

Quantum walks in optical lattices

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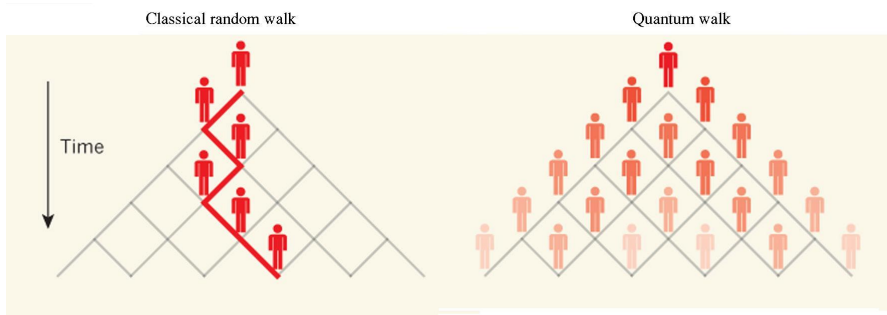
Cracow School of Theoretical Physics,
LVII Course, 2017 Entanglement and Dynamics

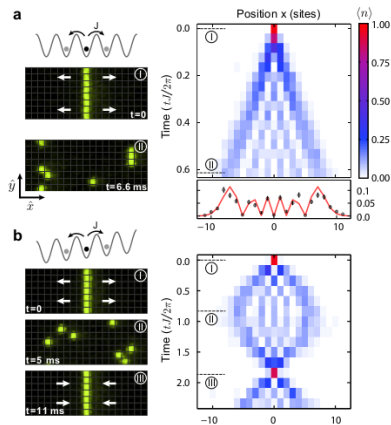
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Outline

- 1 Introduction
 - Classical and quantum walks
 - Hamiltonian of the system
- 2 Quantum evolution of the system
 - Free evolution and Bloch oscillations
 - Long-range interactions
 - Disorder and MBL effects
 - Bloch oscillations decay in disordered media
- 3 Conclusions

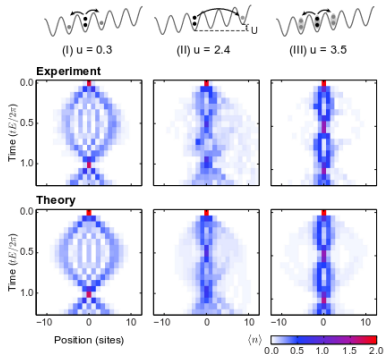
- Classical case refers to the standard random walk with gaussian probability distribution
- Quantum walks can be discrete (which are quantum version of coin flipping) or continuous (which are govern by hamiltonian)





• Experimental realization in optical lattices:

Science 347, 1229 (2015) - Greiner Lab



$$\hat{H}_{\text{BH}} = -J \sum_i \left(\hat{a}_{i+1}^\dagger \hat{a}_i + h.c. \right) + \frac{U}{2} \sum_i \hat{n}_i (\hat{n}_i - 1), \quad (1)$$

external perturbations of the model:

$$\hat{H}_{\text{ext}} = \hat{T} + \hat{V} + \hat{D}, \quad (2)$$

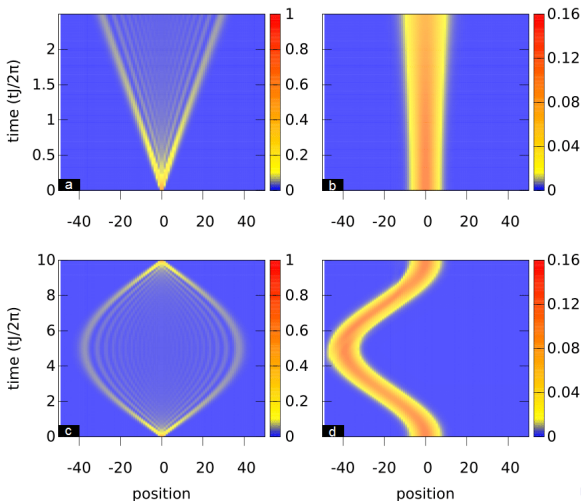
where

$$\hat{T} = F \sum_i i \hat{a}_i^\dagger \hat{a}_i, \quad (3a)$$

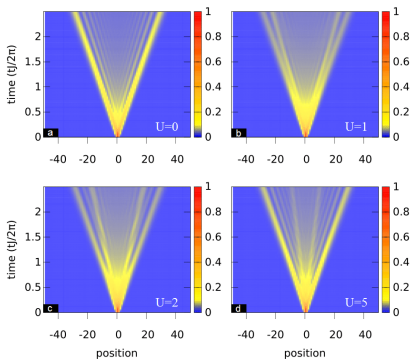
$$\hat{V} = V \sum_i \sum_{k \neq 0} k^{-\alpha} \hat{n}_i \hat{n}_{i+k}, \quad (3b)$$

$$\hat{D} = \lambda \sum_i \cos [2\pi(\tau i + \phi)] \hat{a}_i^\dagger \hat{a}_i. \quad (3c)$$

One particle quantum walk evolution:



Evolution with standard Bose-Hubbard Hamiltonian for a few on-site interaction values:

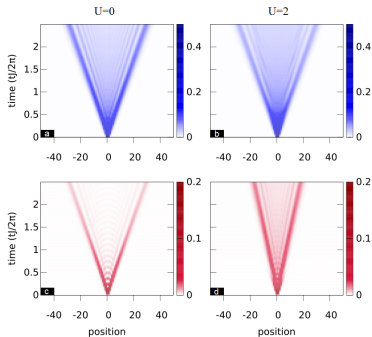


$$n(i) = \langle \psi(t) | \hat{a}_i^\dagger \hat{a}_i | \psi(t) \rangle. \quad (4)$$

We divide $n(i)$ into two sectors:

$$n_2(i) = \langle \psi(t) | \hat{a}_i^\dagger \hat{a}_i^\dagger \hat{a}_i \hat{a}_i | \psi(t) \rangle, \quad (5a)$$

$$n_1(i) = n(i) - n_2(i). \quad (5b)$$



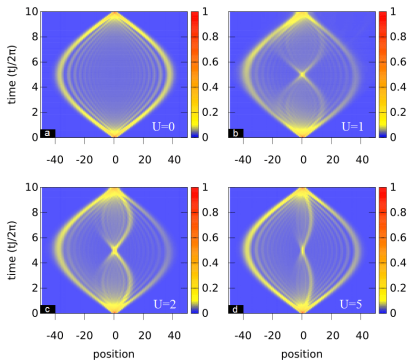
R. Khomeriki, D. O. Krimer, M. Haque, and S. Flach, Phys. Rev. A 81, 065601 (2010):

Effective tunneling for paired bosons:

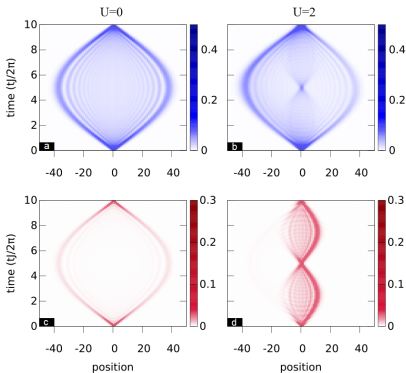
$$t_2 = (\sqrt{U^2 + 16} - U)/4$$

$$\hat{H} = \hat{H}_{BH} + \hat{T}$$

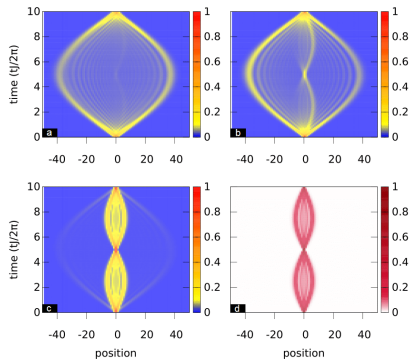
In tilted lattices system reveals Bloch oscillations:



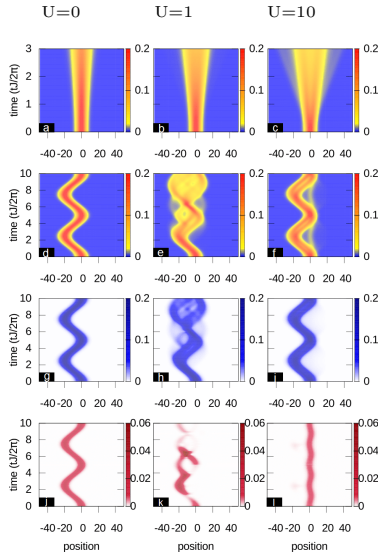
We again divide density distribution into two sectors:



How evolution depends on the initial state?



Evolution for gaussian initial states:



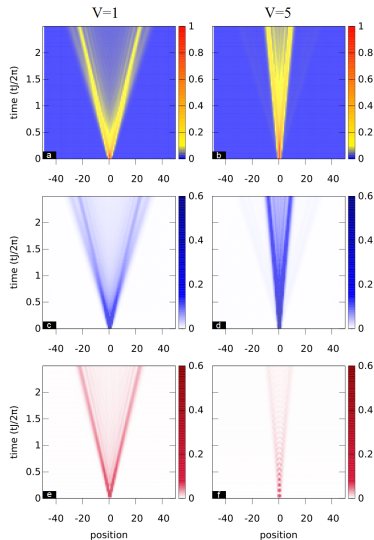
Evolution with long-range interactions:

- Hamiltonian:

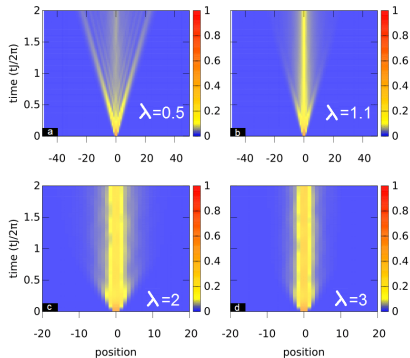
$$\hat{H} = \hat{H}_{BH} + \hat{V}$$

The lattice is not tilted !

- Long-range interactions speeds down expansion

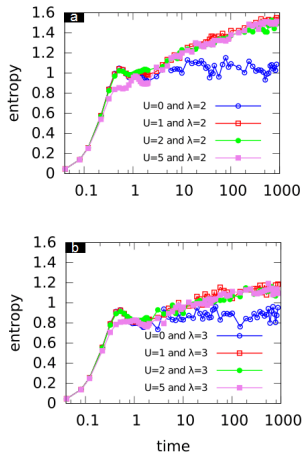


One-particle localization:



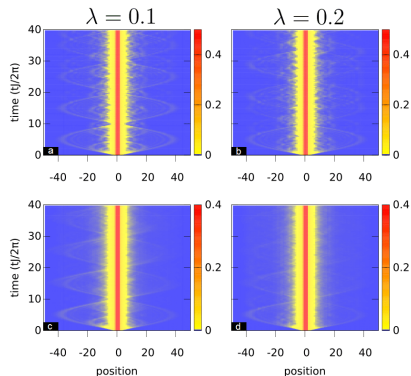
Aubry-Andre localization above threshold $\lambda = 2$

Entanglement entropy (two particle system) - logarithmic growth - signature of the MBL



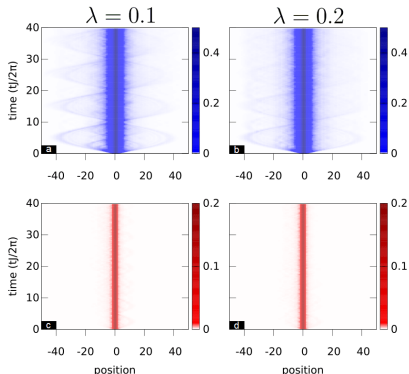
Experimental observation of MBL - Science 349, 842 (2015)

$$\hat{H} = \hat{H}_{BH} + \hat{T} + \hat{D}$$



Bloch oscillations in disordered media are damped!

Comparison between one-particle and two-particle sector:



- Quantum walks were successfully implemented in optical lattices (Greiner Lab)
- They reveal general quantum features like: Bloch oscillations, one-particle localization, MBL
- Evolution strongly depends on the initial state and parameters of the lattice
- Division of the density distribution into one-particle and two-particle shows explicitly different character of the evolution