

Transverse-momentum spectra in heavy-ion collisions at $\sqrt{s_{NN}} = 2.76$ TeV within chemical non-equilibrium model

Viktor Begun

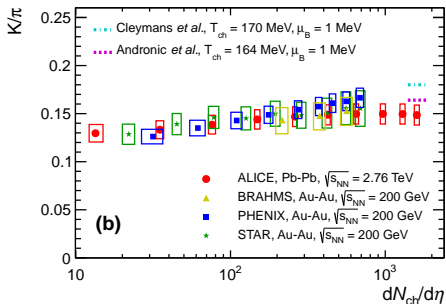
Jan Kochanowski University, Kielce, Poland

June 19, 2014

V.B., W. Florkowski, M. Rybczynski, 1312.1487, 1405.7252

Motivation

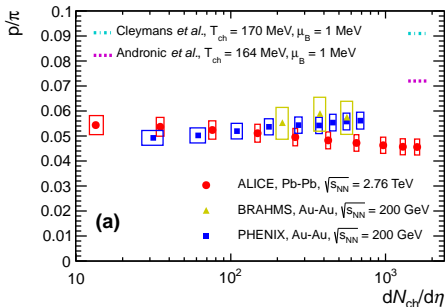
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- ▶ The measured **proton** abundances at \sqrt{s} 2.76 TeV at **LHC** did **not agree** with the predictions of the statistical models



B. Abelev *et al.*, [ALICE Collaboration] PRC 88 (2013)

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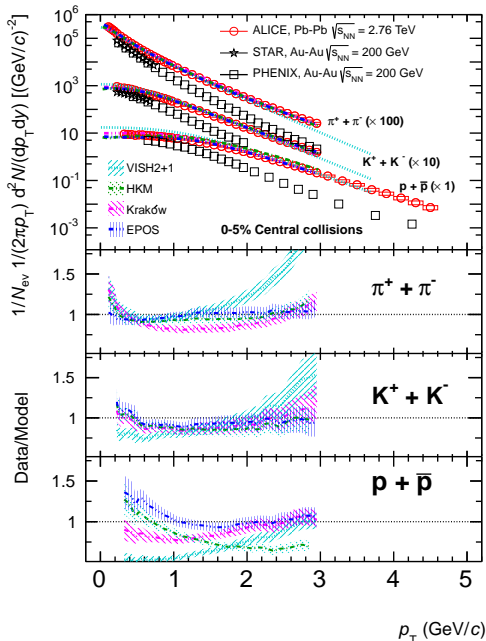
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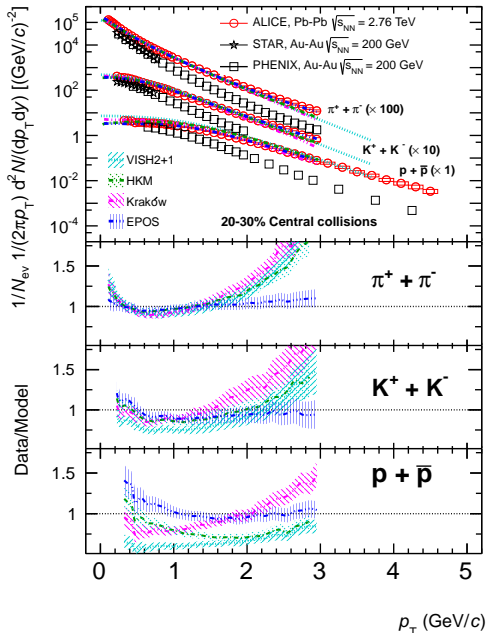
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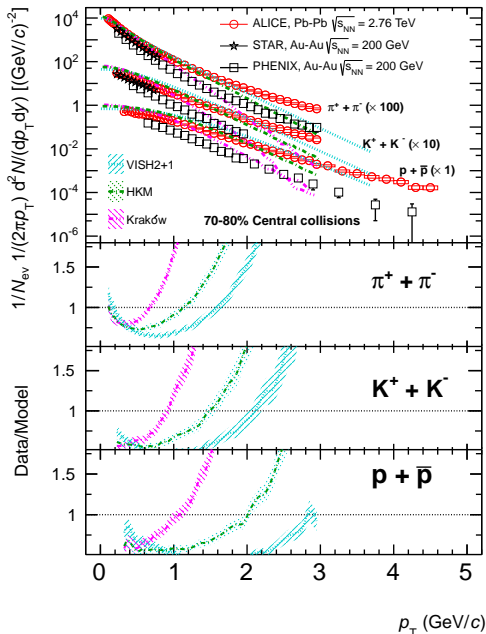
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The Cracow Model

- ▶ Transverse-momentum distributions are calculated from the [Cooper-Frye formula](#):

$$\frac{dN}{dyd^2p_T} = \int d\Sigma_\mu p^\mu f(p \cdot u),$$

where $d\Sigma_\mu$ is an element of the freeze-out hypersurface and u^μ is the hydrodynamic flow at freeze-out

- ▶ The [primordial](#) distribution of the i -th hadron in the local rest frame has the form:

$$f_i = g_i \int \frac{d^3p}{(2\pi)^3} \frac{1}{\Upsilon_i^{-1} \exp(\sqrt{p^2 + m_i^2}/T) \mp 1}$$

where $\Upsilon_i = \gamma_q^{N_q^i + N_{\bar{q}}^i} \gamma_s^{N_s^i + N_{\bar{s}}^i}$. The N_j^i are the numbers of [light](#) (u, d) and [strange](#) (s) [quarks](#) and [anti-quarks](#) in the i -th hadron. We compare the [non-equilibrium](#), $\gamma_j \neq 1$, and [equilibrium](#), $\gamma_j = 1$ cases

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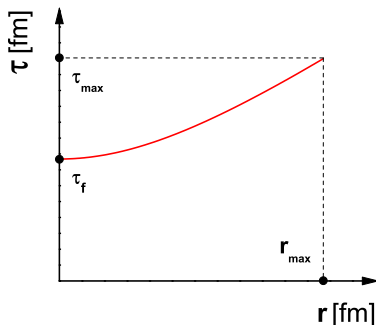
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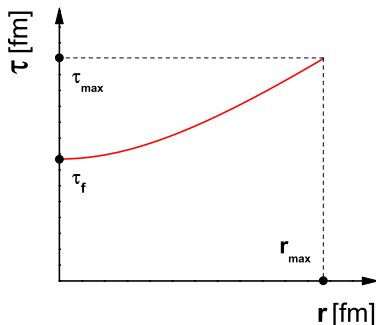
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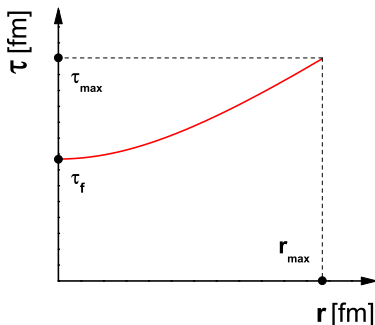
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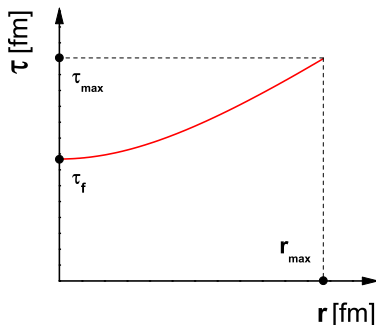
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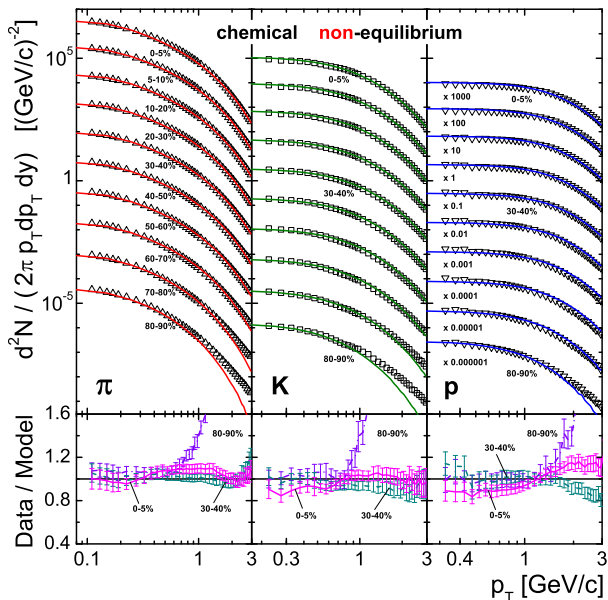
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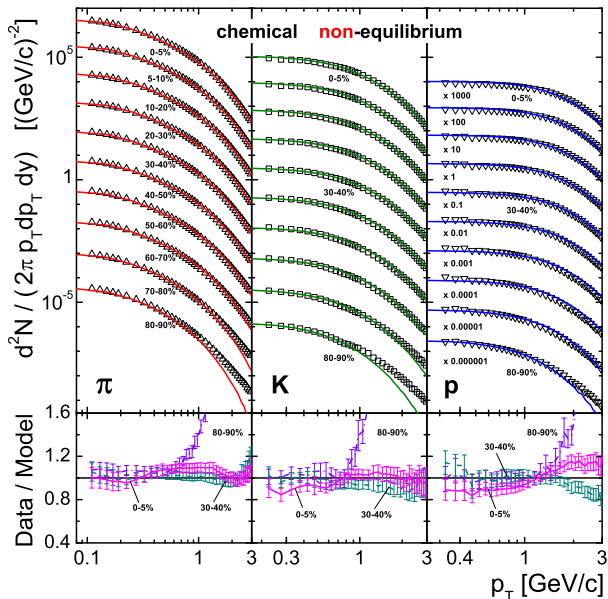
Pions, Kaons and Protons – Non-Equilibrium

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- ▶ Protons are not included in the fit, however our model explains well their spectrum



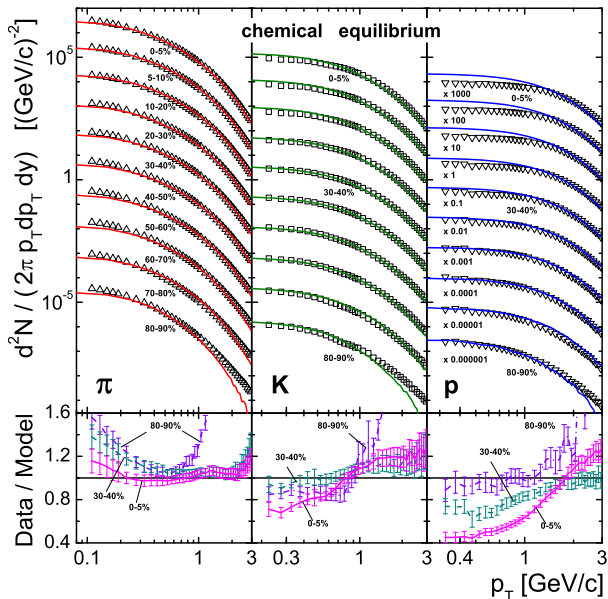
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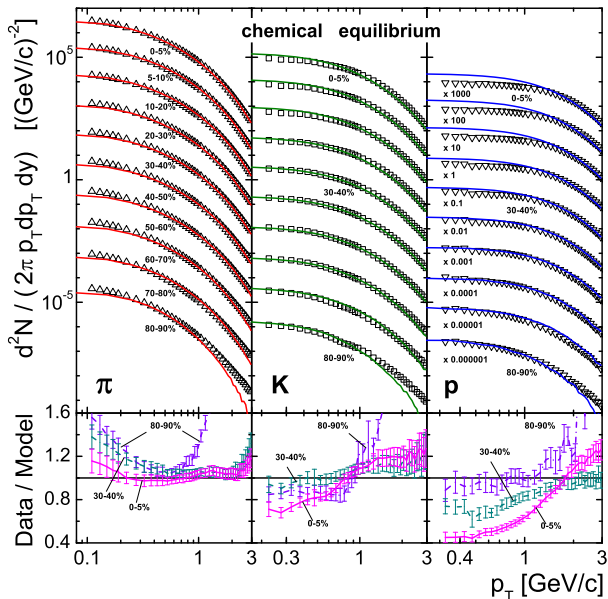
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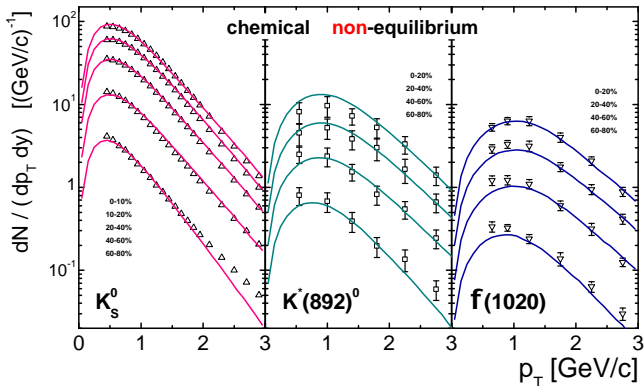
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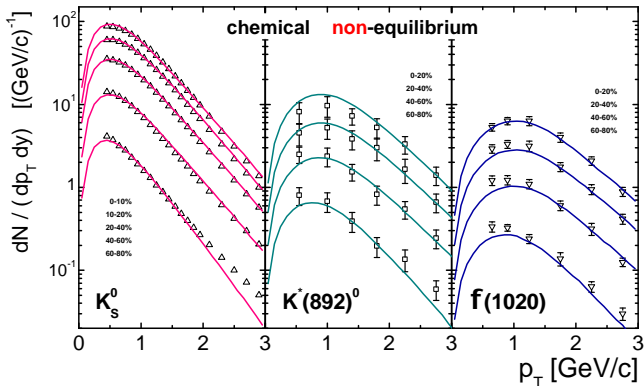
- ▶ Using exactly the **same parameters**, we have obtained an **excellent description** of K_S^0 , K^{*0} , and ϕ



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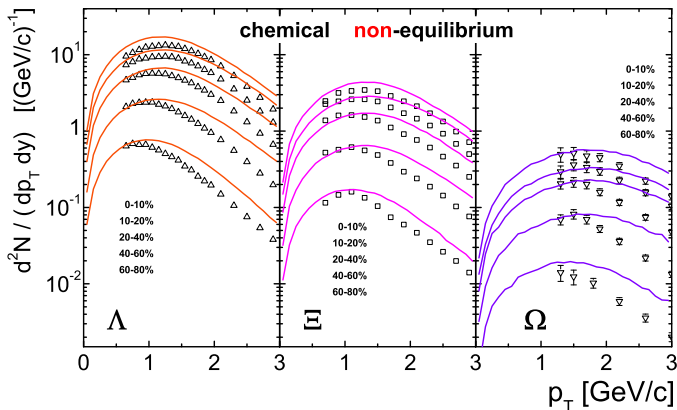
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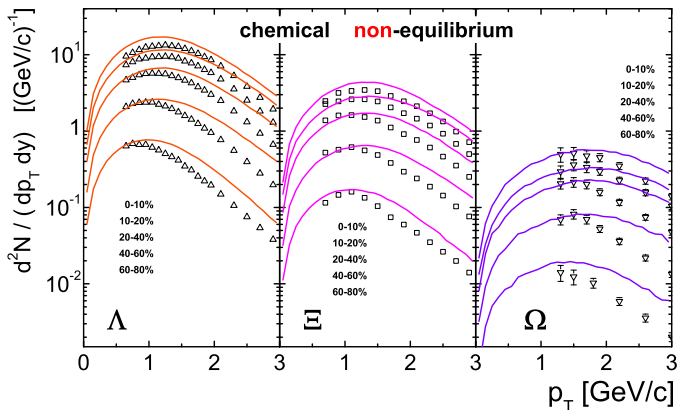
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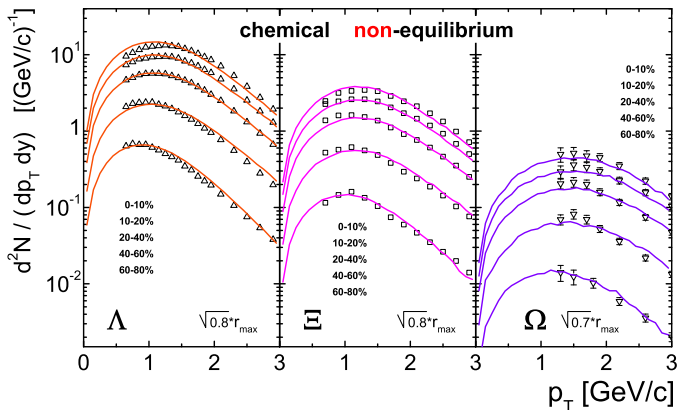
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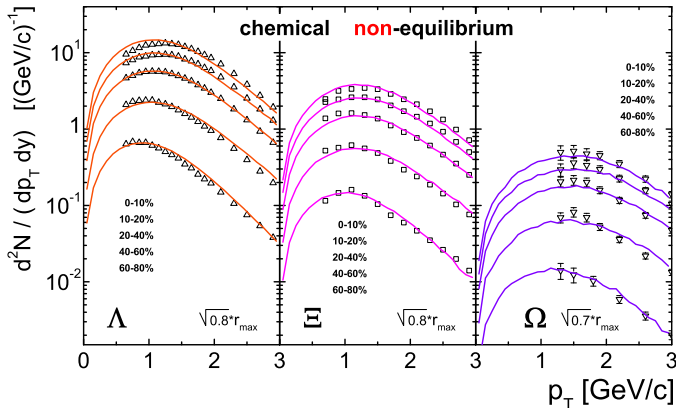
- ▶ The assumption of a **smaller** emission **volume** for Λ 's and Ξ 's (by 20%) and also for Ω 's (by 30%) gives us a **remarkable agreement**.



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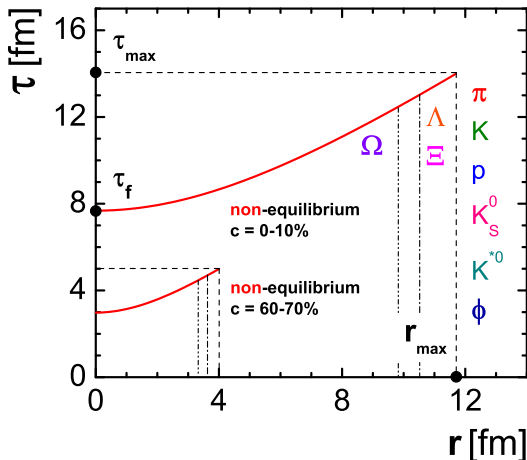
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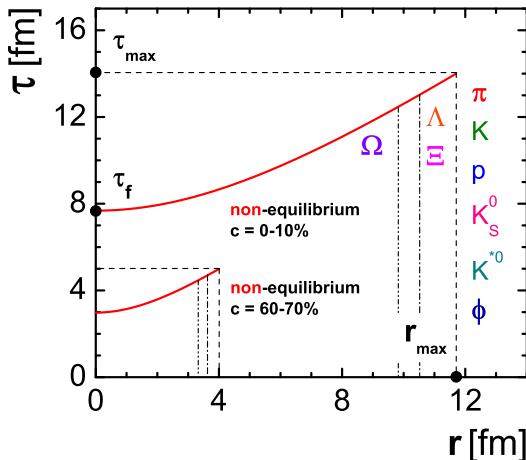
Freeze-out in Cracow Model at LHC

- ▶ In the center-of-mass frame at $z = 0$, the freeze-out starts in the center of the fireball at the time τ_f .
- ▶ Subsequently, it spreads out along the hyperbola $\tau(r) = \sqrt{\tau_f^2 + r^2} \leq \sqrt{\tau_f^2 + r_{\max}^2}$



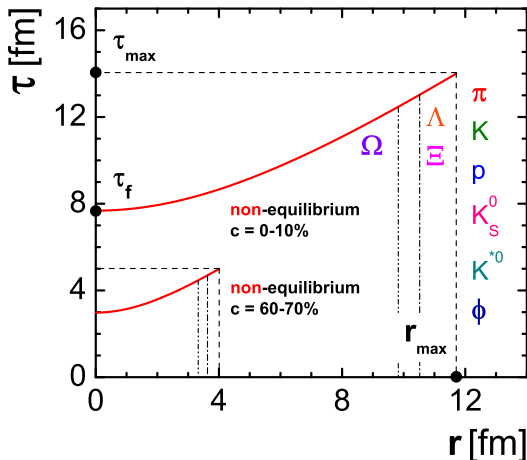
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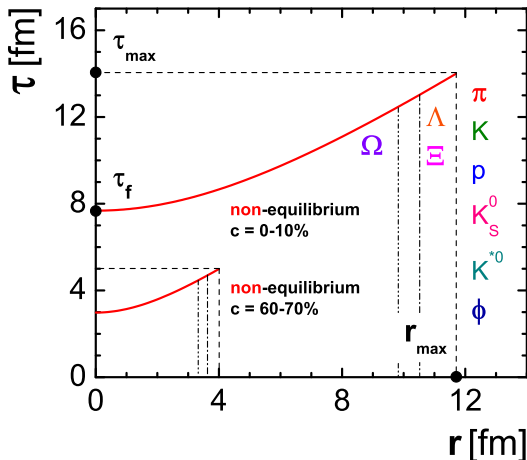
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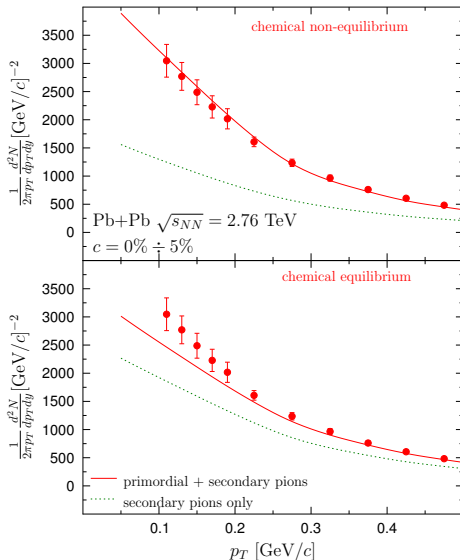
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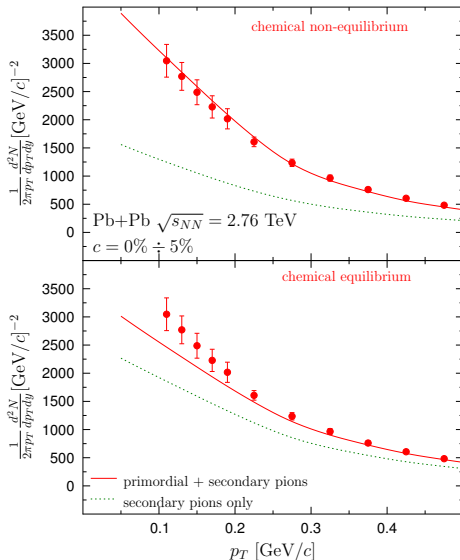
Pion condensation?

- ▶ The **low p_T** enhancement of **pions** can be explained only in **non-equilibrium**
- ▶ The value of γ_q that we use is equivalent to the pion chemical potential
 $\mu_{\pi} = 2T \ln \gamma_q \simeq 134$ MeV, which is very close to the π^0 mass, $m_{\pi^0} \simeq 134.98$



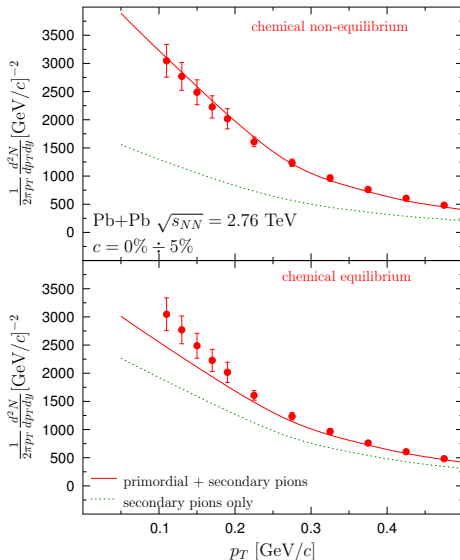
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Conclusions:

- ▶ We **connect** the **proton anomaly** with the **pion enhancement** effect and show that the two problems may be **solved** naturally within the **non-equilibrium Cracow single freeze-out** model
- ▶ The obtained values of the non-equilibrium parameter γ_q are close to the **pion condensation limit** $(\gamma_q^{cond})^2 = e^{m_\pi/T}$
- ▶ It may be interpreted as a signature of the **onset** of **pion condensation** in ultra-relativistic heavy-ion collisions at **LHC**.

Extra Slides

