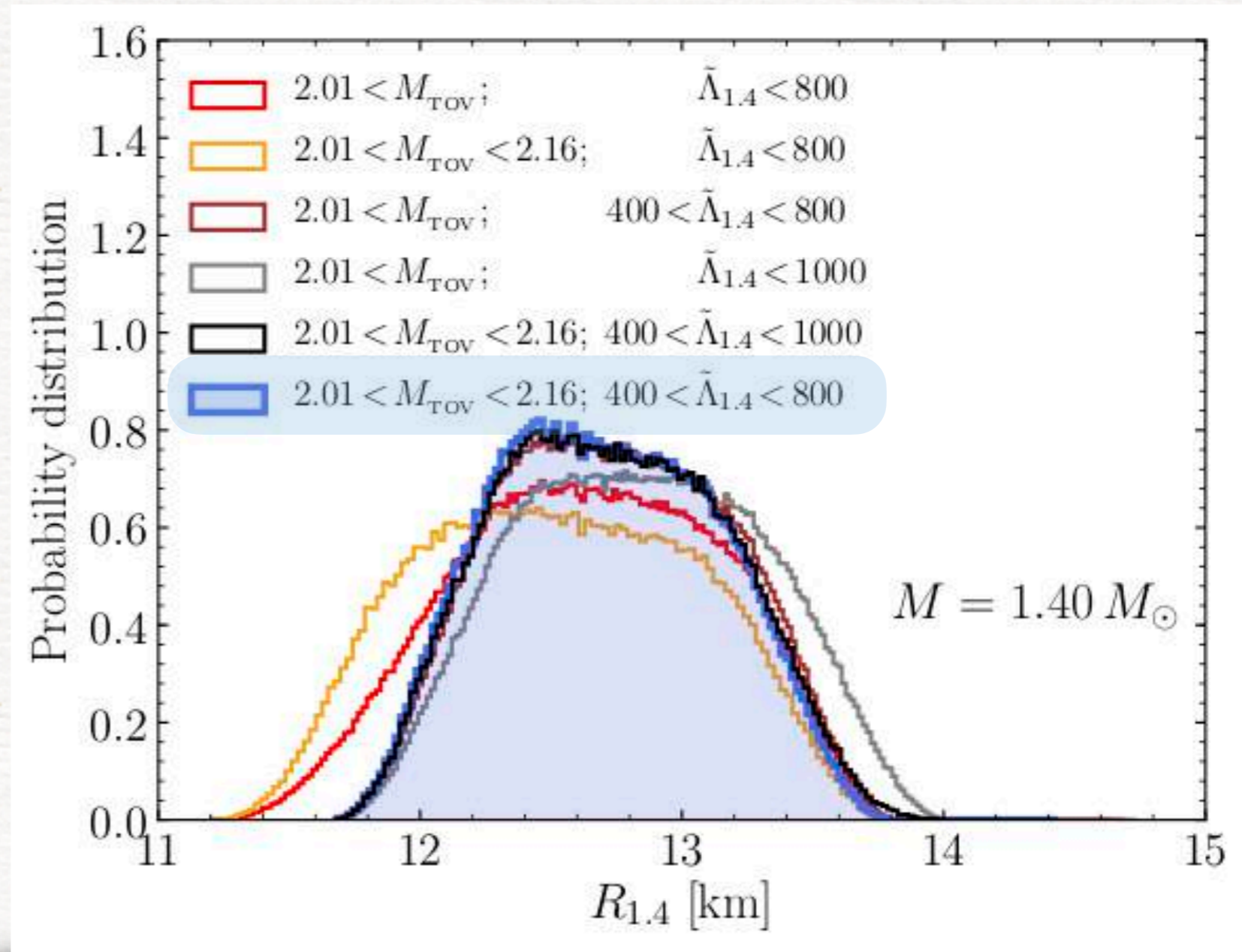


# one-dimensional cuts

- Closer look at a mass of  $M = 1.40 M_{\odot}$
- Can play with different constraints on maximum mass and tidal deformability.
- Overall distribution is very robust

$$12.00 < R_{1.4}/\text{km} < 13.45$$

$$\bar{R}_{1.4} = 12.45 \text{ km}$$



# Constraining tidal deformability

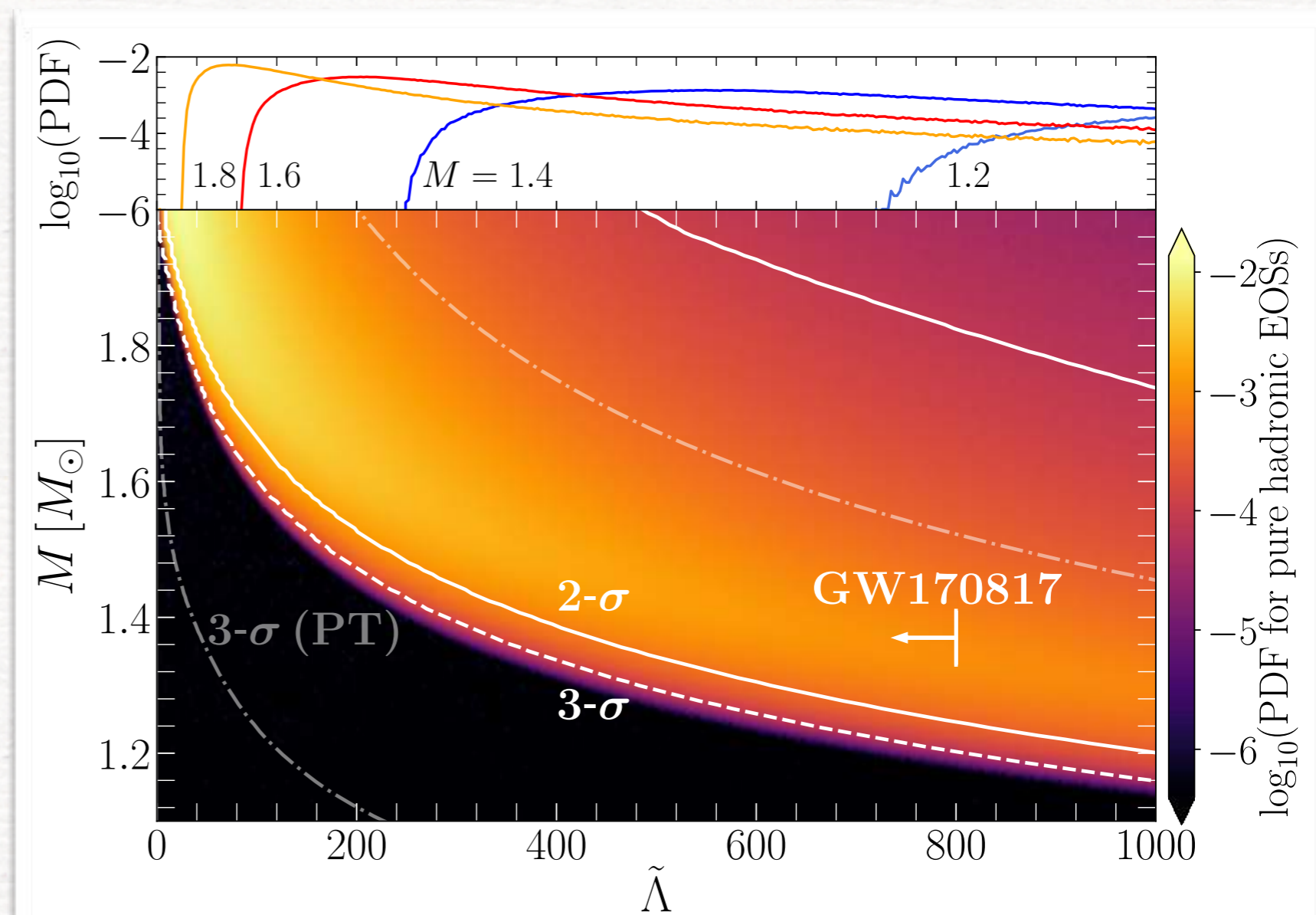
- Can explore statistics of all properties of our  $10^9$  models.
- In particular can study PDF of tidal deformability:  $\tilde{\Lambda}$

- LIGO has already set upper limit:

$$\tilde{\Lambda}_{1.4} \lesssim 800$$

- Our sample naturally sets a lower limit:

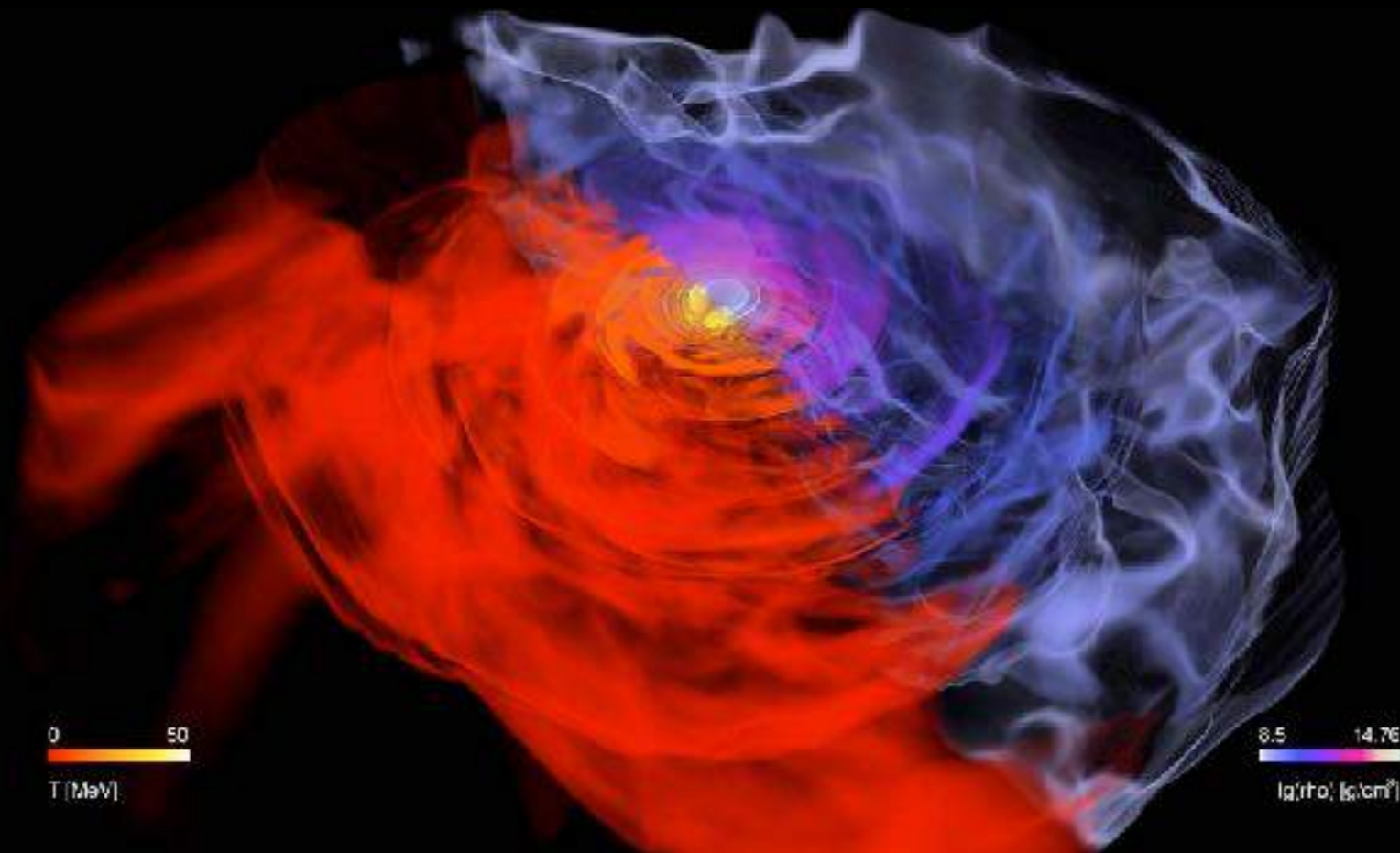
$$\tilde{\Lambda}_{1.4} > 375$$



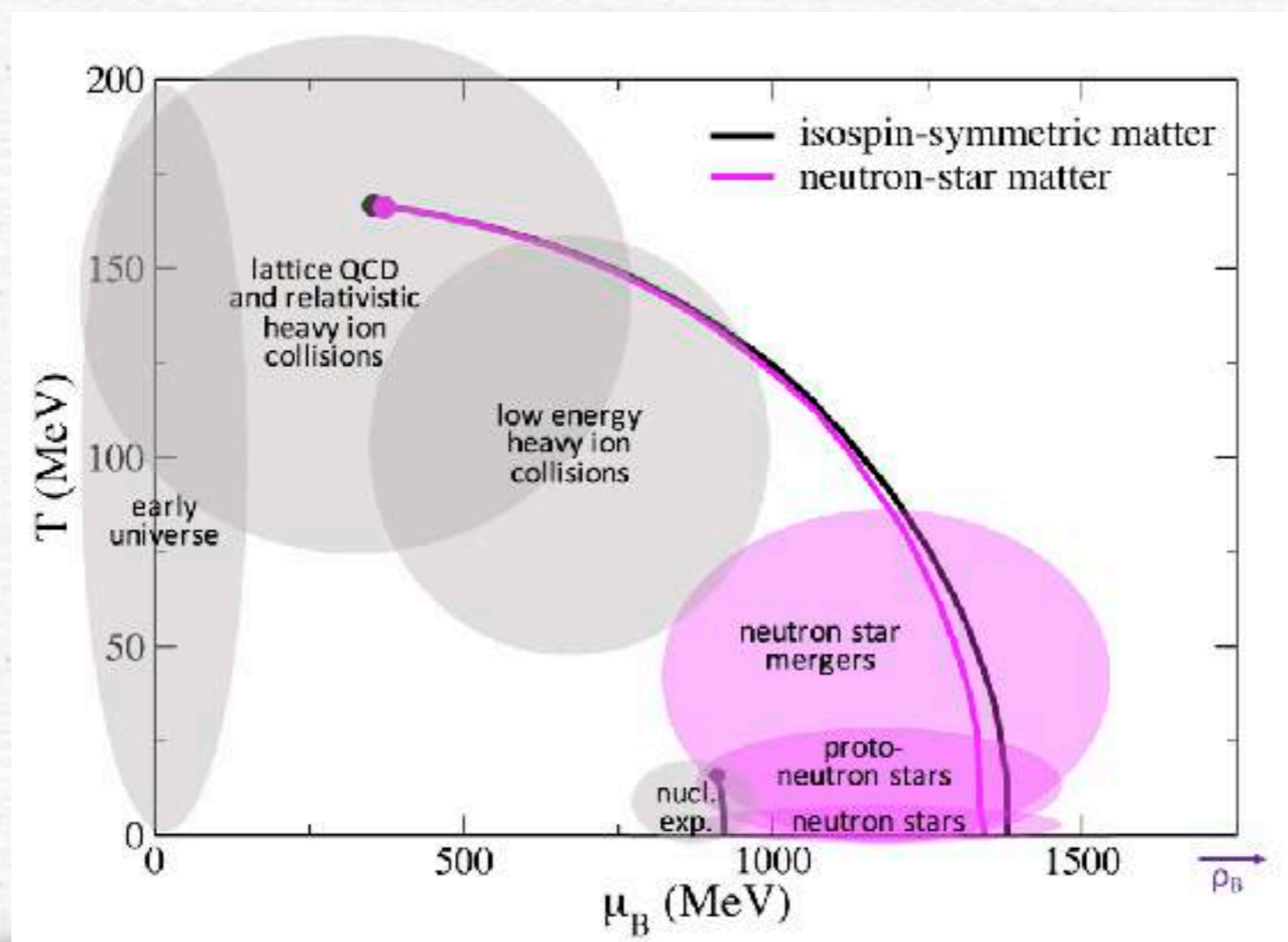


# Phase transitions and their signatures

Most, Papenfort, Dexheimer, Hanauske, Schramm, Stoecker, LR (2019)



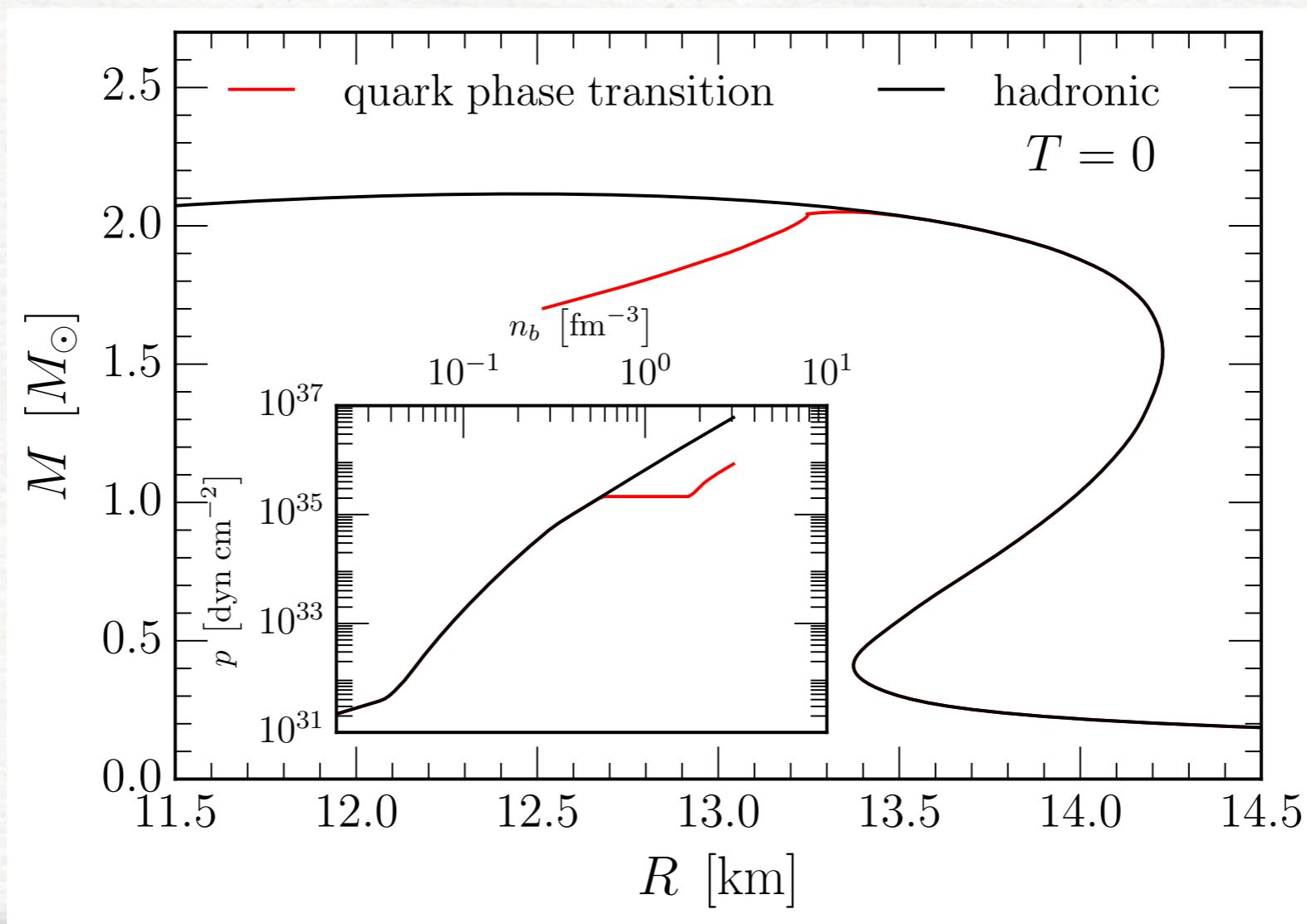
- \* **Strangeness** is expected in neutron stars both in the inspiral (hyperons) and possibly after merger (strange quarks?)
- \* **Isolated** neutron stars probe a small fraction of phase diagram



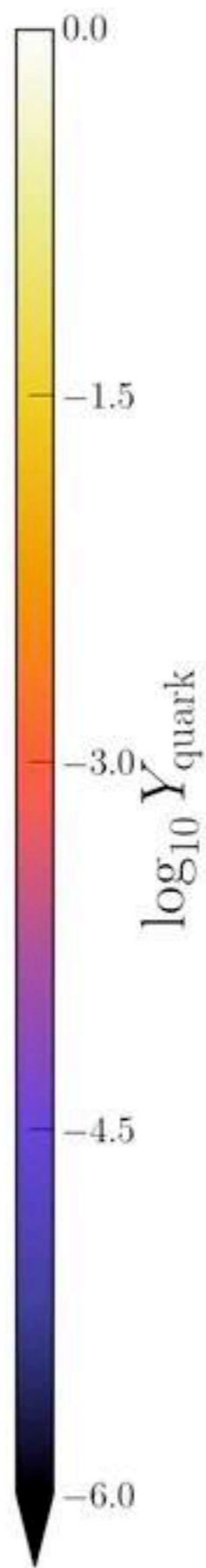
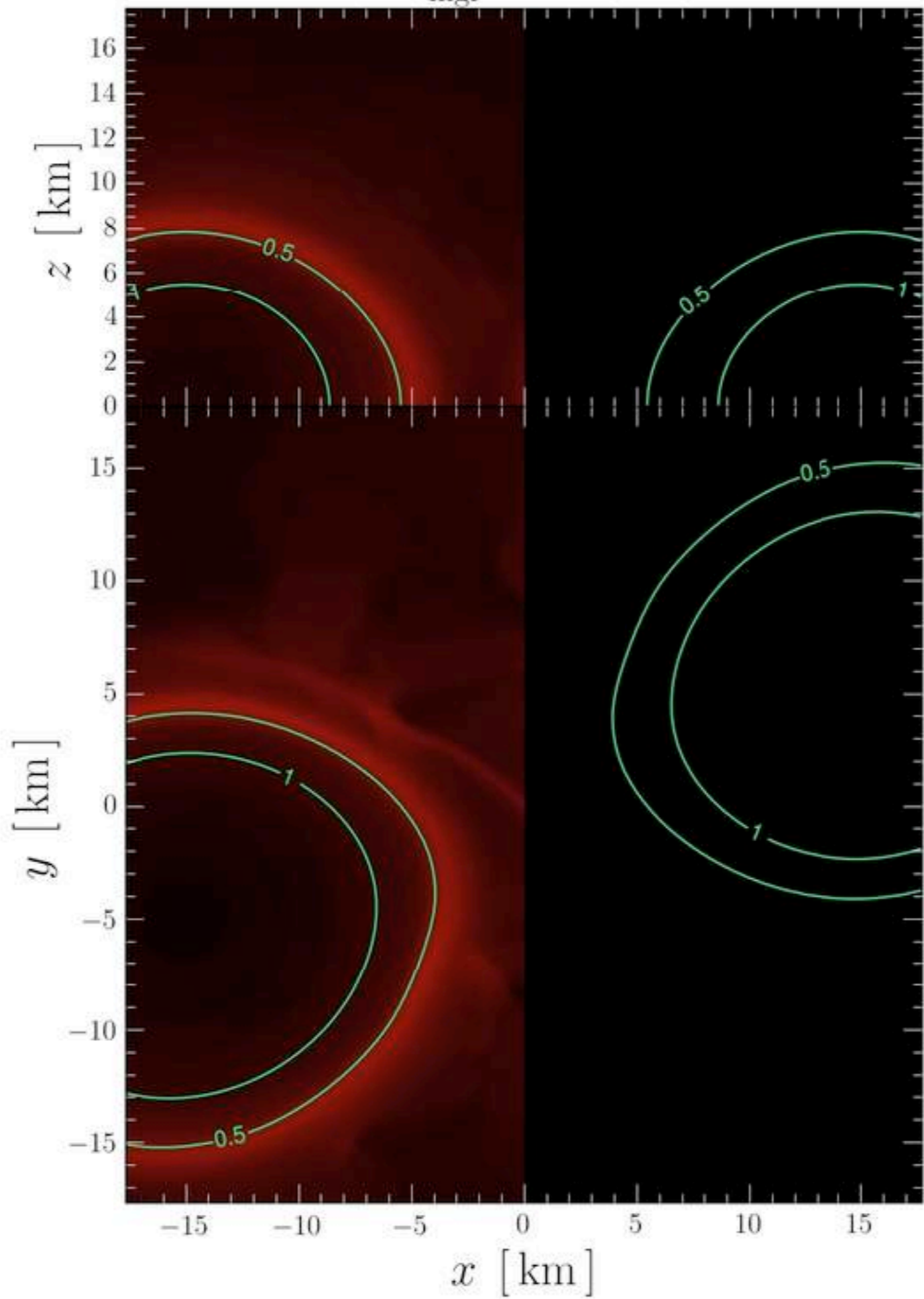
- \* Neutron-star **binary** mergers reach temperatures up to **80 MeV** and probe regions complementary to experiments

# Modelling the EOS

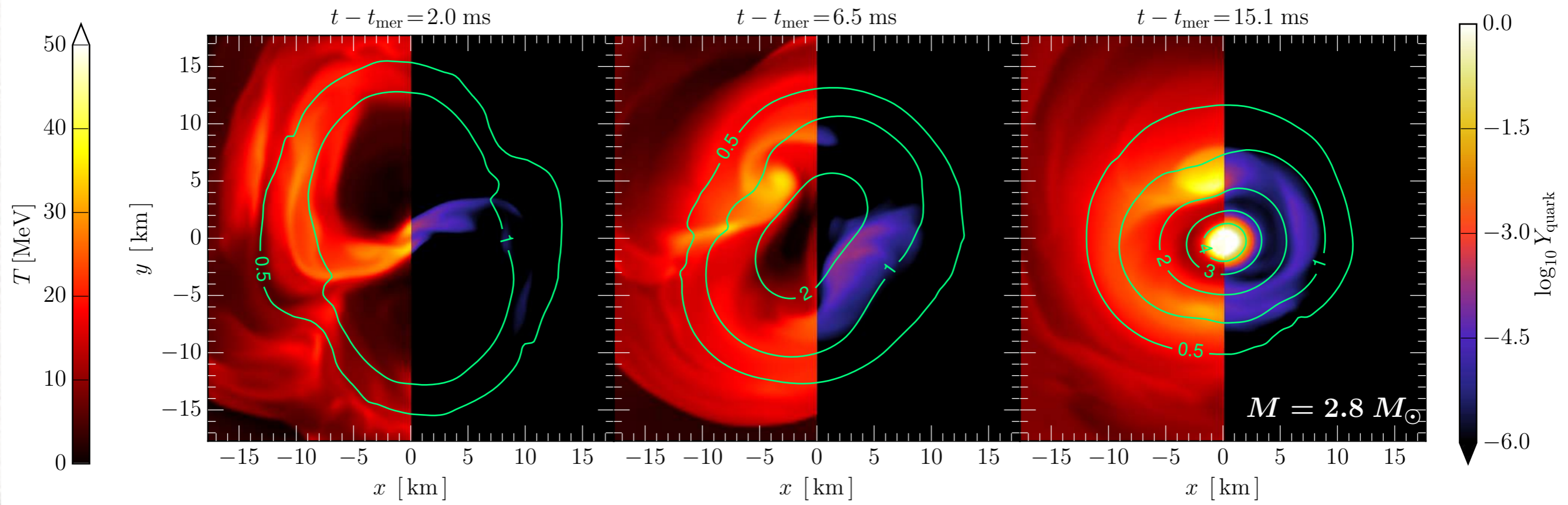
- EOS based on Chiral Mean Field (CMF) and nonlinear SU(3) sigma model
- Includes hyperons and quarks that can be turned on/off
- Uses Polyakov loop to implement a strong first order phase transition
- Includes a cross-over transition at high temperatures



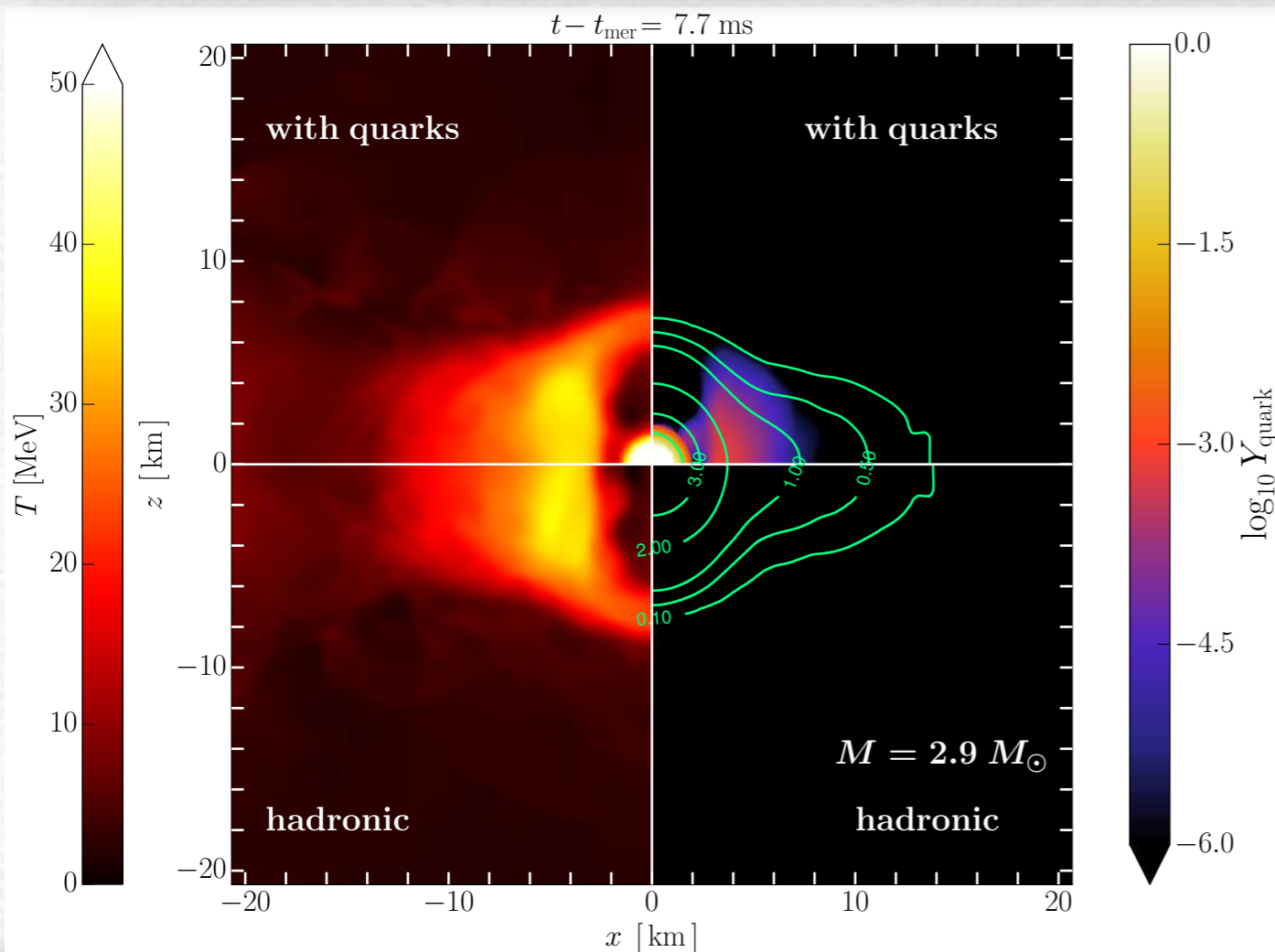
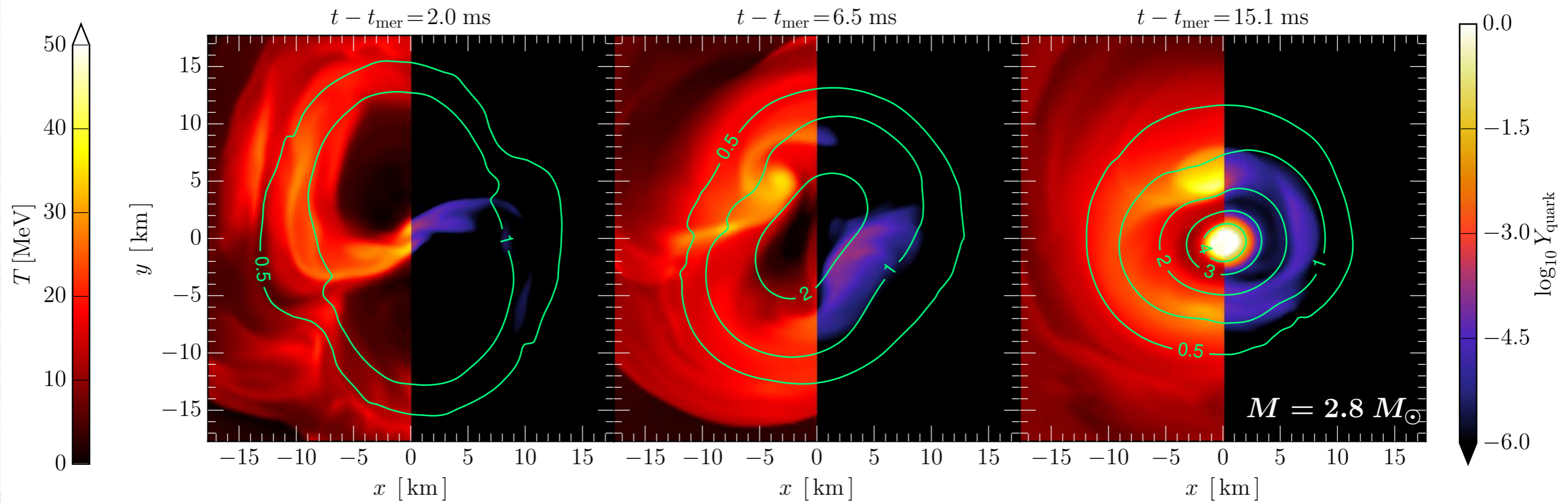
# Temperature



# Quark fraction

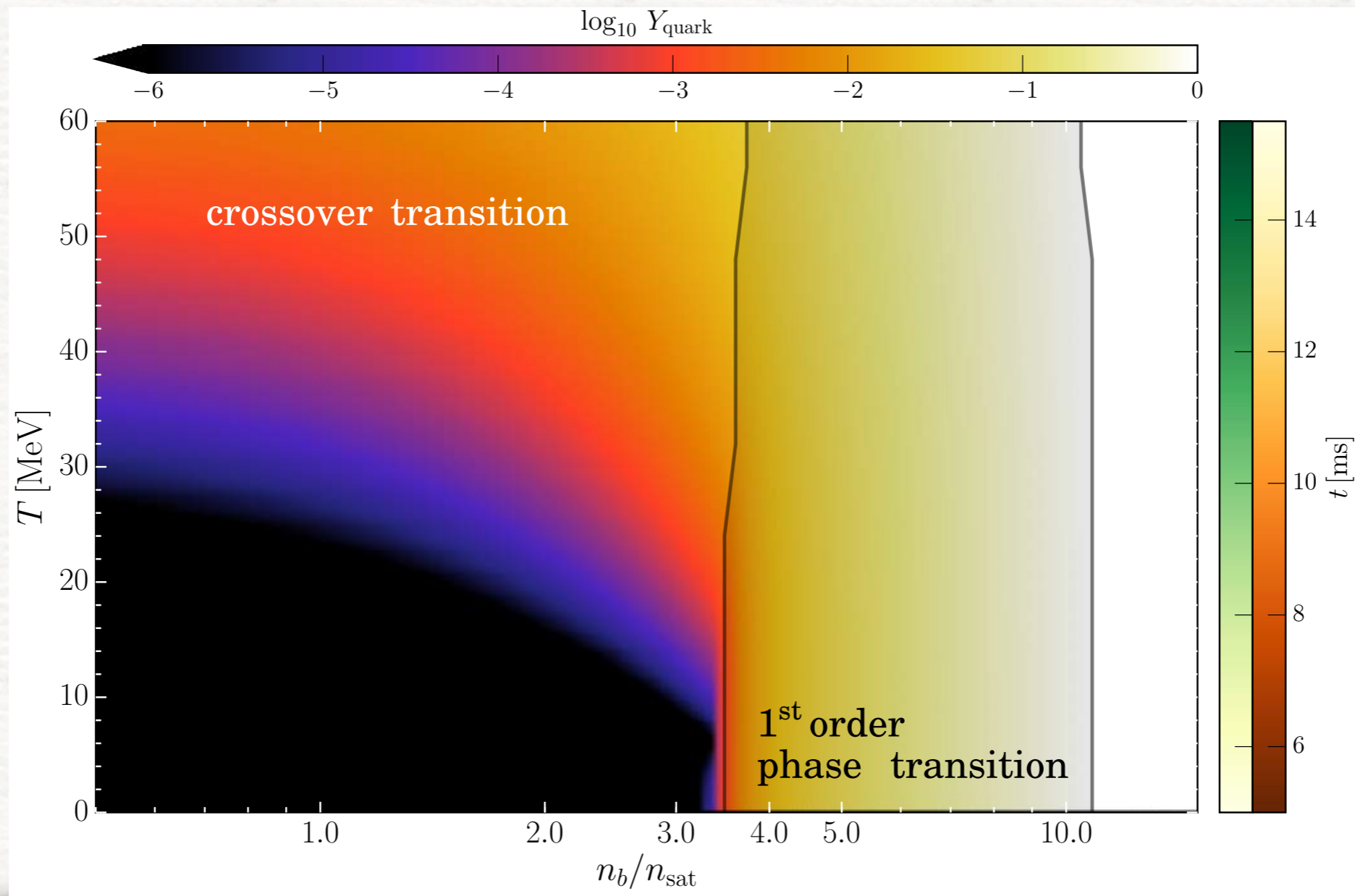


- EOS based on Chiral Mean Field (CMF) model, based on a nonlinear SU(3) sigma model.
- Quarks appear at sufficiently large temperatures and densities.



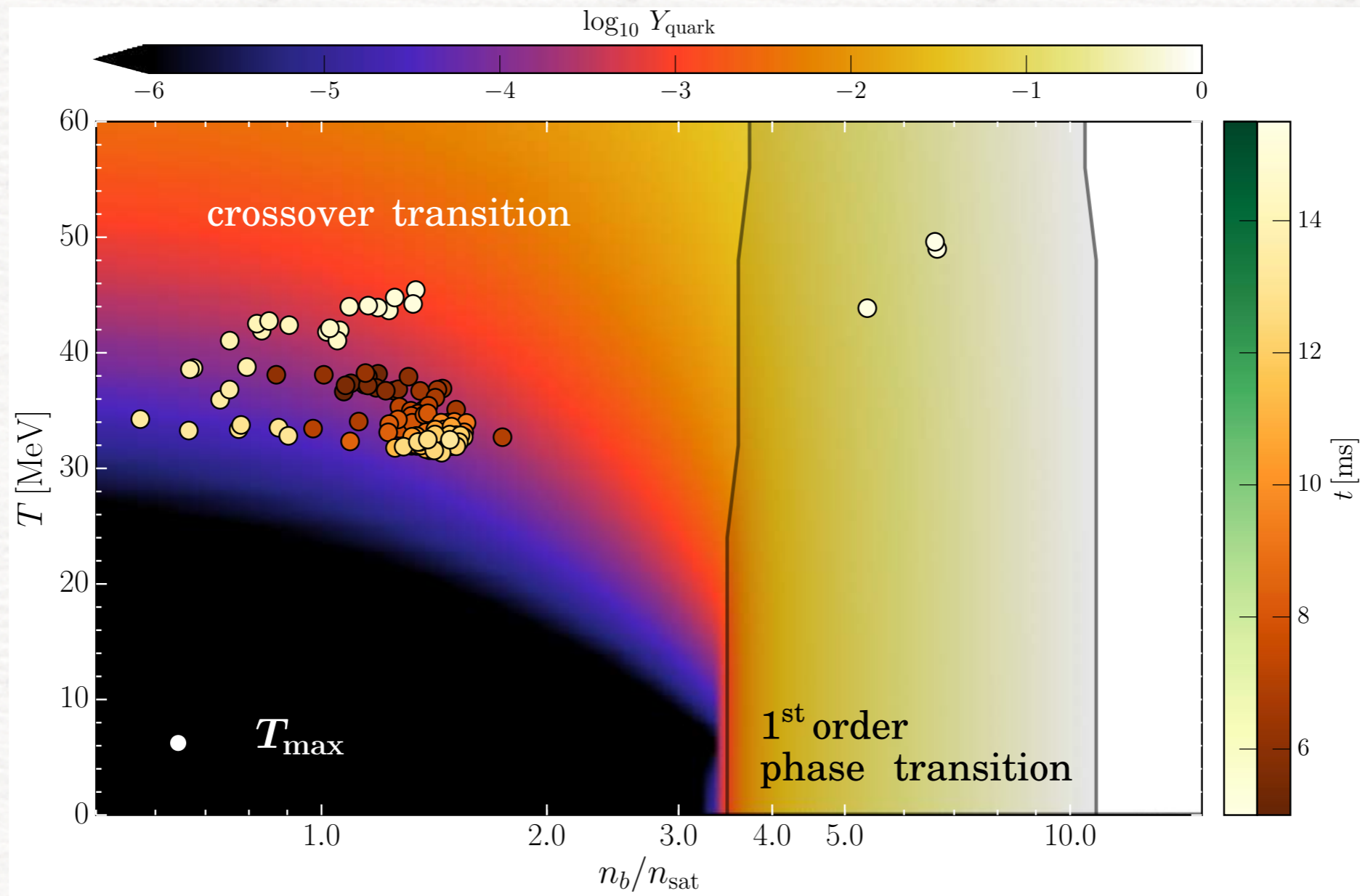
- EOS based on Chiral Mean Field (CMF) model, based on a nonlinear SU(3) sigma model.
- Quarks appear at sufficiently large temperatures and densities.
- For EOS without quarks, the dynamics is very similar, but no PT.

# Comparing with the phase diagram



- Phase diagram with quark fraction

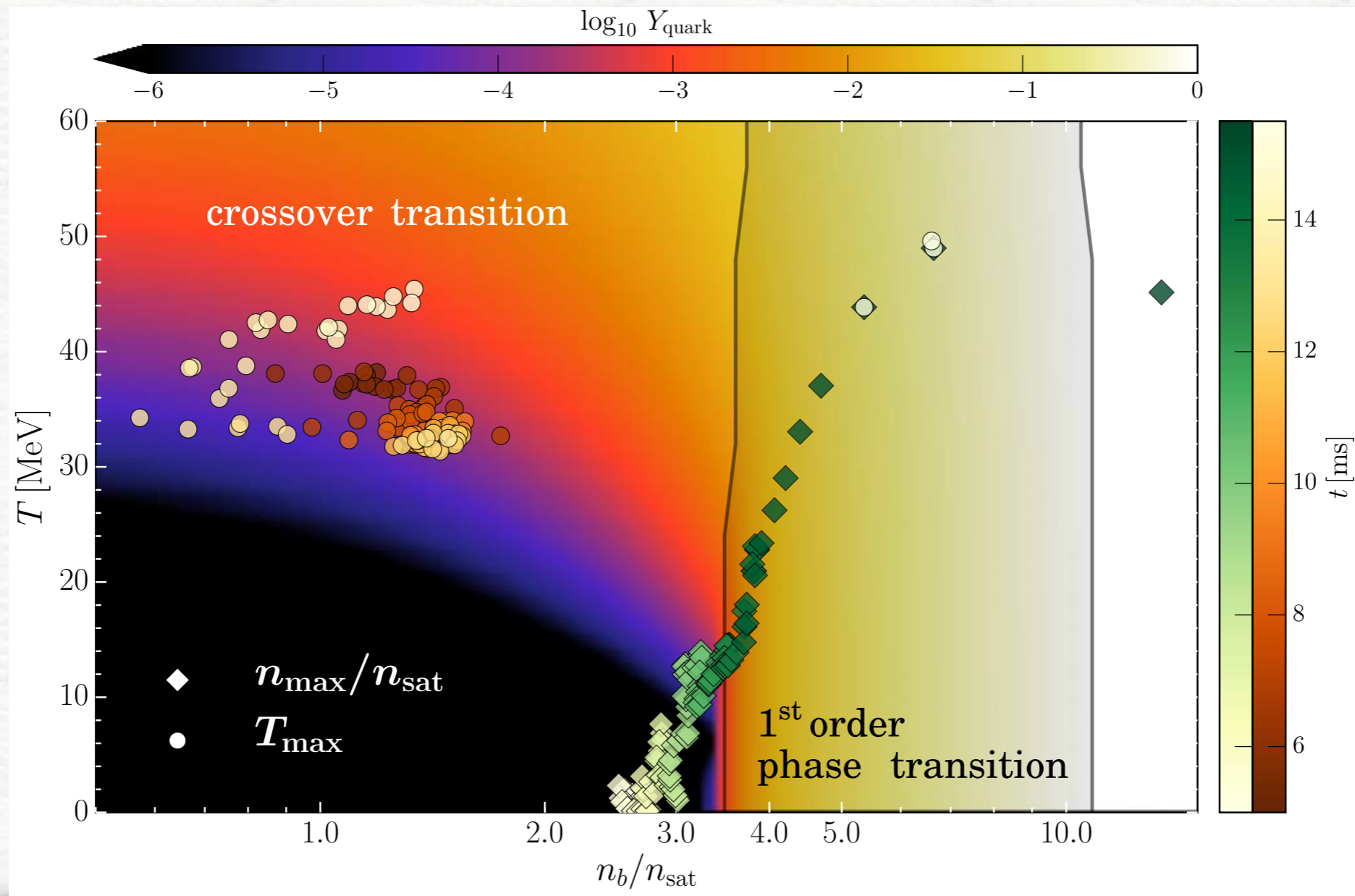
# Comparing with the phase diagram



- Phase diagram with quark fraction
- Circles show the position in the diagram of the maximum temperature as a function of time



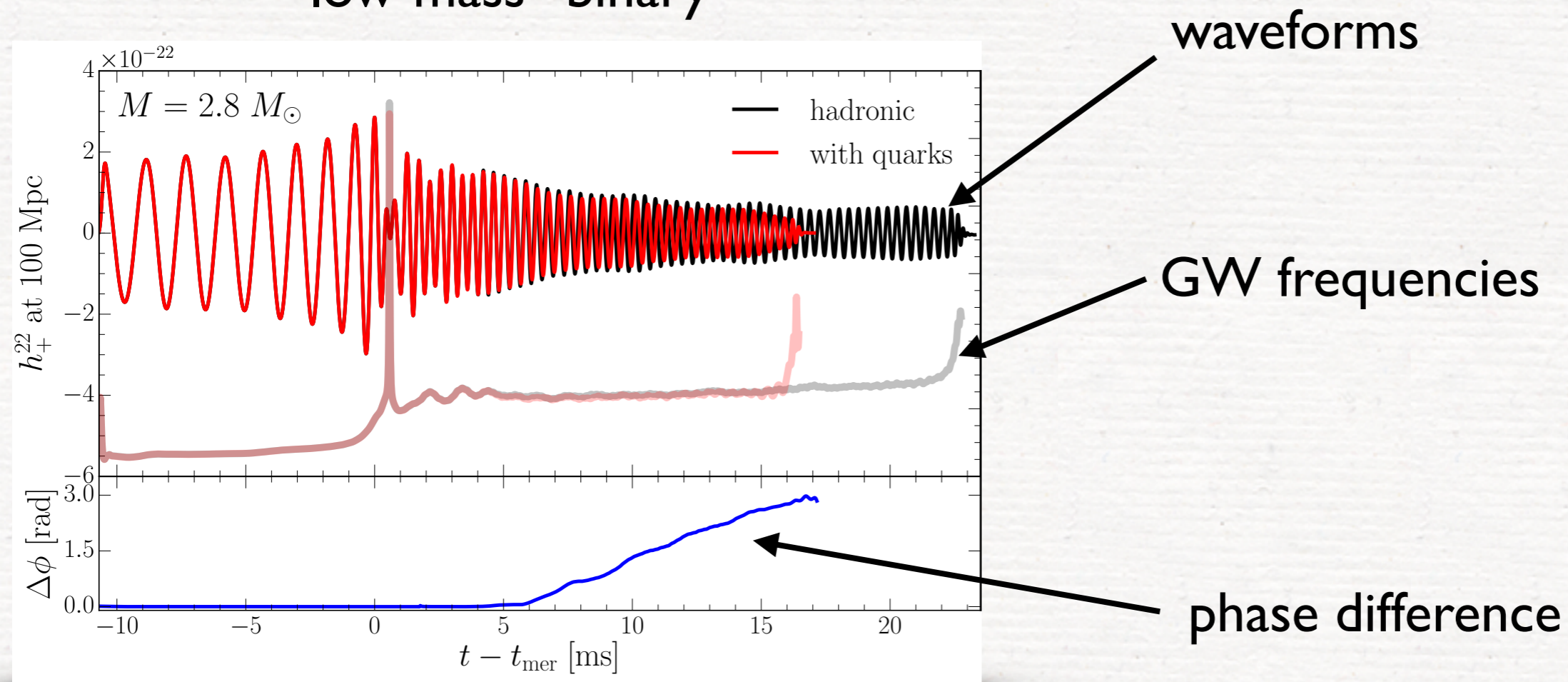
# Comparing with the phase diagram



- Reported are the evolution of the max. temperature and density.
- Quarks appear already early on, but only in small fractions.
- Once sufficient density is reached, a full phase transition takes place.

# Gravitational-wave emission

“low-mass” binary

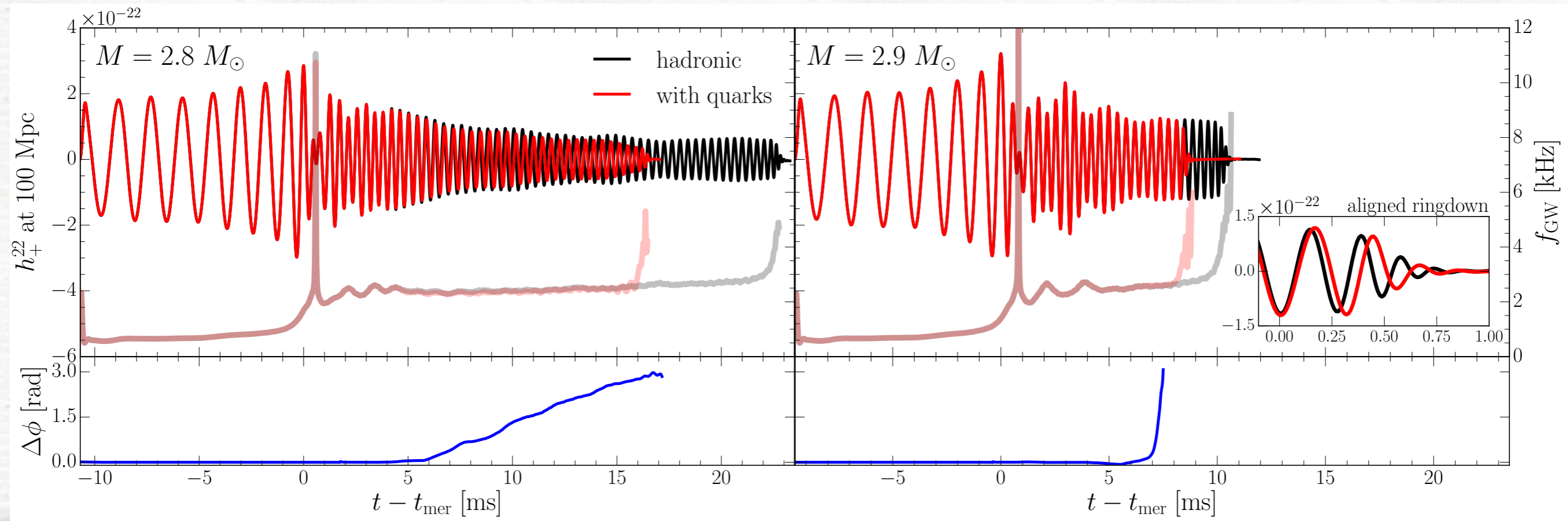


- In **low-mass binary**, after  $\sim 5$  ms, quark fraction is large enough to change quadrupole moment and yield differences in the waveforms.
- Note the phase difference is **zero** in the inspiral.
- Sudden softening of the phase transition leads to collapse and **large difference** in phase evolution.

# Gravitational-wave emission

“low-mass” binary

“high-mass” binary



- In **low-mass binary**, after  $\sim 5$  ms, quark fraction is large enough to change quadrupole moment and yield differences in the waveforms.
- In **high-mass binary**, phase transition takes place rapidly after  $\sim 5$  ms. Waveforms are similar but **ringdown** is **different** (free fall for PT). Observing mismatch between **inspiral** (fully hadronic) and **post-merger** (phase transition): clear **signature** of a **PT**.

# Recap

- ✓ Spectra of post-merger shows clear “**quasi-universal**” peaks
- ✓ GW spectroscopy possible with post-merger signal
- ✓ Unless binary very close, peaks have **SNR  $\sim 1$** . Multiple signals can be stacked and **SNR will increase coherently**.
- ✓ Only inspiral detected in GW170817 but new limits set on:

## Maximum mass

$$2.01_{-0.04}^{+0.04} \leq M_{\text{TOV}}/M_{\odot} \lesssim 2.16_{-0.15}^{+0.17}$$

## Typical radii and tidal deformabilities

$$12.00 < R_{1.4}/\text{km} < 13.45 \quad \tilde{\Lambda}_{1.4} > 375 \quad \text{hadronic EOSs}$$

$$8.53 < R_{1.4}/\text{km} < 13.74 \quad \tilde{\Lambda}_{1.4} \gtrsim 35 \quad \tilde{\Lambda}_{1.7} \lesssim 460 \quad \text{phase transitions}$$

- ✓ Phase transition can take place after merger leading to clear signatures: mismatch between inspiral and postmerger.