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Axions

Motivation, Cosmological Role
and Experimental Searches

52nd Cracow School on Theoretical Physics

Zakopane, Tatra Mountains, Poland, 19–27 May 2012

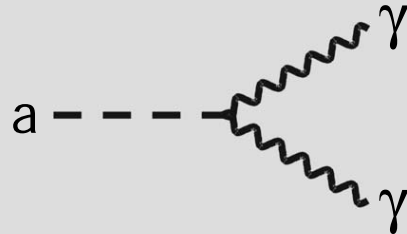
Axion Physics in a Nut Shell

Particle-Physics Motivation

CP conservation in QCD by
Peccei-Quinn mechanism

→ Axions $a \sim \pi^0$

$$m_\pi f_\pi \approx m_a f_a$$



For $f_a \gg f_\pi$ axions are “invisible”
and very light

Solar and Stellar Axions

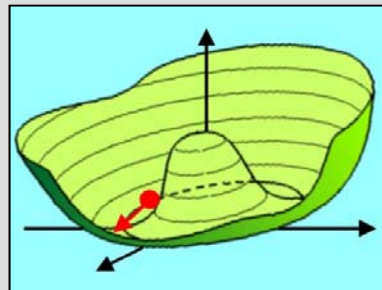
Axions thermally produced in stars,
e.g. by Primakoff production



- Limits from avoiding excessive energy drain
- Solar axion searches (CAST, Sumico)

Cosmology

In spite of small mass, axions are born
non-relativistically
(non-thermal relics)



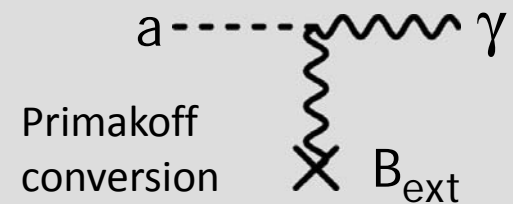
Cold dark matter
candidate

$m_a \sim 10 \mu\text{eV}$ (or much smaller or larger)

Search for Axion Dark Matter



Microwave resonator
(1 GHz = 4 μeV)



ADMX-LF (UW Seattle)
ADMX-HF (Yale)

CP Violation in Particle Physics

Discrete symmetries in particle physics

- C – Charge conjugation, transforms particles to antiparticles
violated by weak interactions
- P – Parity, changes left-handedness to right-handedness
violated by weak interactions
- T – Time reversal, changes direction of motion (forward to backward)
- CPT – exactly conserved in quantum field theory
- CP – conserved by all gauge interactions
violated by three-flavor quark mixing matrix



Physics Nobel Prize 2008

- ❖ All measured CP-violating effects derive from a single phase in the quark mass matrix (Kobayashi-Maskawa phase), i.e. from complex Yukawa couplings
- ❖ Cosmic matter-antimatter asymmetry requires new ingredients

The CP Problem of Strong Interactions

$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{\psi}_q (iD - \underbrace{m_q}_{\text{Real quark mass}} e^{i\theta_q} \underbrace{)}_{\text{Phase from Yukawa coupling}} \psi_q - \frac{1}{4} G_{\mu\nu a} G_a^{\mu\nu} - \underbrace{\bar{\Theta}}_{\text{Angle variable}} \frac{\alpha_s}{8\pi} \underbrace{G_{\mu\nu a} \tilde{G}_a^{\mu\nu}}_{\text{CP-odd quantity} \sim \mathbf{E} \cdot \mathbf{B}}$$

Remove phase of mass term by chiral transformation of quark fields

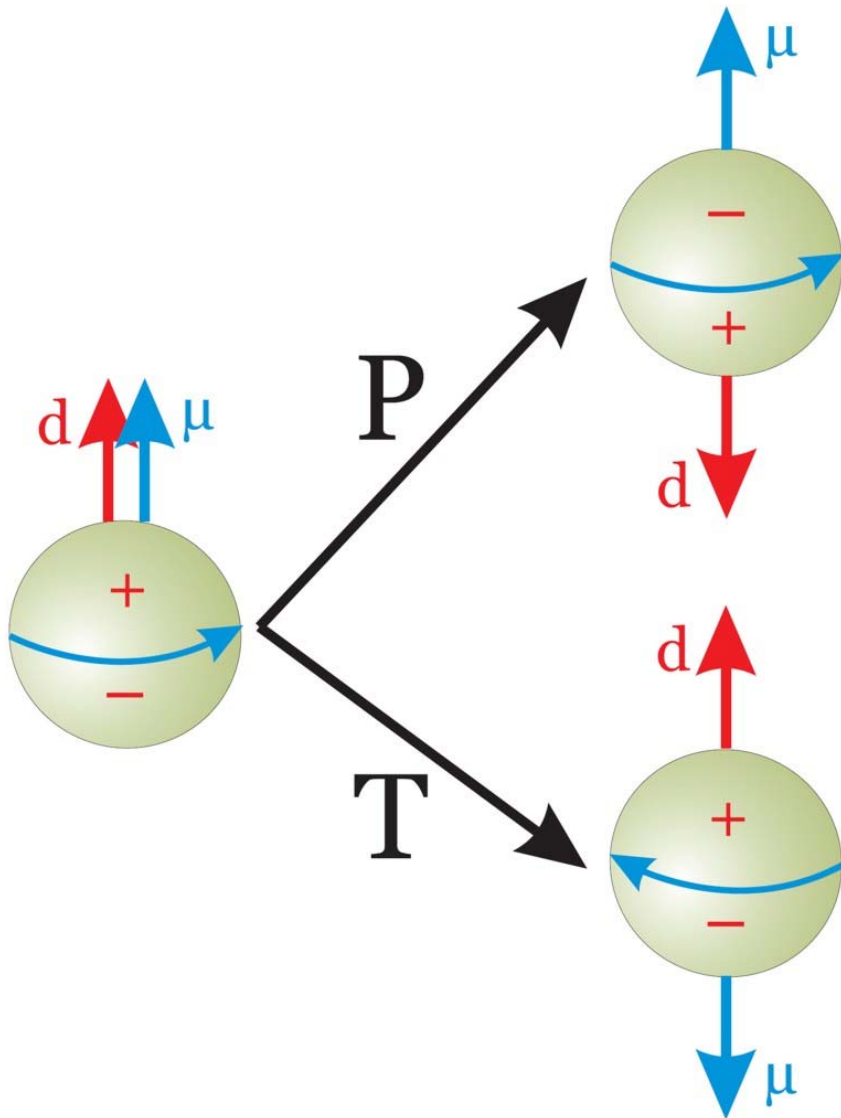
$$\psi_q \rightarrow e^{-i\gamma_5 \theta_q / 2} \psi_q$$

$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{\psi}_q (iD - m_q) \psi_q - \frac{1}{4} GG - \underbrace{(\bar{\Theta} - \arg \det M_q)}_{-\pi \leq \bar{\Theta} \leq +\pi} \frac{\alpha_s}{8\pi} G \tilde{G}$$

- ❖ $\bar{\Theta}$ can be traded between quark phases and $G\tilde{G}$ term
- ❖ No physical impact if at least one $m_q = 0$

Experimental limits: $|\bar{\Theta}| < 10^{-11}$ Why so small?

Neutron Electric Dipole Moment



Violates time reversal (T) and space reflection (P) symmetries

Natural scale

$$\frac{e}{2m_N} = 1.06 \times 10^{-14} e \text{ cm}$$

Experimental limit

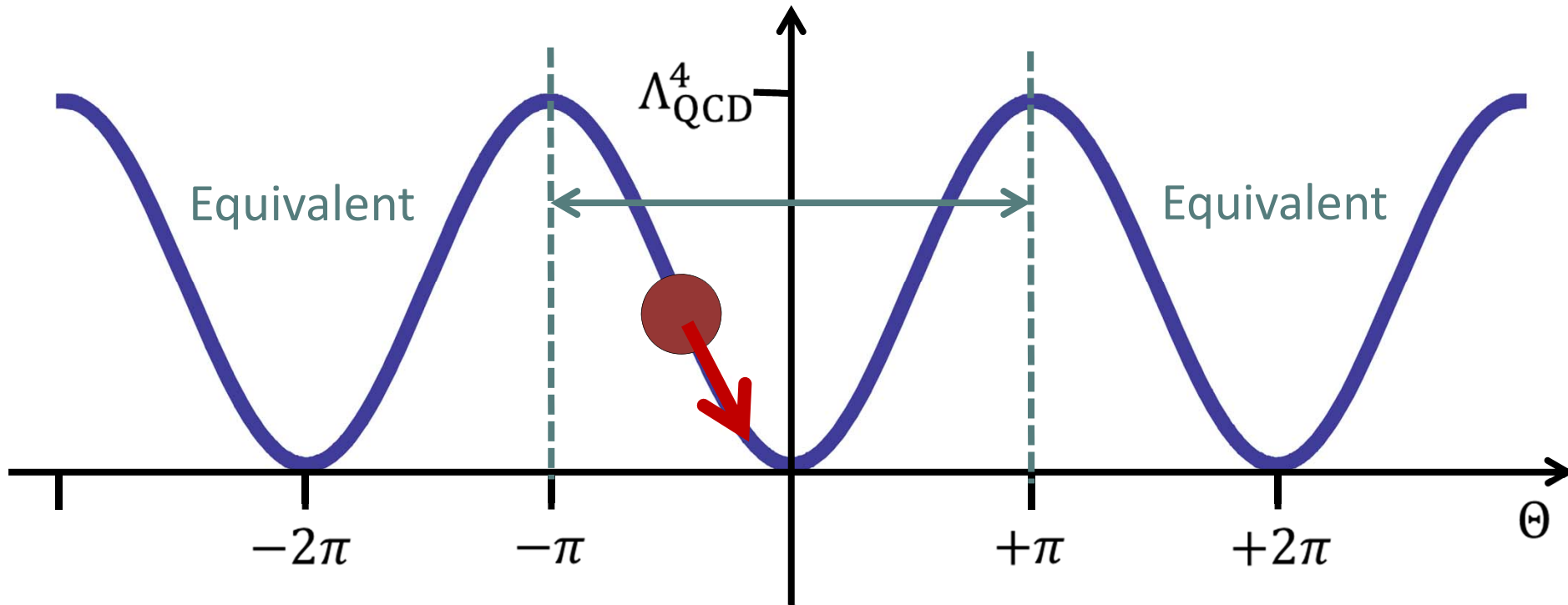
$$|d| < 0.63 \times 10^{-25} e \text{ cm}$$

Limit on coefficient

$$\bar{\Theta} \frac{m_q}{m_N} \lesssim 10^{-11}$$

Strong CP Problem

QCD vacuum energy $V(\Theta)$



- CP conserving vacuum has $\Theta = 0$ (Vafa and Witten 1984)
- QCD could have any $-\pi \leq \Theta \leq +\pi$, is “constant of nature”
- Energy can not be minimized: Θ not dynamical

Peccei-Quinn solution:

Make Θ dynamical, let system relax to lowest energy

Dynamical Solution

Peccei & Quinn 1977, Wilczek 1978, Weinberg 1978

- Re-interpret $\bar{\Theta}$ as a dynamical variable (scalar field)

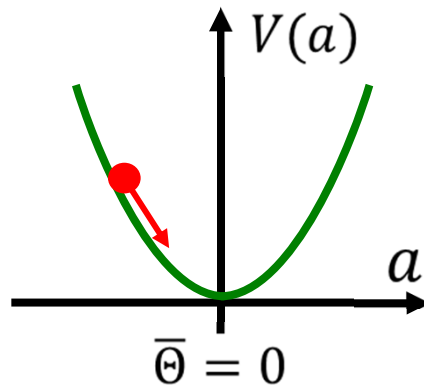
$$\mathcal{L}_{\text{CP}} = -\frac{\alpha_s}{8\pi} \bar{\Theta} \text{Tr}(G\tilde{G}) \rightarrow -\frac{\alpha_s}{8\pi} \frac{a(x)}{f_a} \text{Tr}(G\tilde{G})$$

$a(x)$ is pseudoscalar axion field, f_a axion decay constant (Peccei-Quinn scale)

- Axions generically couple to two gluons and mix with, π^0 , η , η' mesons, inducing a mass (potential) for $a(x)$

$$m_a f_a = \frac{\sqrt{m_u m_d}}{m_u + m_d} m_\pi f_\pi \quad \left(\begin{array}{l} \text{Axion mass} \\ \text{\& couplings} \end{array} \right) \sim \left(\begin{array}{l} \text{Pion mass} \\ \text{\& couplings} \end{array} \right) \times \frac{f_\pi}{f_a}$$

- Potential (mass term) induced by \mathcal{L}_{CP} drives $a(x)$ to CP-conserving minimum



CP-symmetry
dynamically
restored

35 Years of Axions

VOLUME 40, NUMBER 4

PHYSICAL REVIEW LETTERS

23 JANUARY 1978

A New Light Boson?

Steven Weinberg

Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138

(Received 6 December 1977)

It is pointed out that a global $U(1)$ symmetry, that has been introduced in order to preserve the parity and time-reversal invariance of strong interactions despite the effects of instantons, would lead to a neutral pseudoscalar boson, the "axion," with mass roughly of order 100 keV to 1 MeV. Experimental implications are discussed.

VOLUME 40, NUMBER 5

PHYSICAL REVIEW LETTERS

30 JANUARY 1978

Problem of Strong P and T Invariance in the Presence of Instantons

F. Wilczek^(a)

Columbia University, New York, New York 10027, and The Institute for Advanced Studies, Princeton, New Jersey 08540^(b)

(Received 29 November 1977)

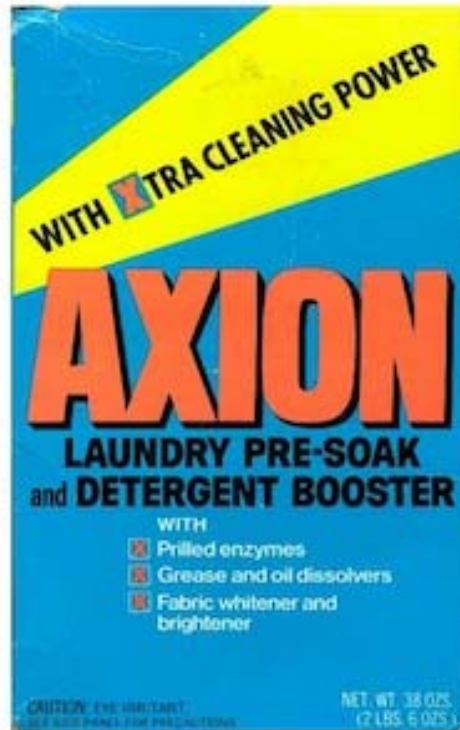
The requirement that P and T be approximately conserved in the color gauge theory of strong interactions without arbitrary adjustment of parameters is analyzed. Several possibilities are identified, including one which would give a remarkable new kind of very light, long-lived pseudoscalar boson.

One of the main advantages of the color gauge theory of strong interactions is that so many of the observed symmetries of strong interactions seem to follow automatically as a consequence of the gauge principle and renormalizability— P , T , C , flavor conservation, the $3 \oplus 3^*$ structure of chi-

a certain class of theories^{4,5,7} the parameter θ is physically meaningless,^{4,5} or dynamically determined.⁷ In this case, if the strong interaction conserves P and T , we shall say the conservation is *automatic*.

I regard a theory of type (i) as very unattrac-

The Cleansing Axion

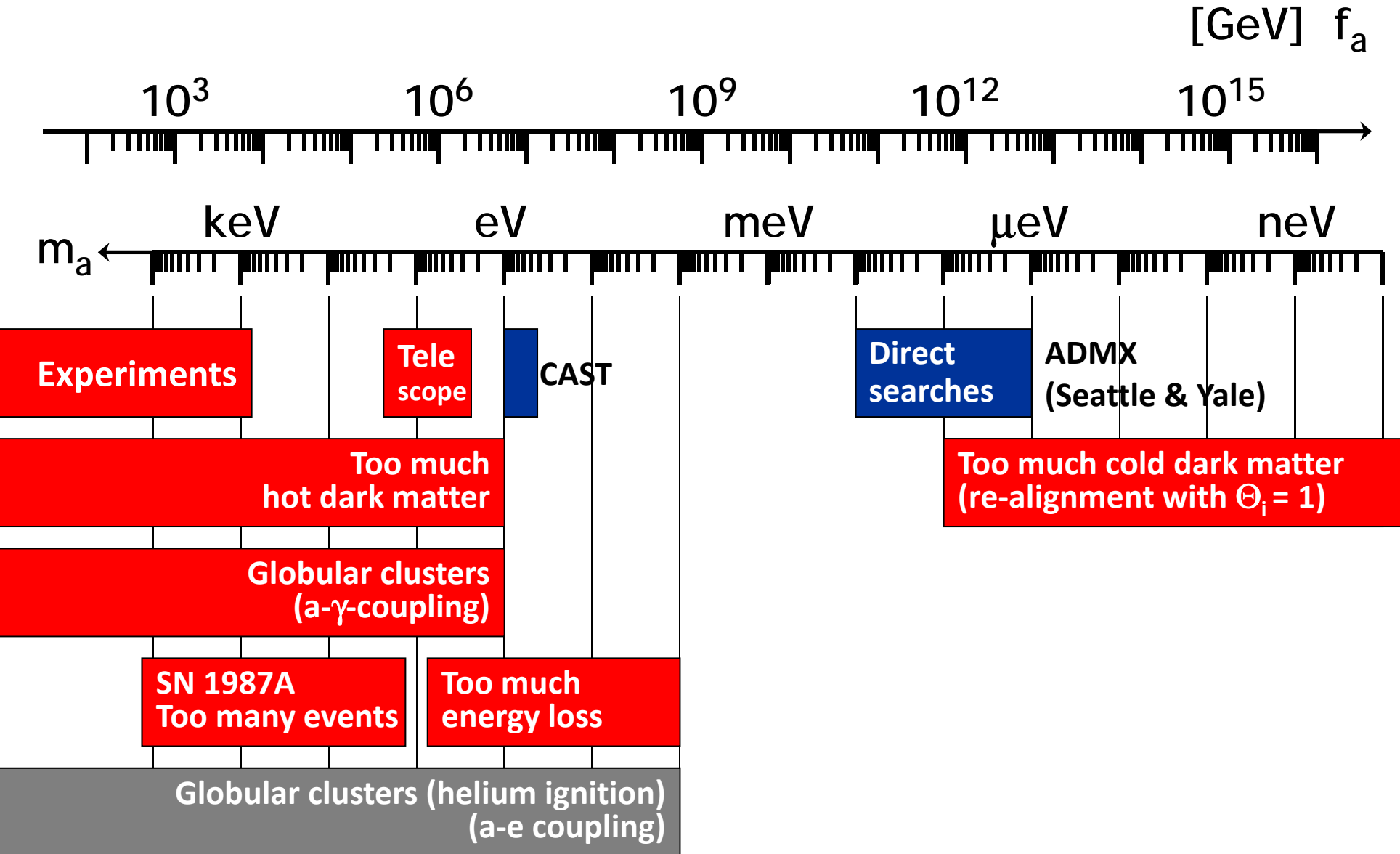


Frank Wilczek



**“I named them after a laundry detergent, since they clean up a problem with an axial current.”
(Nobel lecture 2004)**

Axion Bounds and Searches



A group of approximately 20 people, likely scientists and engineers, are standing in a large industrial facility. They are positioned in front of a large, blue cylindrical detector labeled 'CAST'. The detector is mounted on a green structure and is supported by a yellow A-frame crane. The facility has a high ceiling with industrial lighting and various pipes and equipment visible. The text 'Searching for Axion-Like Particles' is overlaid in large white font across the center of the image.

Searching for Axion-Like Particles

Experimental Tests of the “Invisible” Axion

P. Sikivie

Physics Department, University of Florida, Gainesville, Florida 32611

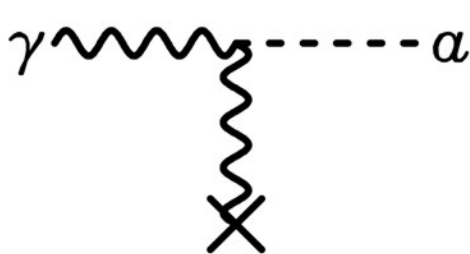
(Received 13 July 1983)

Experiments are proposed which address the question of the existence of the “invisible” axion for the whole allowed range of the axion decay constant. These experiments exploit the coupling of the axion to the electromagnetic field, axion emission by the sun, and/or the cosmological abundance and presumed clustering of axions in the halo of our galaxy.

Primakoff effect:

Axion-photon transition in external static E or B field

(Originally discussed for π^0 by Henri Primakoff 1951)

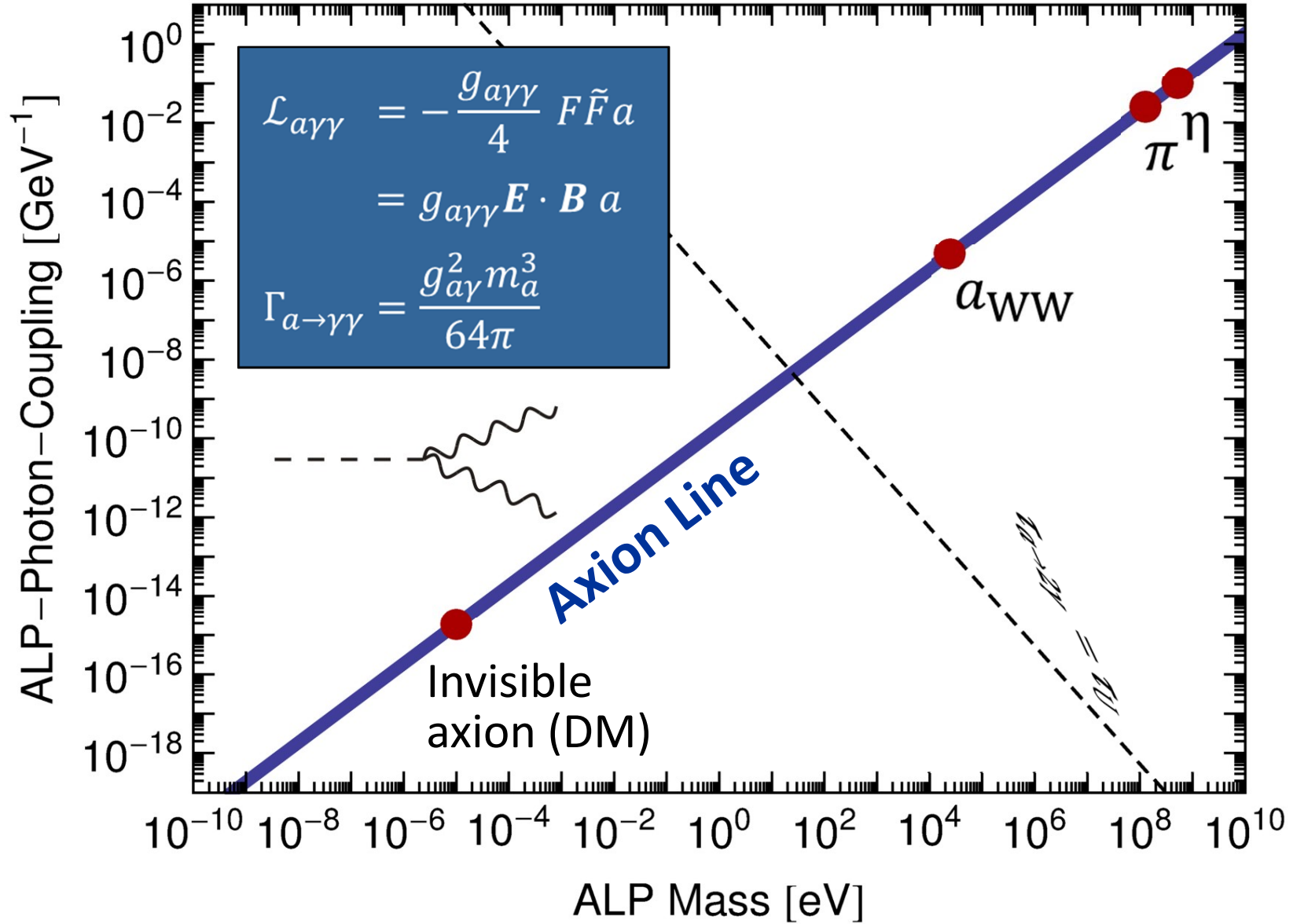


Pierre Sikivie:

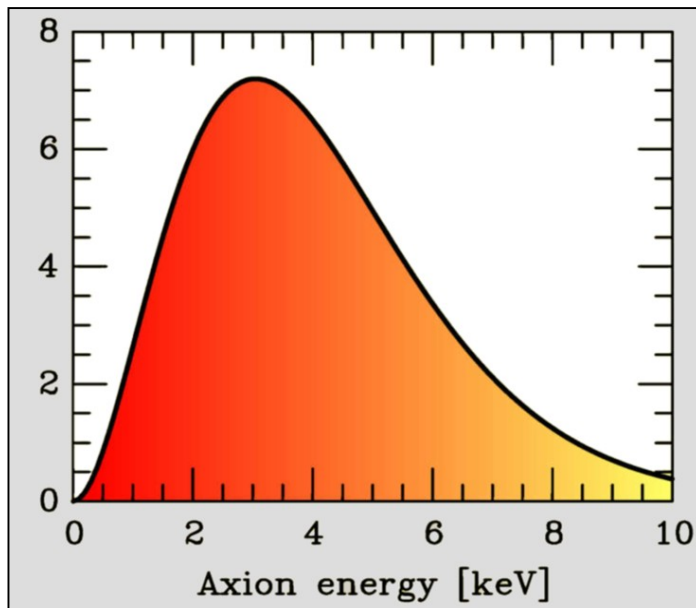
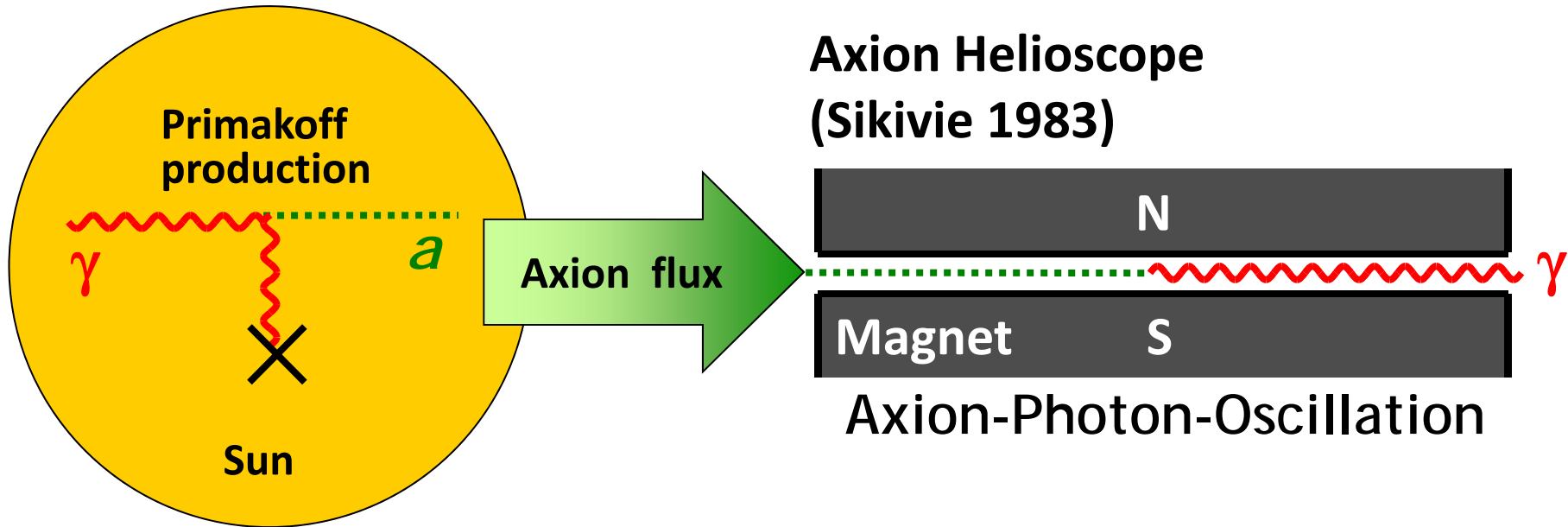
Macroscopic B-field can provide a large coherent transition rate over a big volume (low-mass axions)

- Axion helioscope:
Look at the Sun through a dipole magnet
- Axion haloscope:
Look for dark-matter axions with
A microwave resonant cavity

Parameter Space for Axion-Like Particles (ALPs)



Search for Solar Axions



Axion Helioscope (Sikivie 1983)

Axion-Photon-Oscillation

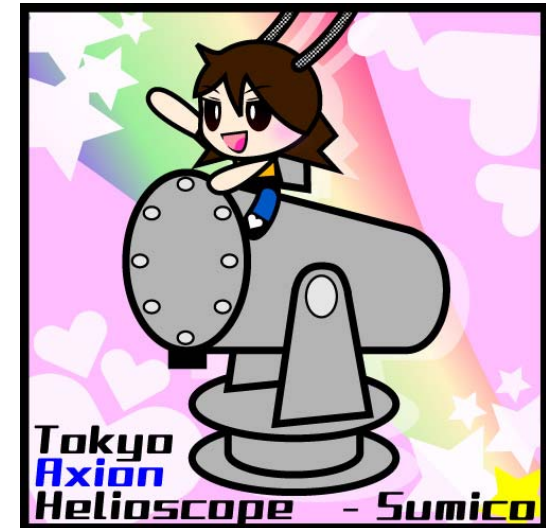
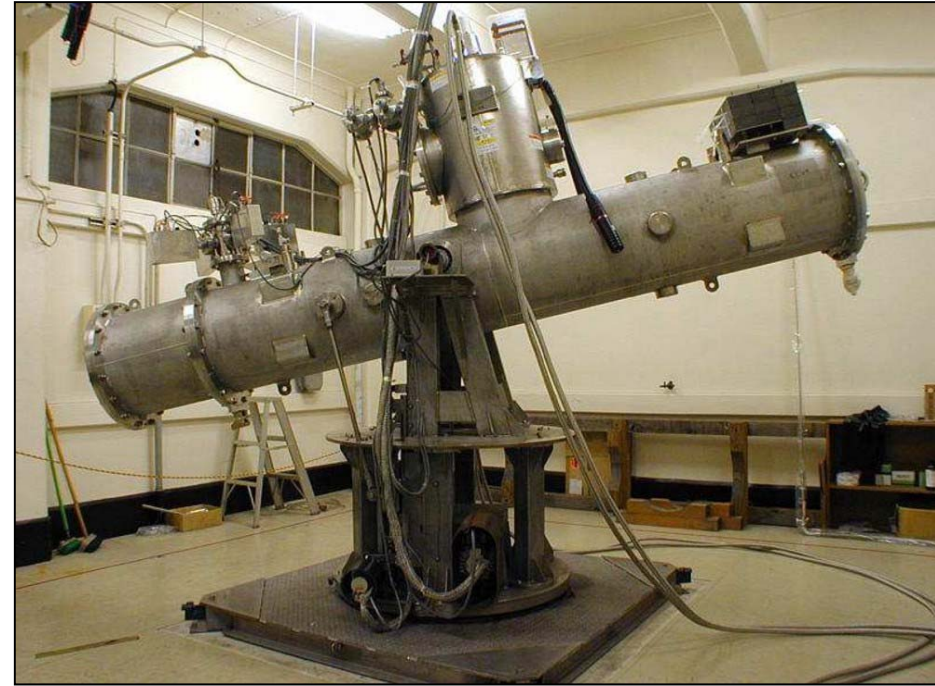
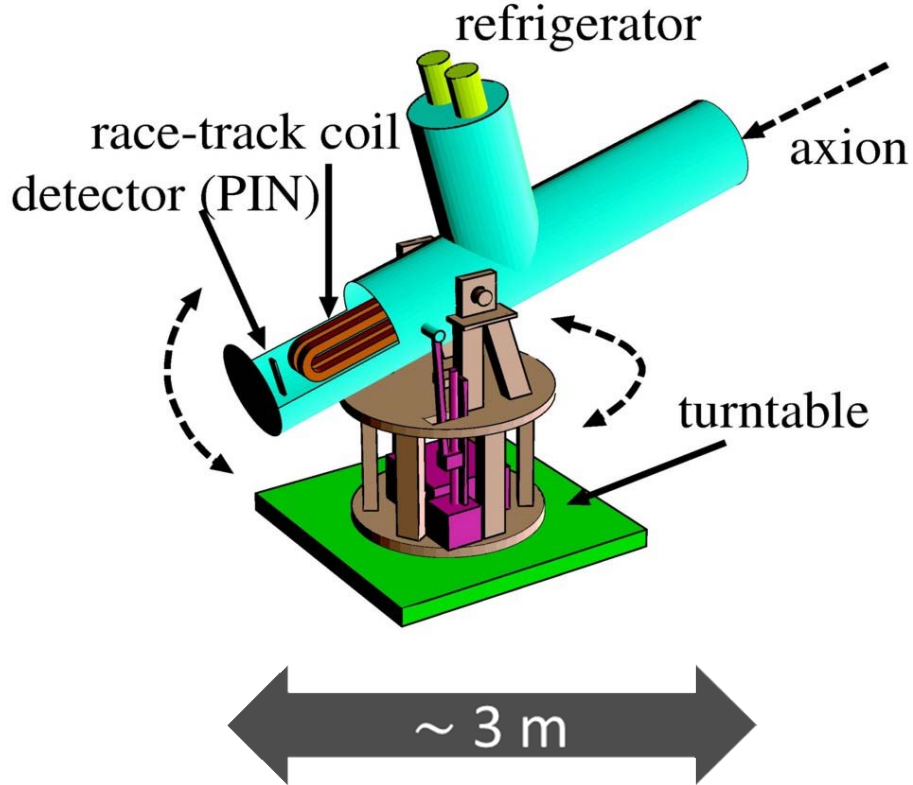
- Tokyo Axion Helioscope ("Sumico")
(Results since 1998, up again 2008)
- CERN Axion Solar Telescope (CAST)
(Data since 2003)

Alternative technique:

Bragg conversion in crystal

Experimental limits on solar axion flux
from dark-matter experiments
(SOLAX, COSME, DAMA, CDMS ...)

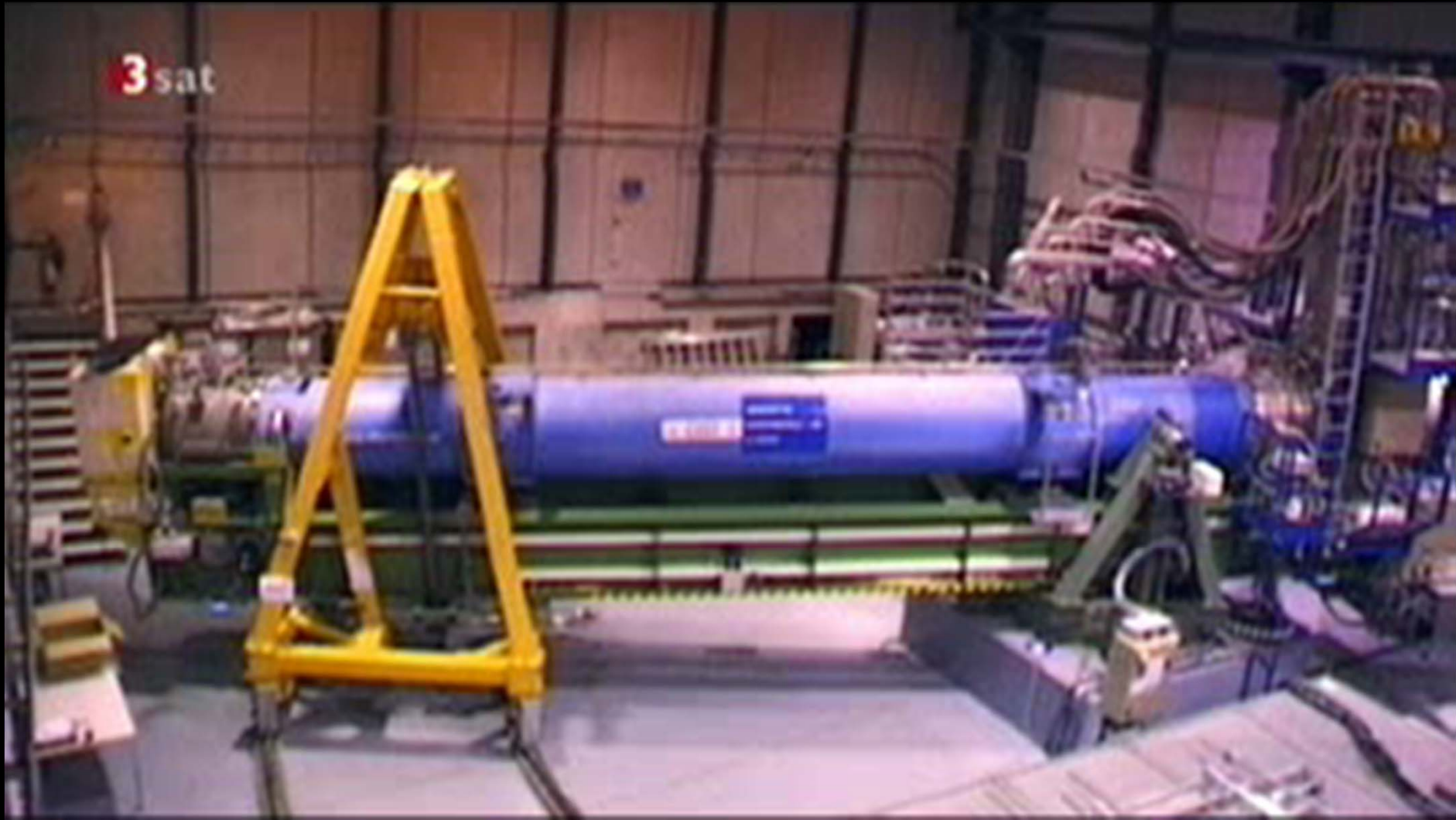
Tokyo Axion Helioscope ("Sumico")



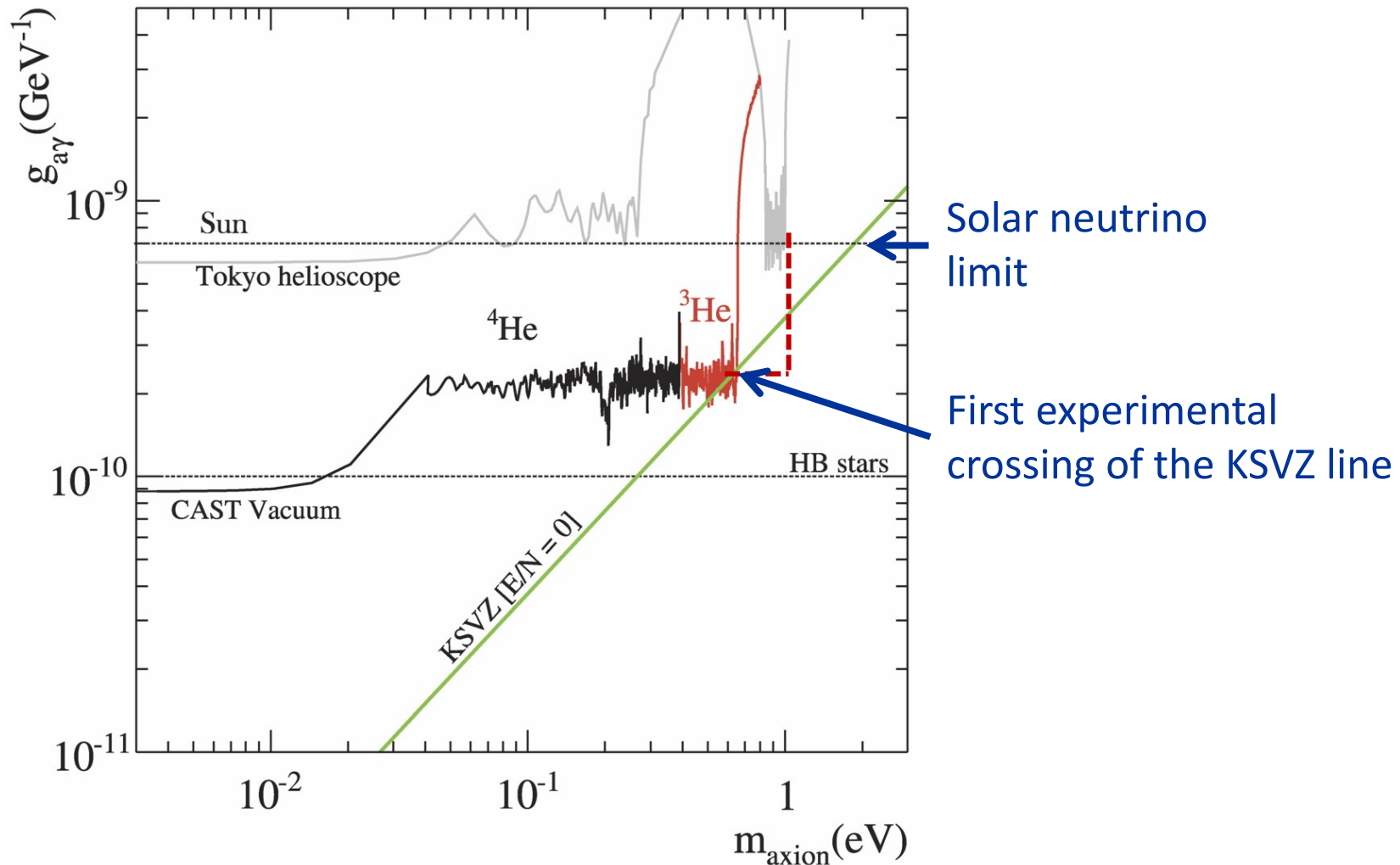
Moriyama, Minowa, Namba, Inoue, Takasu & Yamamoto
PLB 434 (1998) 147

Inoue, Akimoto, Ohta, Mizumoto, Yamamoto & Minowa
PLB 668 (2008) 93

CAST at CERN



Helioscope Limits



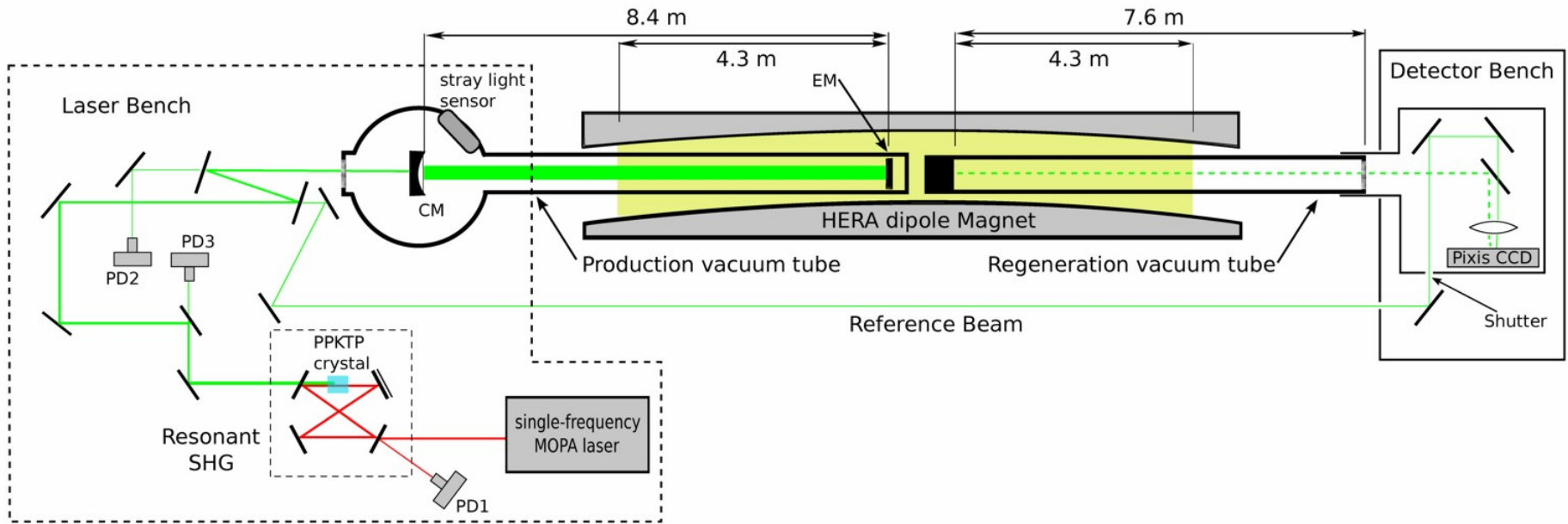
CAST-I results: PRL 94:121301 (2005) and JCAP 0704 (2007) 010

CAST-II results (He-4 filling): JCAP 0902 (2009) 008

CAST-II results (He-3 filling, range 1): PRL 107 (2011) 261302

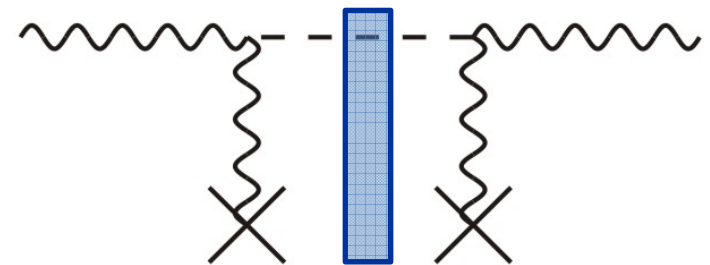
Photon Regeneration Experiments

Ehret et al. (ALPS Collaboration), arXiv:1004.1313

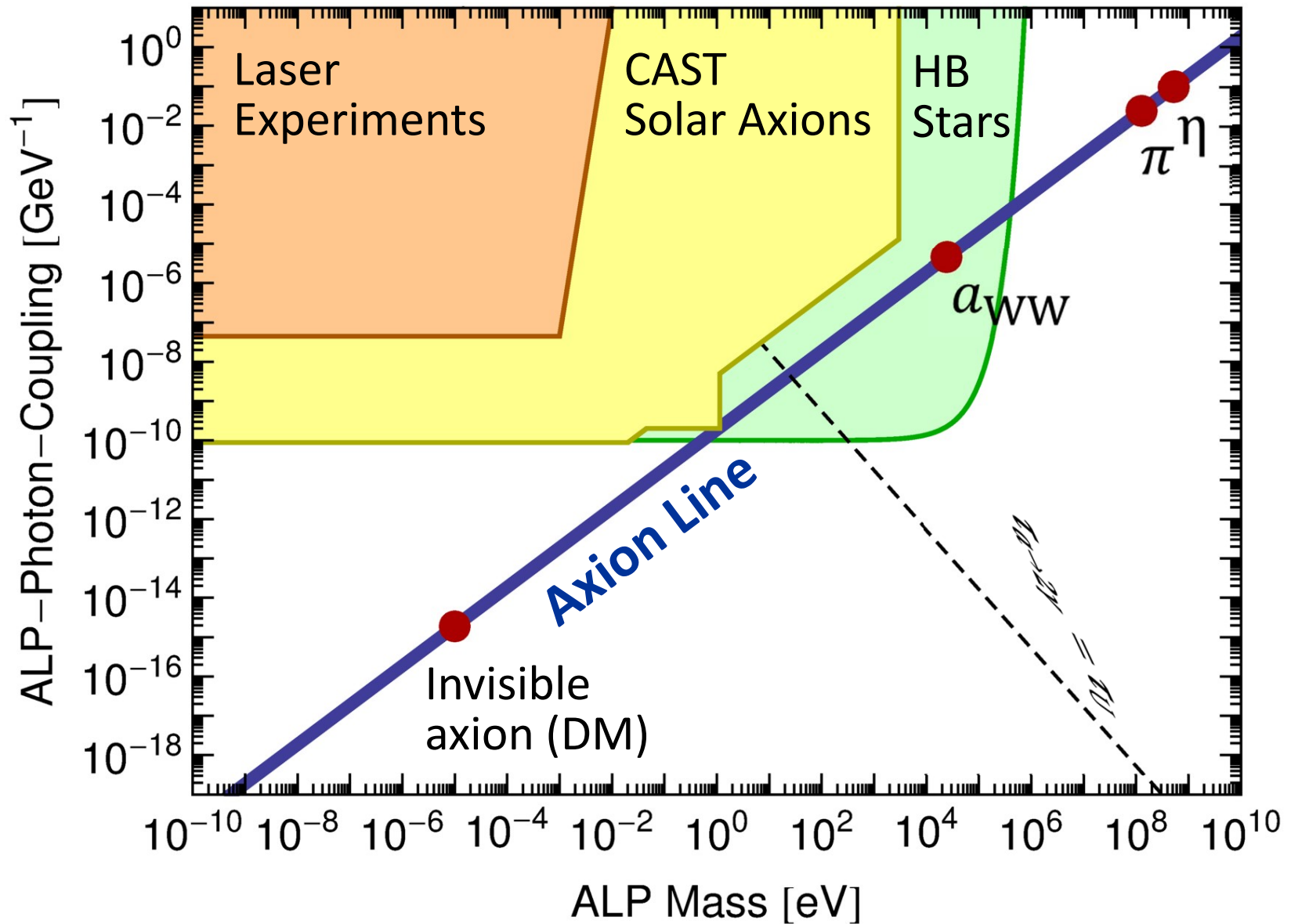


Recent “shining-light-through-a-wall” or vacuum birefringence experiments:

- ALPS (DESY, using HERA dipole magnet)
- BMV (Laboratoire National des Champs Magnétiques Intens, Toulouse)
- BFRT (Brookhaven, 1993)
- GammeV (Fermilab)
- LIPPS (Jefferson Lab)
- OSQAR (CERN, using LHC dipole magnets)
- PVLAS (INFN Trieste)



Parameter Space for Axion-Like Particles



Shining TeV Gamma Rays through the Universe

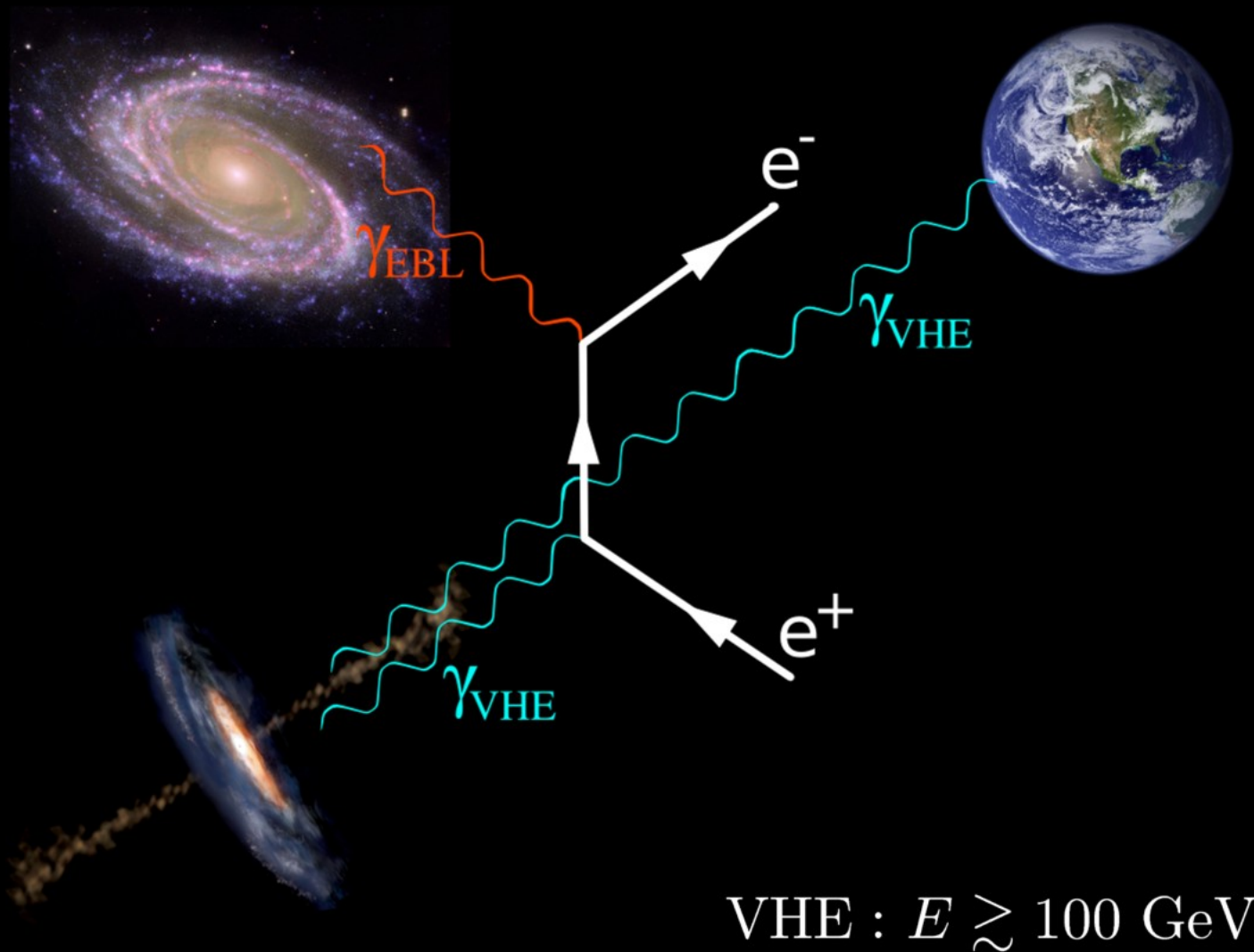


Figure from a talk by Manuel Meyer (Univ. Hamburg)

Shining TeV Gamma Rays through the Universe

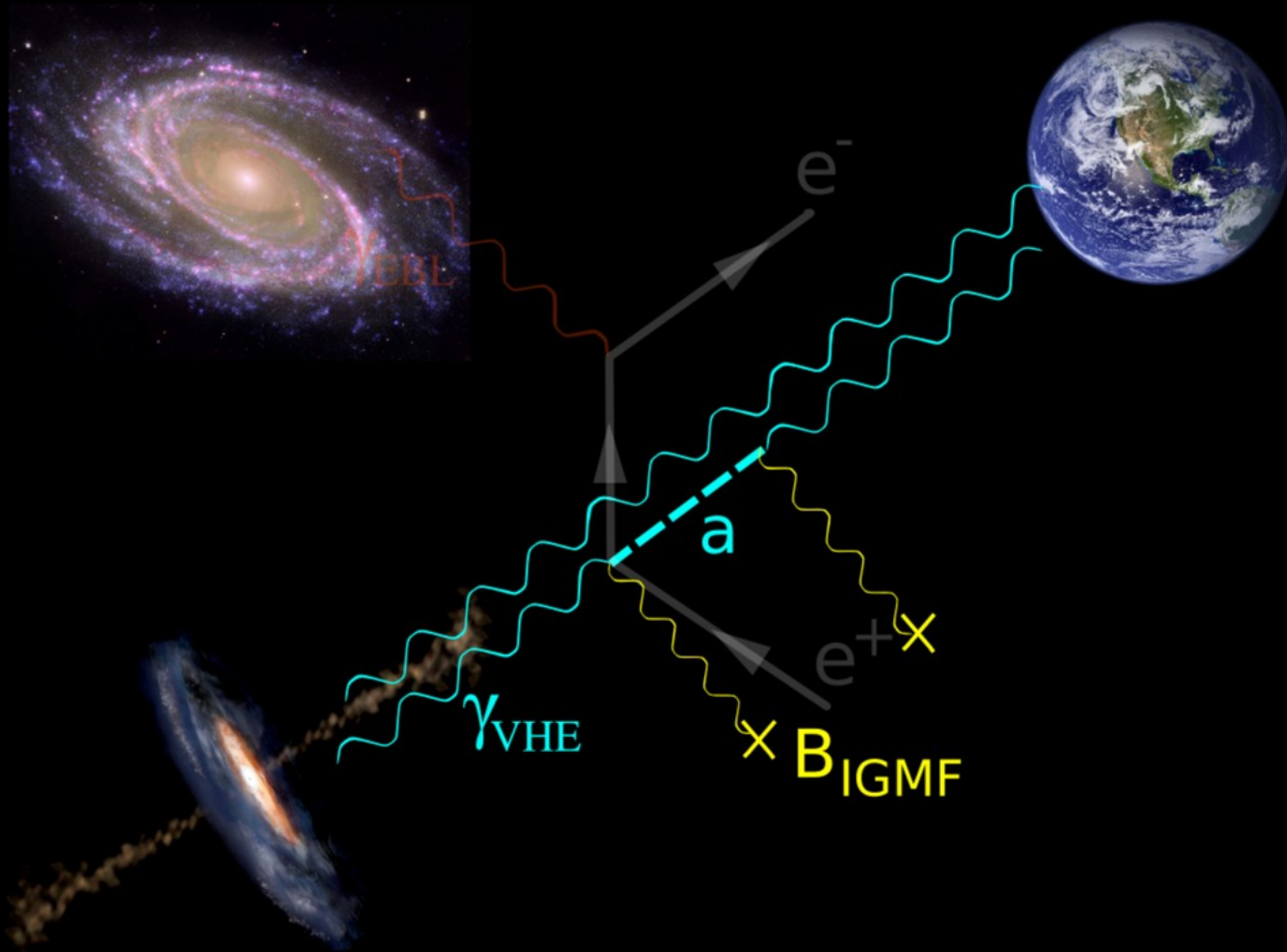
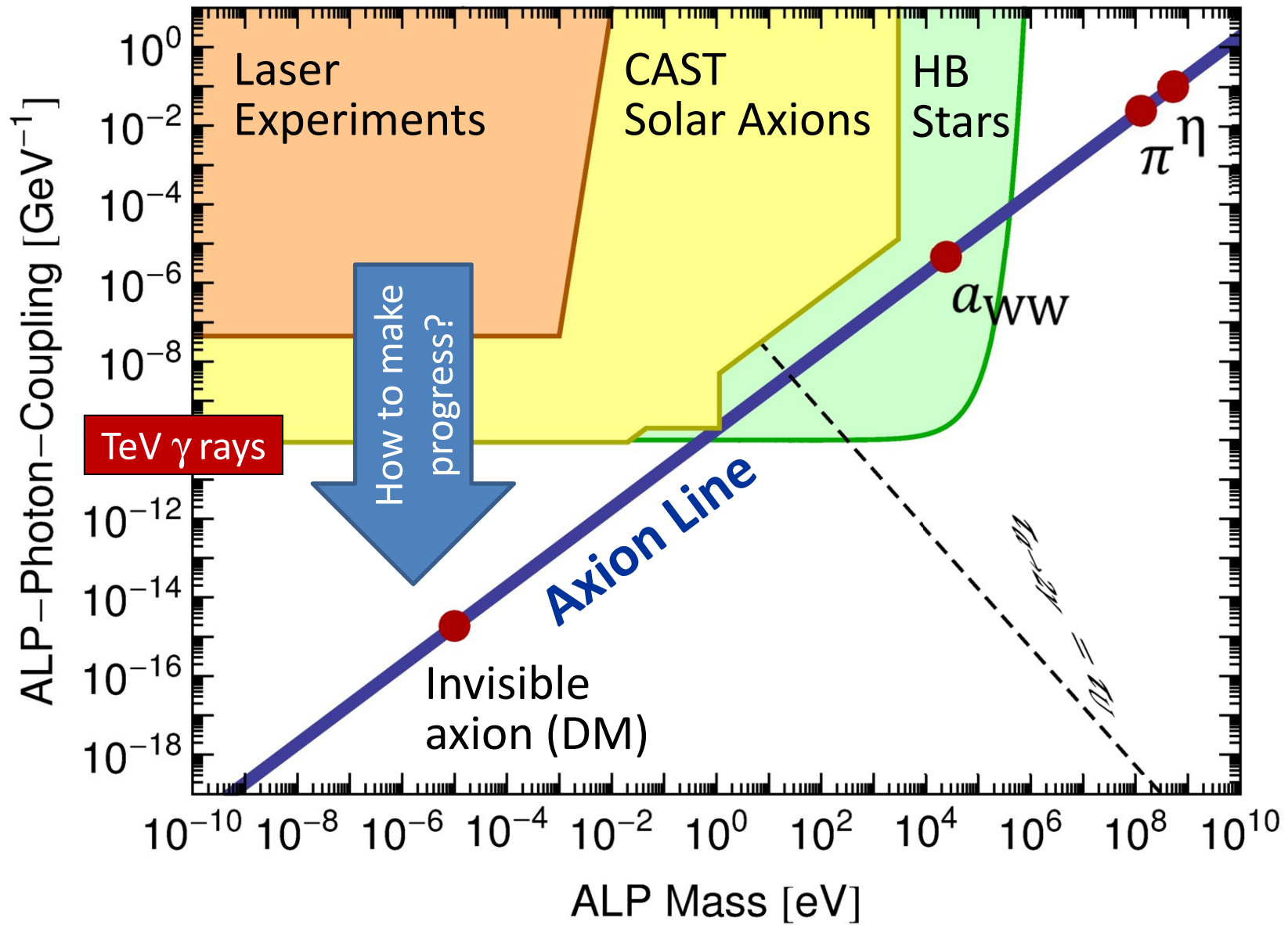
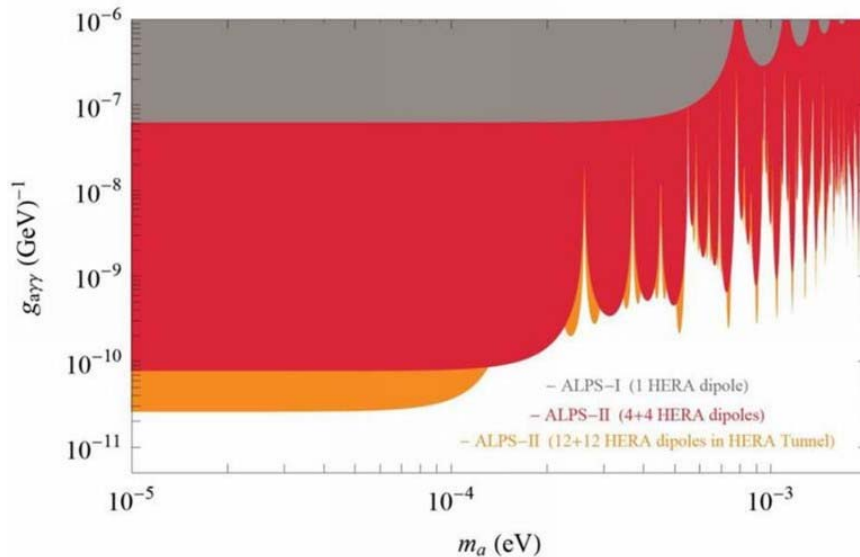


Figure from a talk by Manuel Meyer (Univ. Hamburg)

Parameter Space for Axion-Like Particles



Perspectives for ALPS-II (DESY)



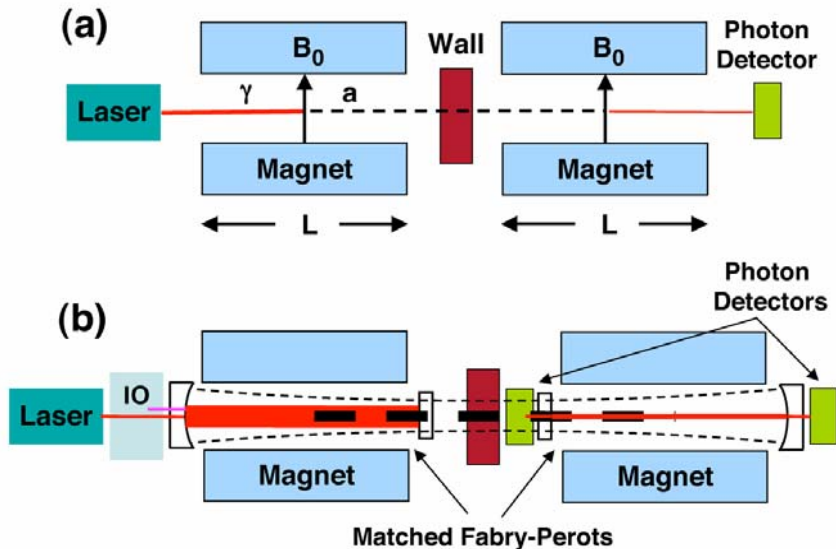
Photon regeneration experiment with 12+12 HERA dipoles

- May reach $10^{-11} \text{ GeV}^{-1}$ level

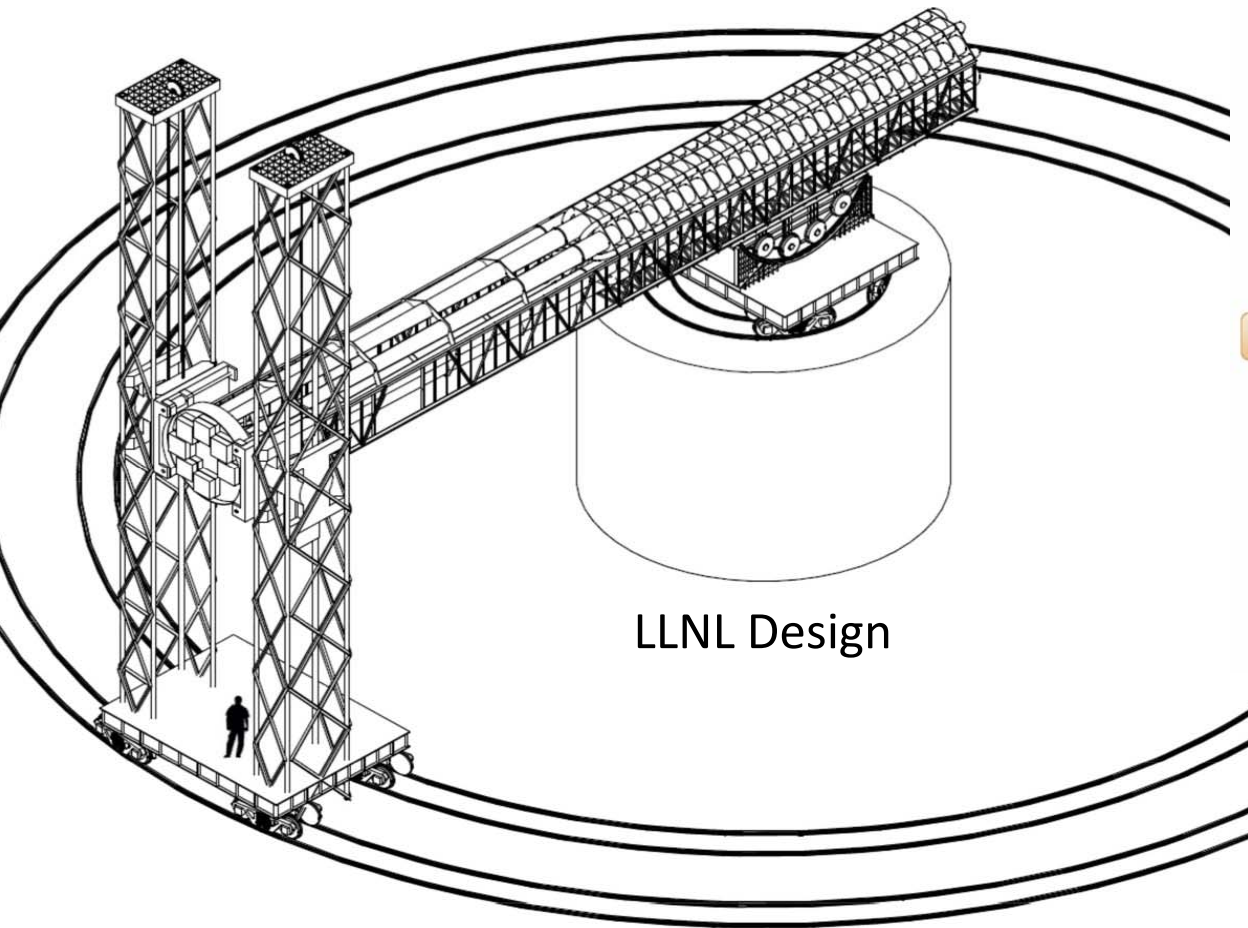
Challenges

- Optical system
- Getting dipoles straight
- Detectors
- Running a 260 m long system (decision 2015)

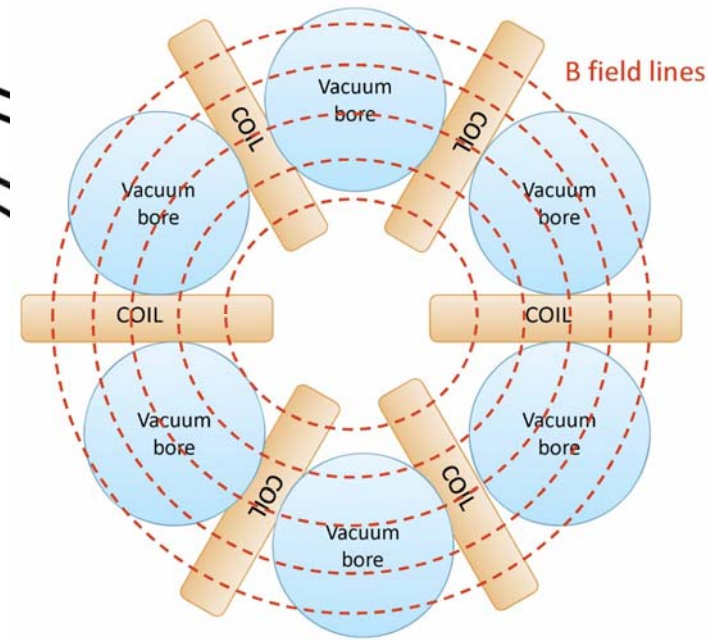
(Axel Lindner and Andreas Ringwald
PIs at DESY)



Next Generation Axion Helioscope (IAXO)



LLNL Design

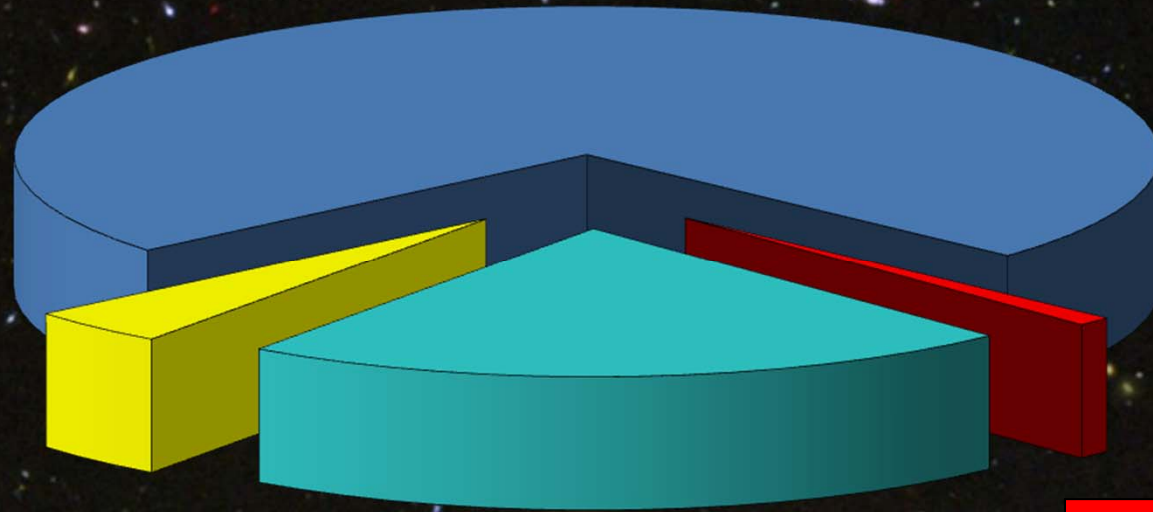


- Need new magnet with
- Much bigger aperture:
~1 m² per bore
- Lighter (no iron yoke)
- Bores at room temperature

Irastorza et al., “Towards a new generation axion helioscope”, arXiv:1103.5334

Axions as Cold Dark Matter of the Universe

Dark Energy 73%
(Cosmological Constant)



Ordinary Matter 4%
(of this only about 10% luminous)

Dark Matter 23%

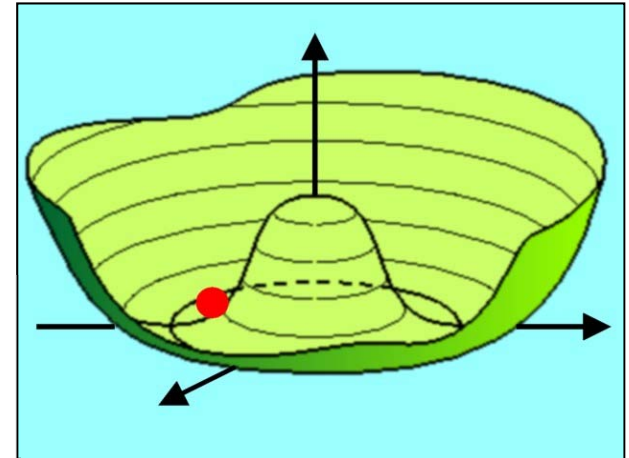
Neutrinos 0.1-2%

Axion as a Nambu-Goldstone Boson

$$\mathcal{L}_{\text{CP}} = \frac{\alpha_s}{8\pi} \bar{\psi} G_a \tilde{G}_a \rightarrow \frac{\alpha_s}{8\pi} \underbrace{\left(\bar{\psi} - \frac{a(x)}{f_a} \right)}_{\text{Periodic variable (angle)}} G_a \tilde{G}_a$$

Periodic variable (angle)

$$\Phi = \frac{f_a + \rho(x)}{\sqrt{2}} e^{i \frac{a(x)}{f_a}}$$



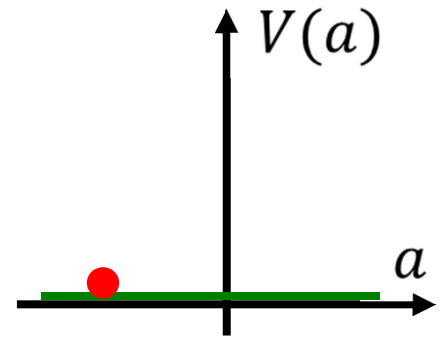
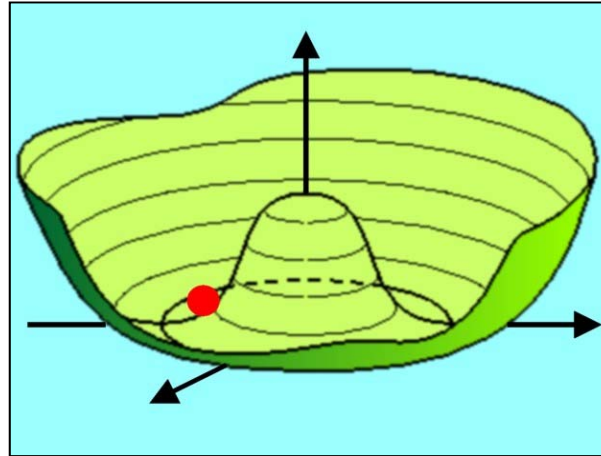
- New U(1) symmetry, spontaneously broken at a large scale f_a
- Axion is “phase” of new Higgs field: angular variable $a(x)/f_a$
- By construction couples to $G\tilde{G}$ term with strength $\alpha_s/8\pi$, e.g. triangle loop with new heavy quark (KSVZ model)
- Mixes with π^0 - η - η' mesons
- Axion mass
(vanishes if m_u or $m_d = 0$)

$$m_a = \frac{\sqrt{m_u m_d}}{m_u + m_d} \frac{m_\pi}{f_\pi f_a}$$

Creation of Cosmological Axions

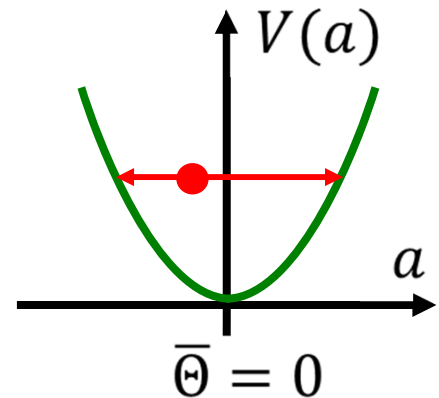
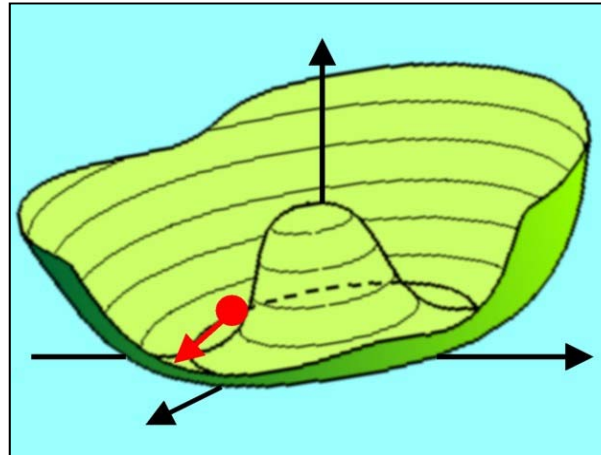
$T \sim f_a$ (very early universe)

- $U_{PQ}(1)$ spontaneously broken
- Higgs field settles in “Mexican hat”
- Axion field sits fixed at $a_i = \Theta_i f_a$



$T \sim 1 \text{ GeV}$ ($H \sim 10^{-9} \text{ eV}$)

- Axion mass turns on quickly by thermal instanton gas
- Field starts oscillating when $m_a \gtrsim 3H$
- Classical field oscillations (axions at rest)



Axions are born as nonrelativistic, classical field oscillations
Very small mass, yet cold dark matter

Axion Cosmology in PLB 120 (1983)

THE NOT-SO-HARMLESS AXION

Michael DINE

The Institute for Advanced Study, Princeton, NJ 08540, USA

and

Willy FISCHLER

Department of Physics

Received 17 September 1982

Received manuscript

Cosmological aspects discussed by Sikivie is needed to give an upper bound

A COSMOLOGICAL BOUND ON THE INVISIBLE AXION

L.F. ABBOTT ¹

Physics Department, Brandeis University, Waltham, MA 02254, USA

and

P. SIKIVIE ²

Particle Theory

Received 14 September 1982

The production of axions with mass $m_a \lesssim 10^{-5}$ GeV are found

COSMOLOGY OF THE INVISIBLE AXION

John PRESKILL ¹, Mark B. WISE ²

Lyman Laboratory of Physics, Harvard University, Cambridge, MA 02138, USA

and

Frank WILCZEK

Institute for Theoretical Physics, University of California, Santa Barbara, CA 93106, USA

Received 10 September 1982

We identify a new cosmological problem for models which solve the strong CP puzzle with an invisible axion, unrelated to the domain wall problem. Because the axion is very weakly coupled, the energy density stored in the oscillations of the classical axion field does not dissipate rapidly; it exceeds the critical density needed to close the universe unless $f_a \lesssim 10^{12}$ GeV, where f_a is the axion decay constant. If this bound is saturated, axions may comprise the dark matter of the universe.

Cosmic Axion Density

Modern values for QCD parameters and temperature-dependent axion mass imply (Bae, Huh & Kim, arXiv:0806.0497)

$$\Omega_a h^2 = 0.195 \Theta_i^2 \left(\frac{f_a}{10^{12} \text{GeV}} \right)^{1.184} = 0.105 \Theta_i^2 \left(\frac{10 \mu\text{eV}}{m_a} \right)^{1.184}$$

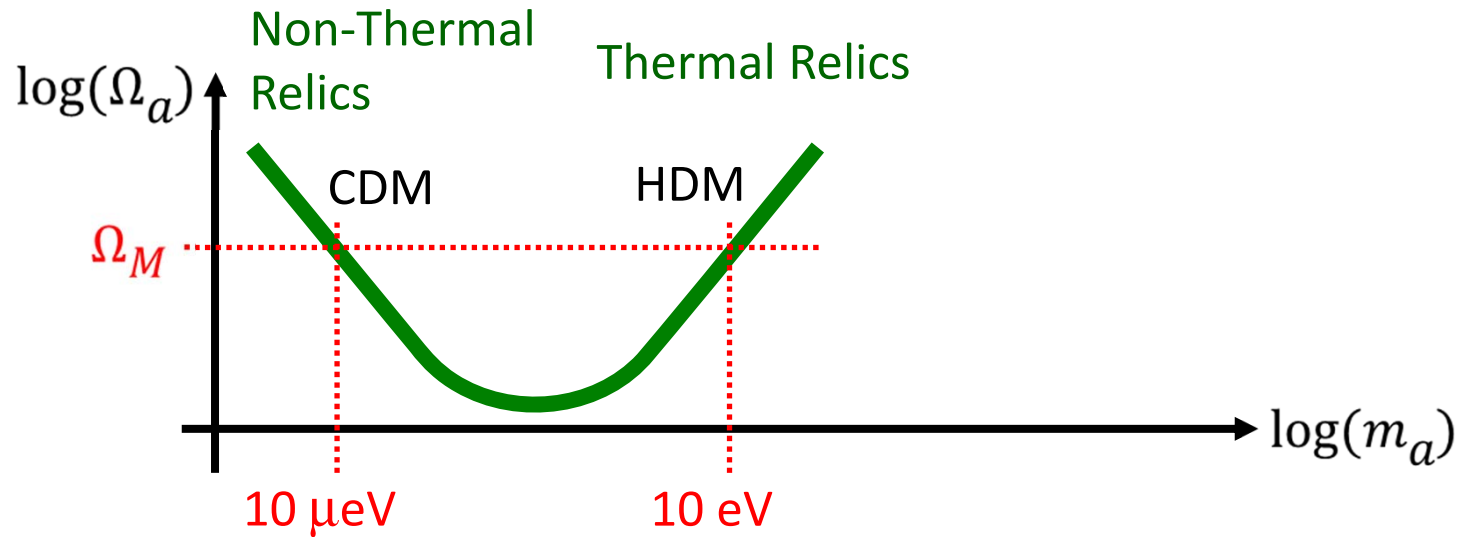
If axions provide the cold dark matter: $\Omega_a h^2 = 0.11$

$$\Theta_i = 0.75 \left(\frac{10^{12} \text{GeV}}{f_a} \right)^{0.592} = 1.0 \left(\frac{m_a}{10 \mu\text{eV}} \right)^{0.592}$$

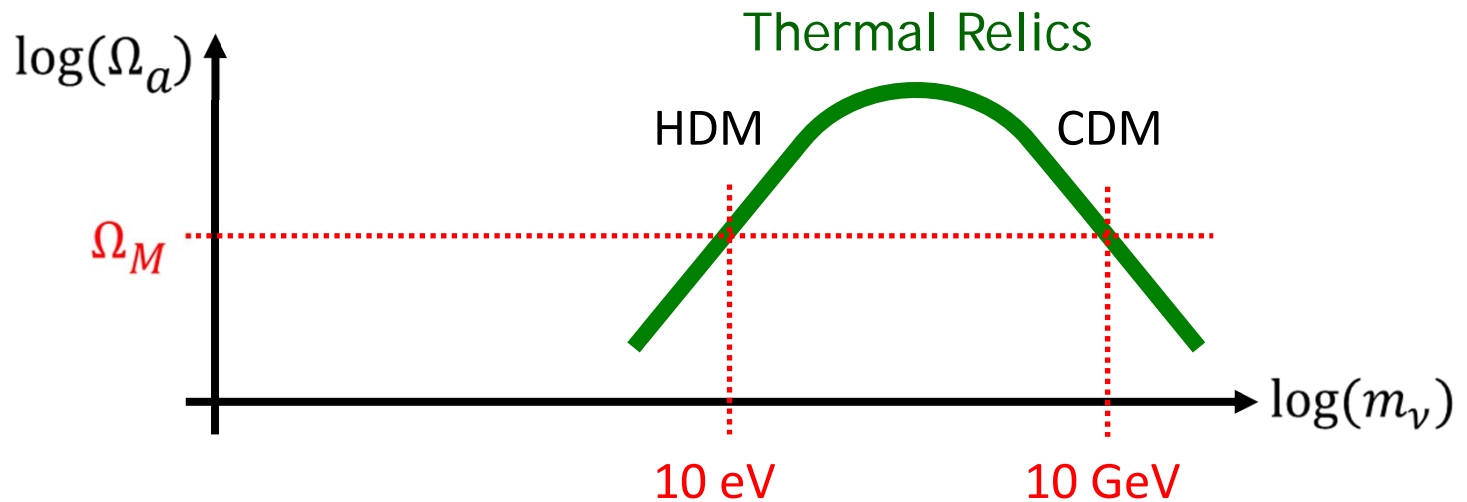
- $\Theta_i \sim 1$ implies $f_a \sim 10^{12}$ GeV and $m_a \sim 10 \mu\text{eV}$ (“classic window”)
- $f_a \sim 10^{16}$ GeV (GUT scale) or larger (string inspired) requires $\Theta_i \lesssim 0.003$ (“anthropic window”)

Lee-Weinberg Curve for Neutrinos and Axions

Axions



Neutrinos
& WIMPs



Cold Axion Populations

Case 1

Inflation after PQ symmetry breaking

Homogeneous mode oscillates after

$$T \lesssim \Lambda_{\text{QCD}}$$

Dependence on initial misalignment angle

$$\Omega_a \propto \Theta_i^2$$

Dark matter density a cosmic random number (“environmental parameter”)

- Isocurvature fluctuations from large quantum fluctuations of massless axion field created during inflation
- Strong CMB bounds on isocurvature fluctuations
- Scale of inflation required to be small

Case 2

Reheating restores PQ symmetry

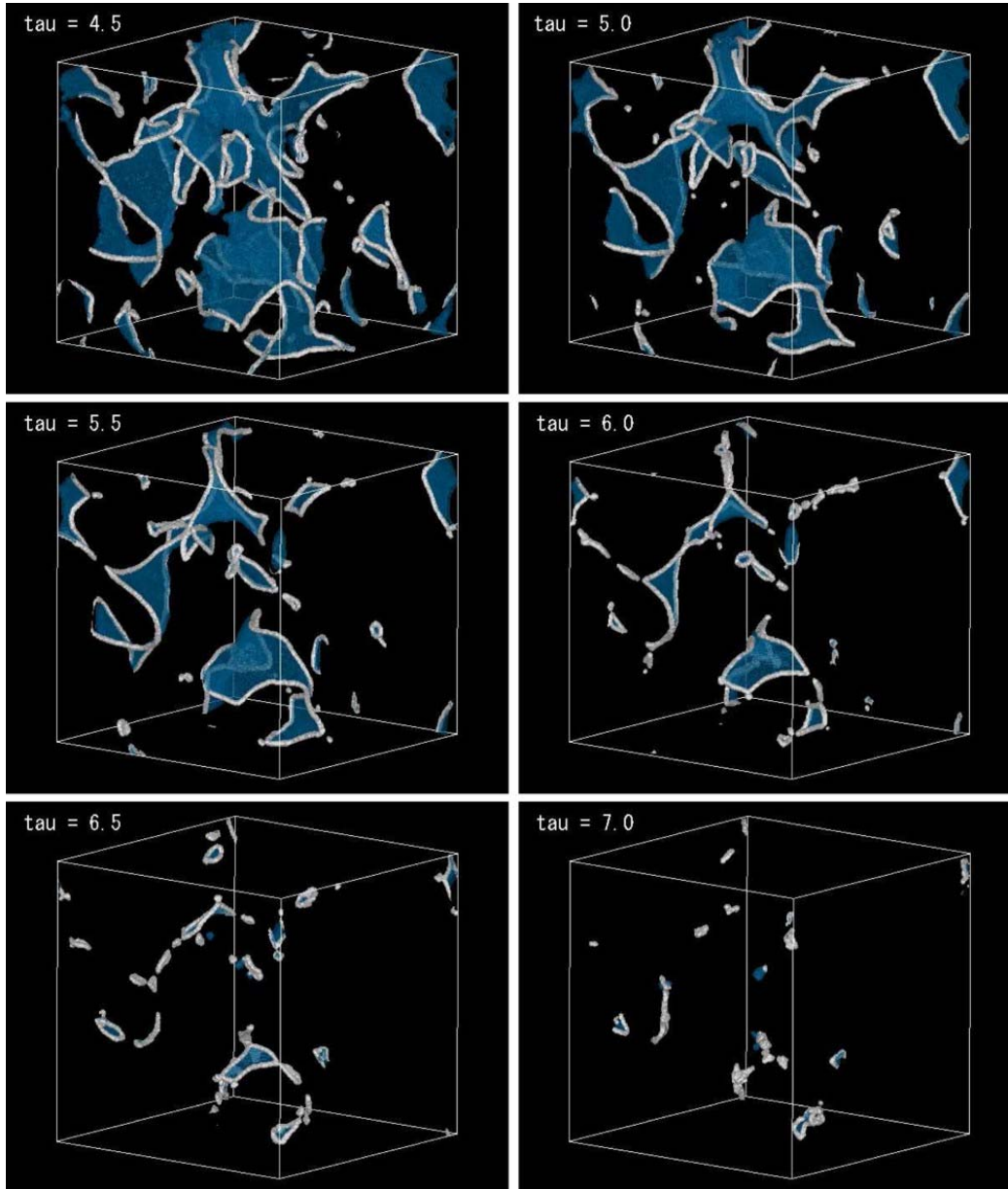
- Cosmic strings of broken $U_{\text{PQ}}(1)$ form by Kibble mechanism
- Radiate long-wavelength axions
- Ω_a independent of initial conditions
- $N = 1$ or else domain wall problem

Inhomogeneities of axion field large, self-couplings lead to formation of mini-clusters

Typical properties

- Mass $\sim 10^{-12} M_{\text{sun}}$
- Radius $\sim 10^{10}$ cm
- Mass fraction up to several 10%

Axion Production by Domain Wall and String Decay



Recent numerical studies of collapse of string-domain wall system

$$\Omega_a h^2 = (16 \pm 6) \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{1.19} \times \left(\frac{g_{*,1}}{70} \right)^{-0.41} \left(\frac{\Lambda}{400 \text{ MeV}} \right)$$

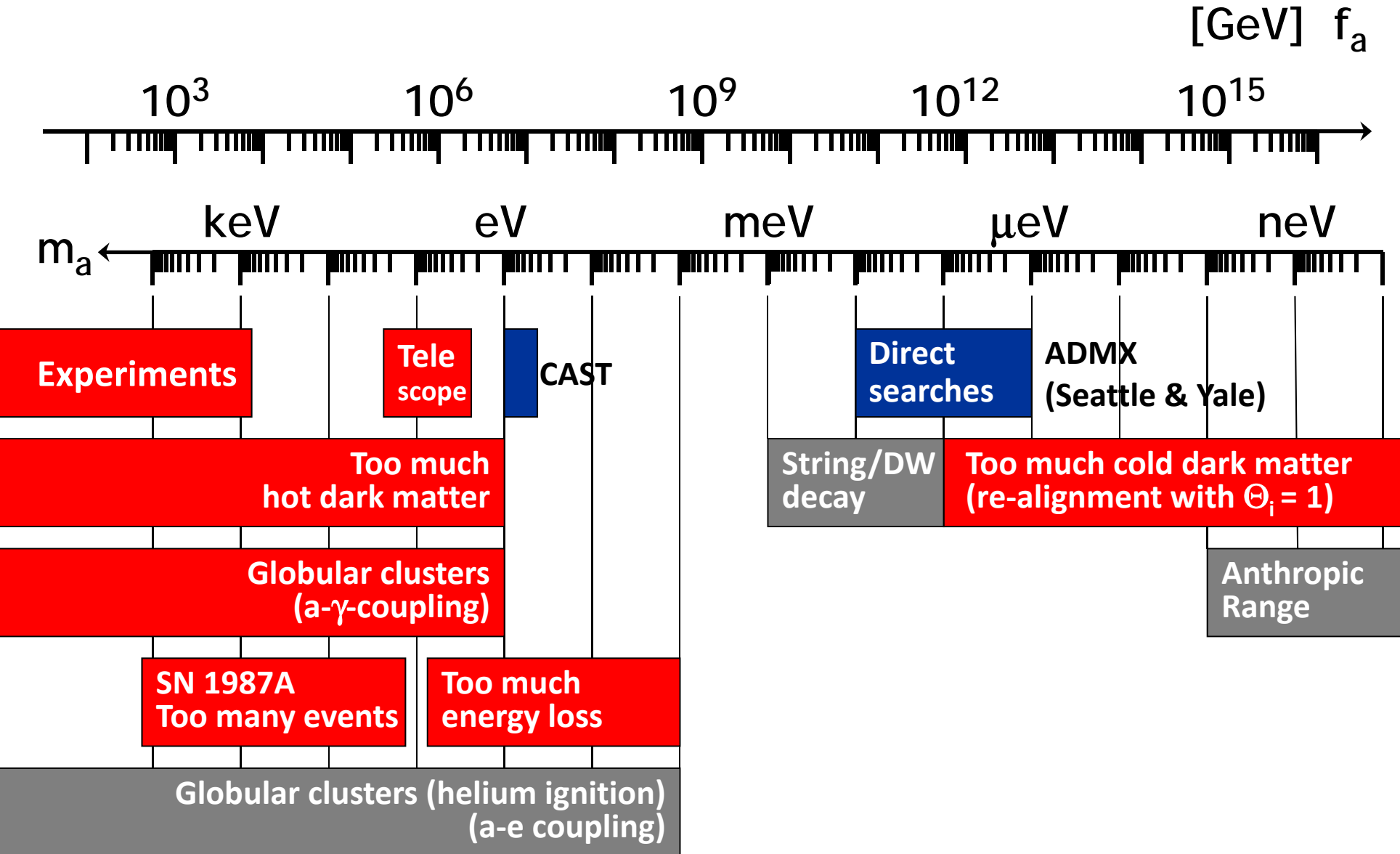
Implies a CDM axion mass of

$$m_a \sim 1 \text{ meV}$$

Hiramatsu, Kawasaki, Saikawa, Sekiguchi, arXiv:1202.5851 (2012)

Remains to be confirmed, interpretation of numerical studies not entirely straightforward

Axion Bounds and Searches



A deep field image of the universe, showing a vast field of galaxies in various colors (blue, green, orange, purple) and shapes (spiral, elliptical, irregular) against a black background. The galaxies are scattered across the frame, with some appearing as bright, distinct points and others as faint, diffuse structures. The overall scene is a rich, multi-colored tapestry of cosmic objects.

Searching for Axion Dark Matter

Experimental Tests of the “Invisible” Axion

P. Sikivie

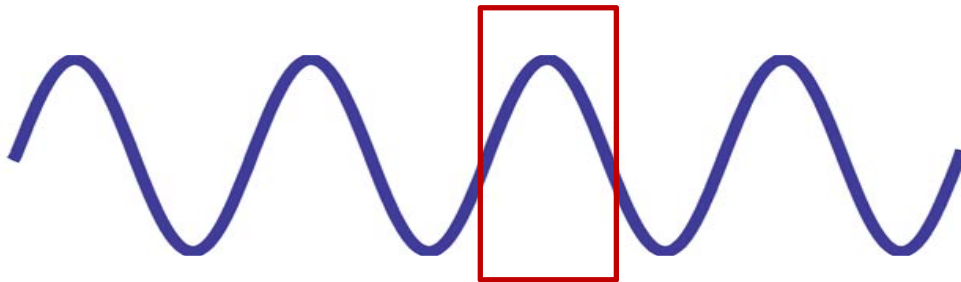
Physics Department, University of Florida, Gainesville, Florida 32611

(Received 13 July 1983)

Experiments are proposed which address the question of the existence of the “invisible” axion for the whole allowed range of the axion decay constant. These experiments exploit the coupling of the axion to the electromagnetic field, axion emission by the sun, and/or the cosmological abundance and presumed clustering of axions in the halo of our galaxy.

Magnet — N

Axion field homogeneous on > 30 m scales

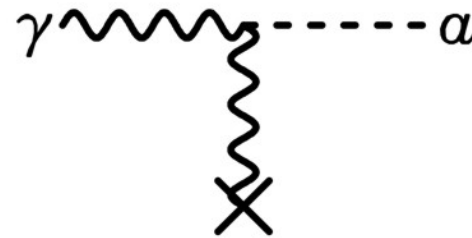


Use cavity to achieve large overlap integral between photon and axion waves

S

Primakoff effect:

Axion-photon transition in external static E or B field



Search for Galactic Axions (Cold Dark Matter)

Dark matter axions
Velocities in galaxy
Energies therefore

$$m_a = 1-100 \mu\text{eV}$$

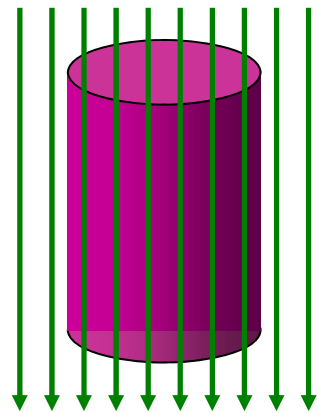
$$v_a \approx 10^{-3} c$$

$$E_a \approx (1 \pm 10^{-6}) m_a$$



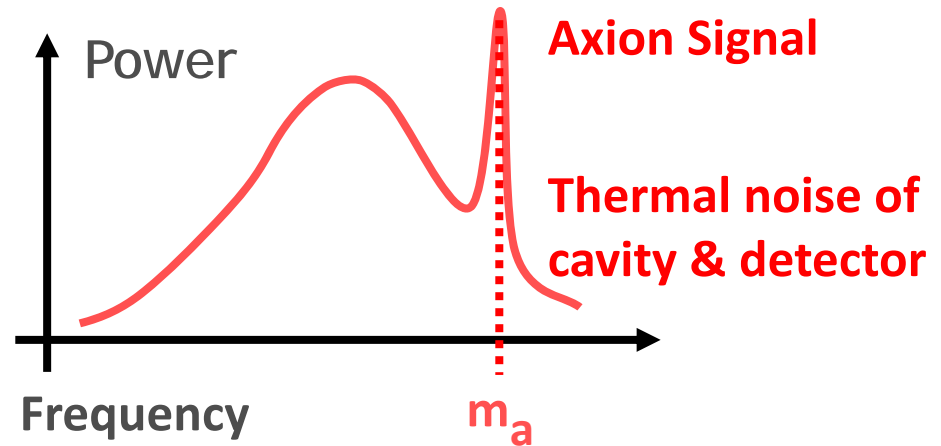
Microwave Energies
(1 GHz \approx 4 μeV)

Axion Haloscope (Sikivie 1983)

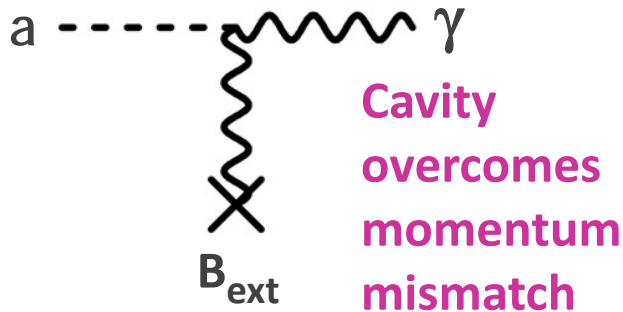


$B_{\text{ext}} \approx 8 \text{ Tesla}$

Microwave Resonator
 $Q \approx 10^5$



Primakoff Conversion



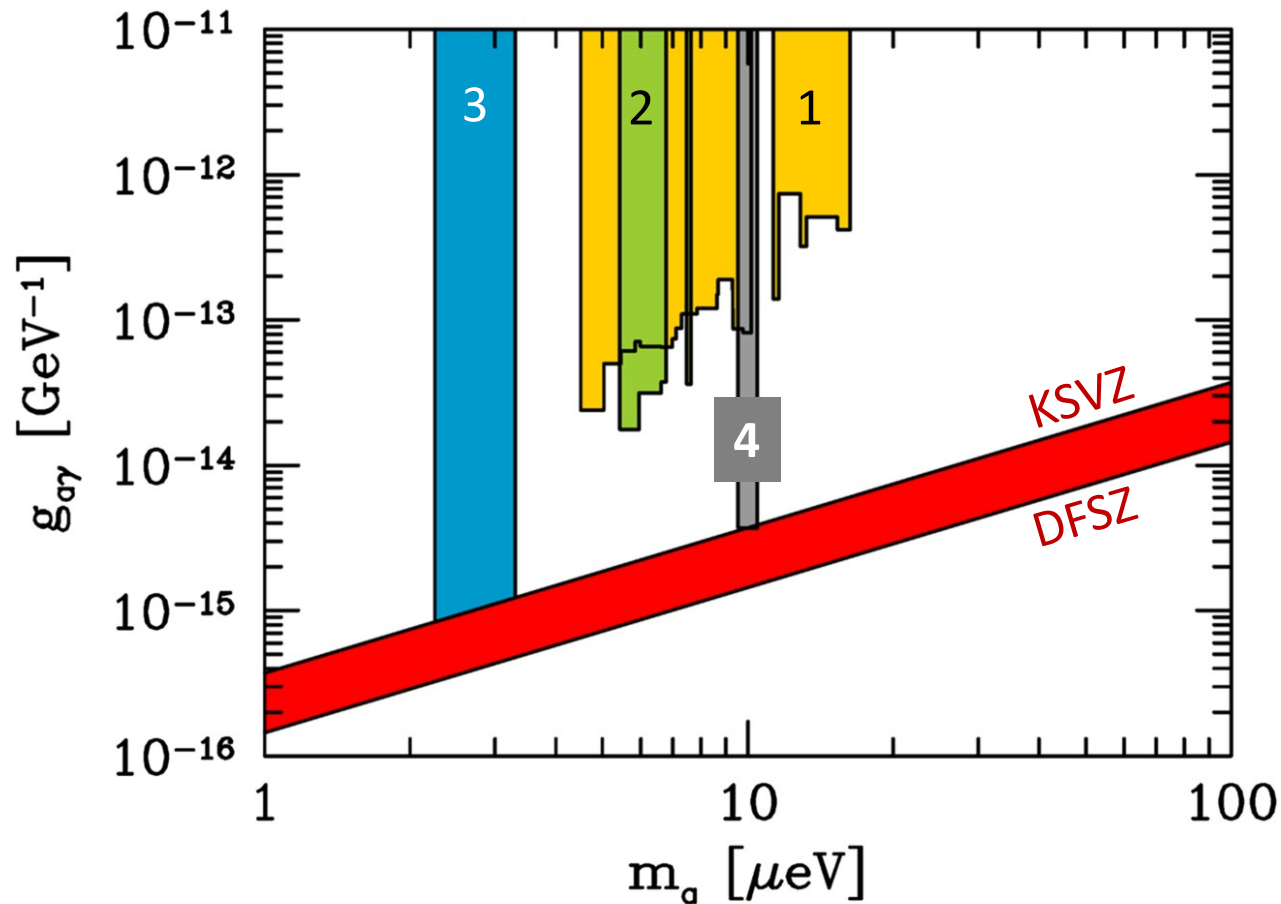
Power of galactic axion signal

$$4 \times 10^{-21} \text{ W} \frac{V}{0.22 \text{ m}^3} \left(\frac{B}{8.5 \text{ T}} \right)^2 \frac{Q}{10^5}$$

$$\times \left(\frac{m_a}{2\pi \text{ GHz}} \right) \left(\frac{\rho_a}{5 \times 10^{-25} \text{ g/cm}^3} \right)$$

Axion Dark Matter Searches

Limits assuming axions are the galactic dark matter with standard halo



1. Rochester-Brookhaven-Fermilab,
PRD 40 (1989) 3153

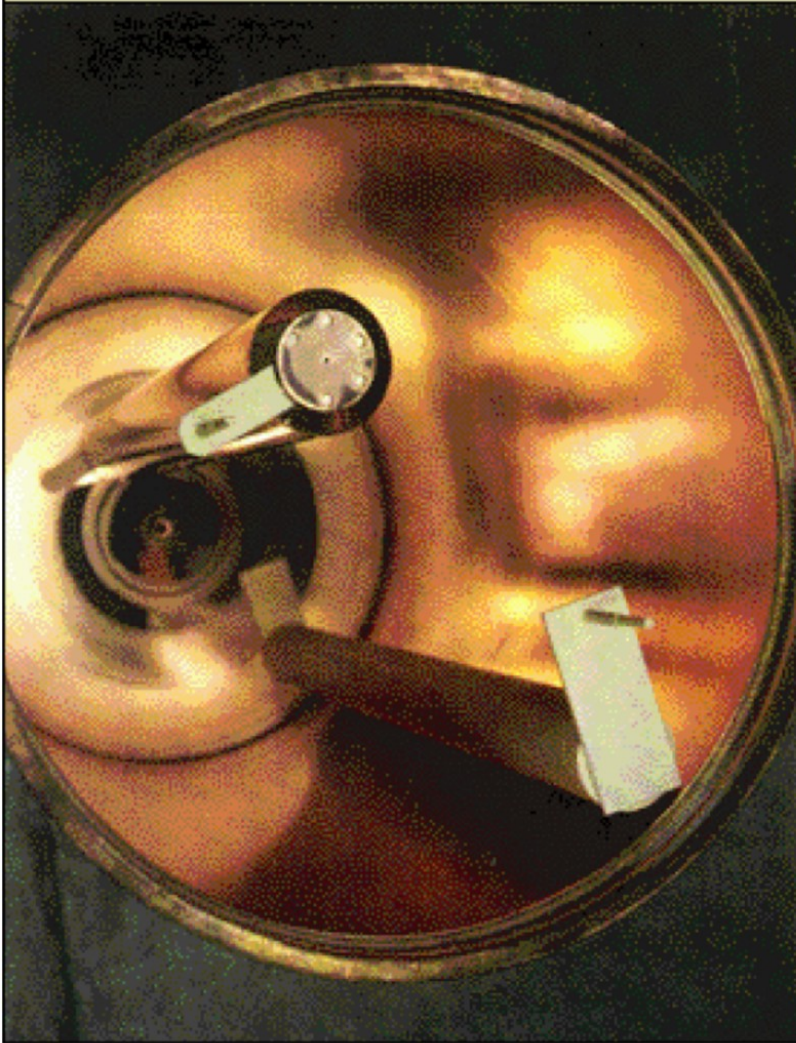
2. University of Florida
PRD 42 (1990) 1297

3. US Axion Search
ApJL 571 (2002) L27

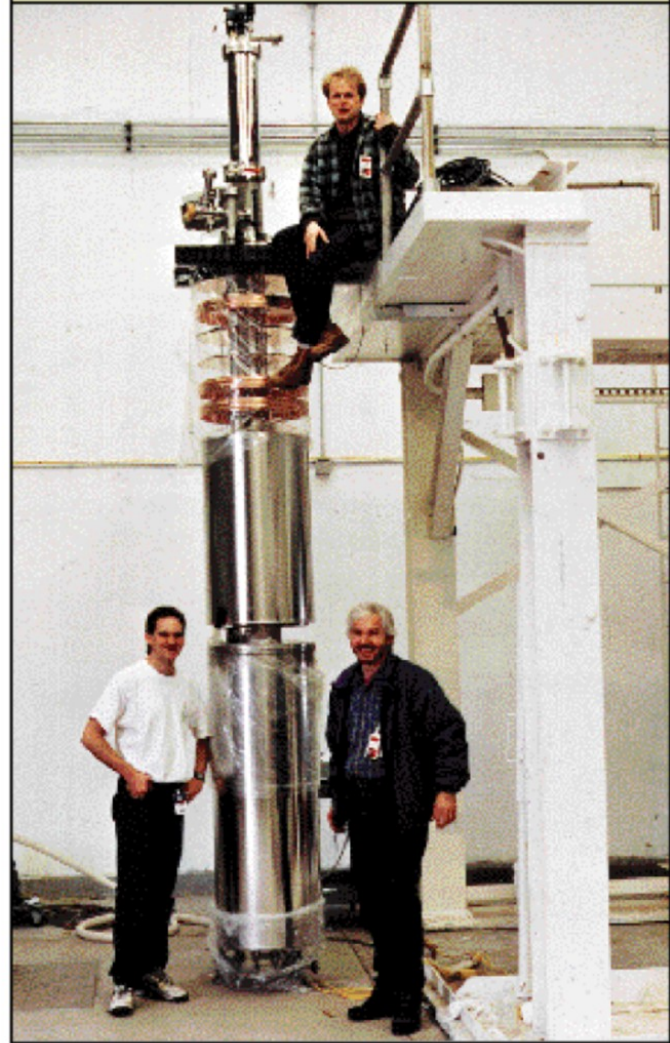
4. CARRACK I (Kyoto)
hep-ph/0101200

ADMX Hardware

High-Q Cavity (~200,000)



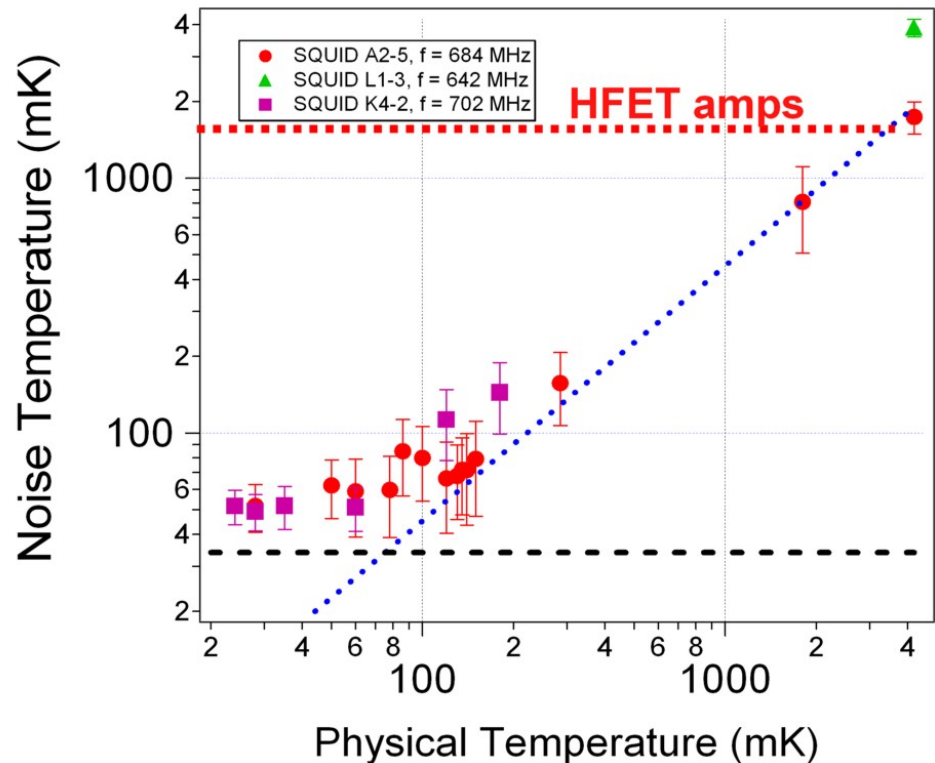
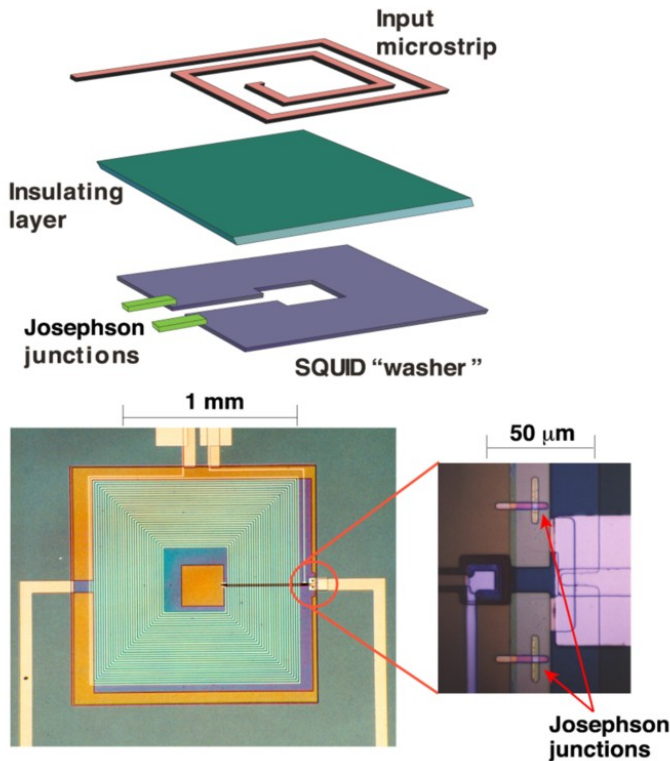
Experimental Insert



SQUID Microwave Amplifiers in ADMX

Presently the noise temperature of our HFET amps is $\sim 1.5\text{K}$
But the quantum limit at 1 GHz is $\sim 50\text{ mK}$

*Prof. John Clark and Dr. Darin Kinion (UC Berkeley)



Our latest SQUIDs are now within 15% of the Standard Quantum Limit

ADMX phase I: First-year science data (2009)

PRL 104, 041301 (2010)

PHYSICAL REVIEW LETTERS

week ending
29 JANUARY 2010

SQUID-Based Microwave Cavity Search for Dark-Matter Axions

S. J. Asztalos,^{*} G. Carosi, C. Hagmann, D. Kinion, and K. van Bibber
Lawrence Livermore National Laboratory, Livermore, California 94550, USA

M. Hotz, L. J. Rosenberg, and G. Rybka
University of Washington, Seattle, Washington 98195, USA

J. Hoskins, J. Hwang,[†] P. Sikivie, and D. B. Tanner
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R. Bradley
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University of California and Lawrence Berkeley National Laboratory, Berkeley, Calif
(Received 27 October 2009; published 28 January 2010)

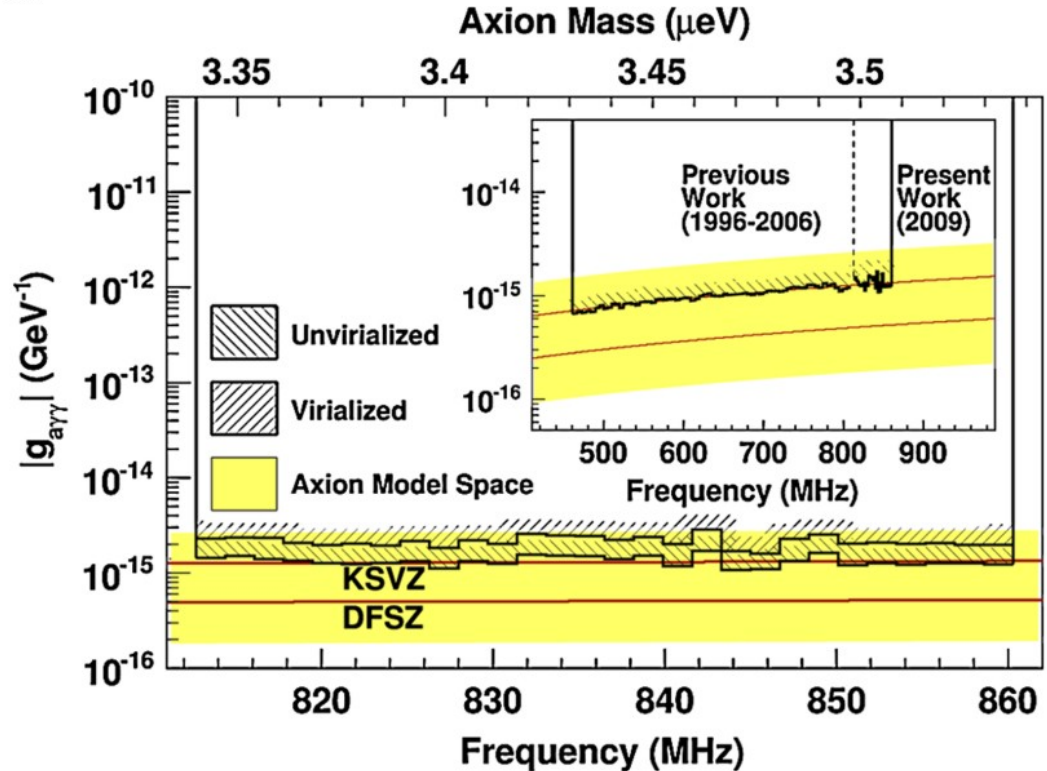


FIG. 5 (color online). Axion-photon coupling excluded at the 90% confidence level assuming a local dark-matter density of $0.45 \text{ GeV}/\text{cm}^3$ for two dark-matter distribution models. The shaded region corresponds to the range of the axion-photon coupling models discussed in [28].

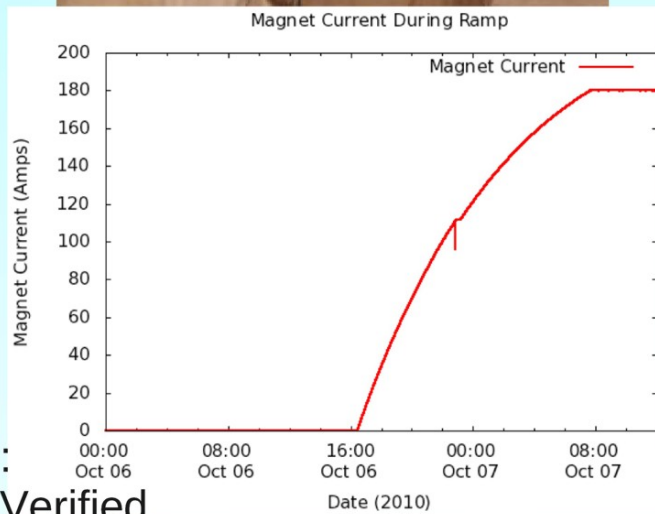
ADMX Comes to UW



August 2010:
ADMX Moves to UW



May 2011:
Main Magnet Installed
in Experiment Area (CENPA)



October 2010:
Main Magnet Verified





Schedule

~~Summer 2010~~ ~~Winter 2010~~

~~Spring 2011~~ Summer 2011 – Funding Clears

2011-2012 Construct new insert

small axion search here

2012-2013 Commission new insert, order dilution refrigerator

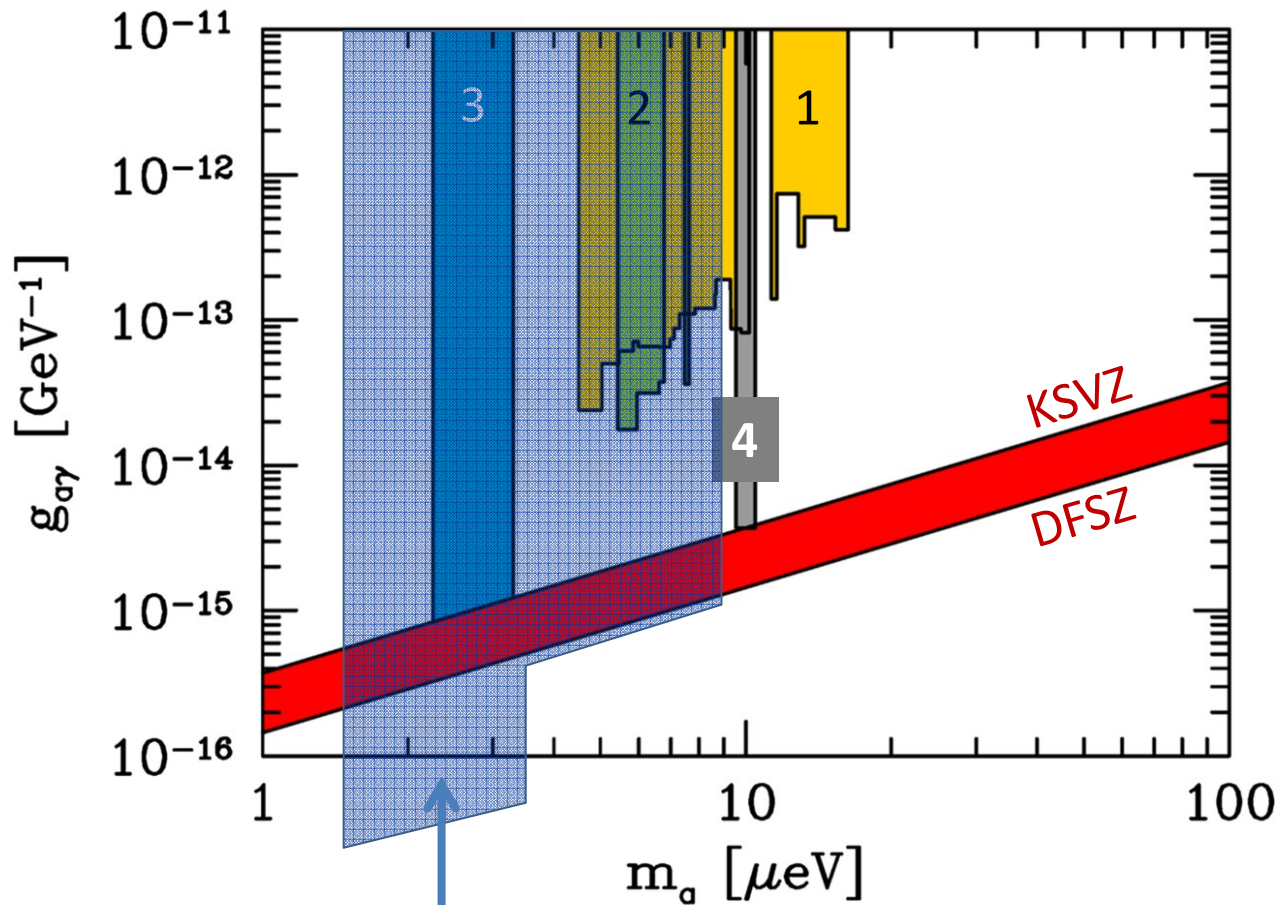
2013-2014 Install dilution refrigerator, commission

2015+ Definitive Axion search



Axion Dark Matter Searches

Limits assuming axions are the galactic dark matter with standard halo



1. Rochester-Brookhaven-Fermilab,
PRD 40 (1989) 3153

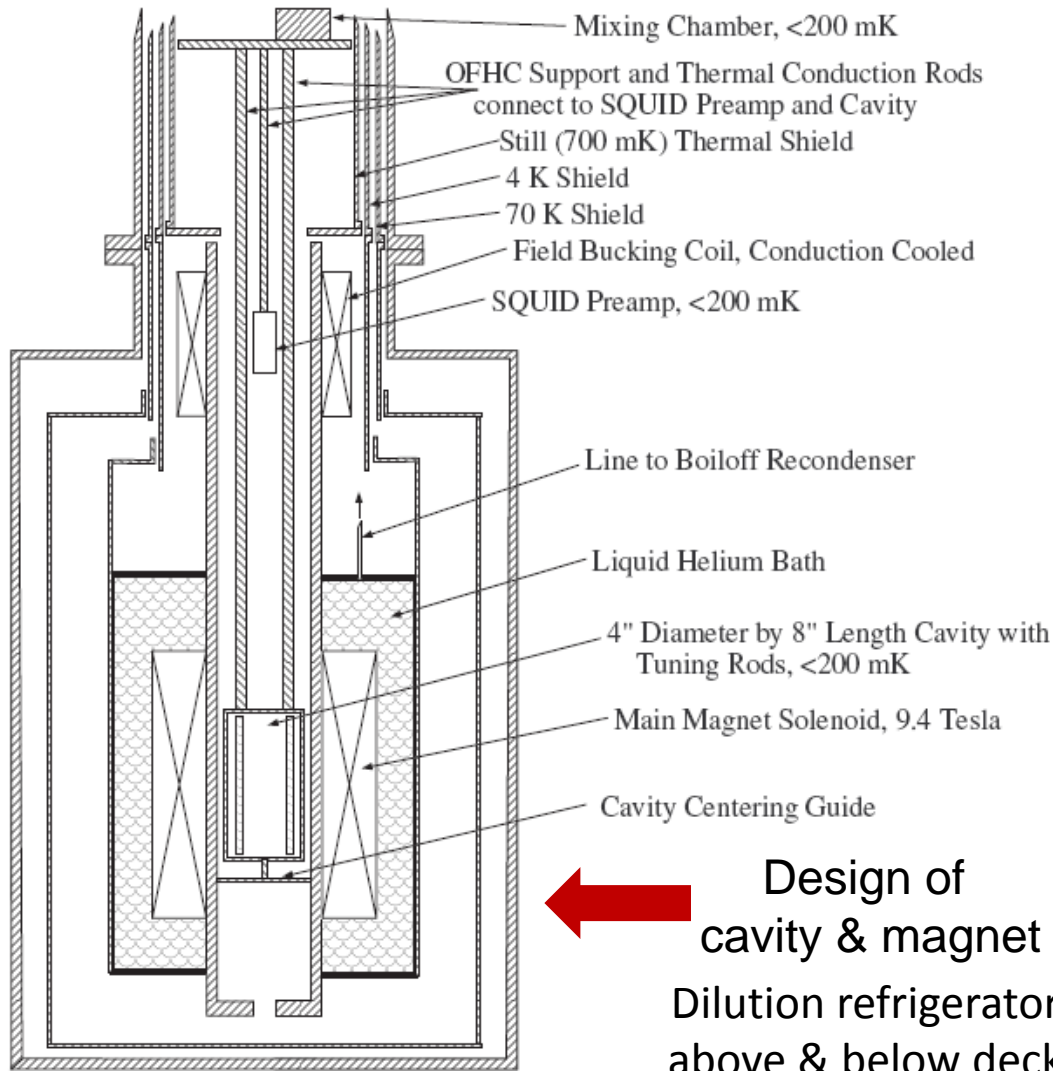
2. University of Florida
PRD 42 (1990) 1297

3. US Axion Search
ApJL 571 (2002) L27

4. CARRACK I (Kyoto)
hep-ph/0101200

ADMX-LF (Seattle) search range (2015+)

ADMX-HF at Yale (Steve Lamoreaux Group)

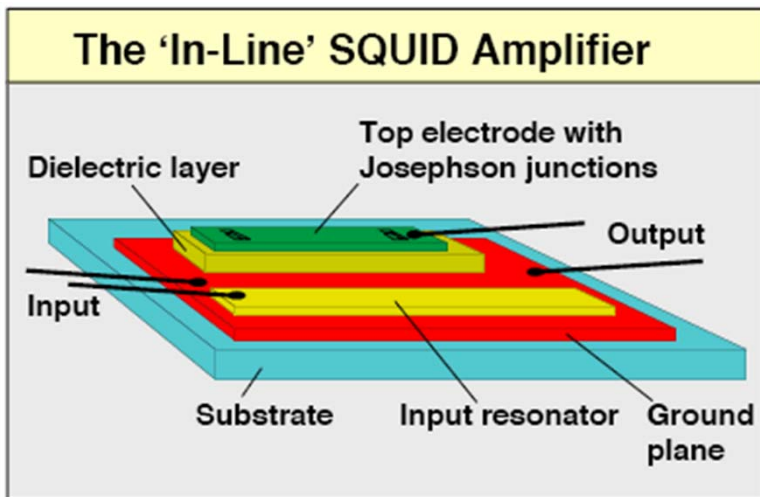


← Design of cavity & magnet
Dilution refrigerator above & below deck →



ADMX-HF will also be a test-bed for innovative concepts, e.g. thin-film superconducting cavities

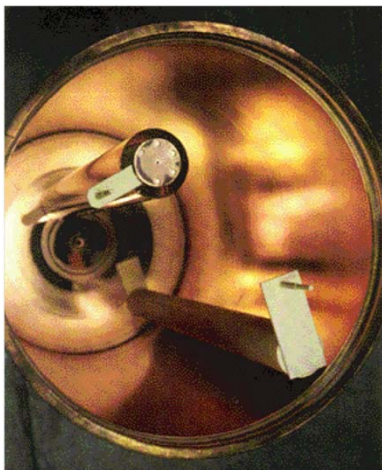
For the long term, ADMX needs concurrent R&D



To get to 10 GHz ($40 \mu\text{eV}$), and ultimately 100 GHz (0.4 meV), we need to:

- Develop new RF cavity geometries
- Develop new SQUID geometries

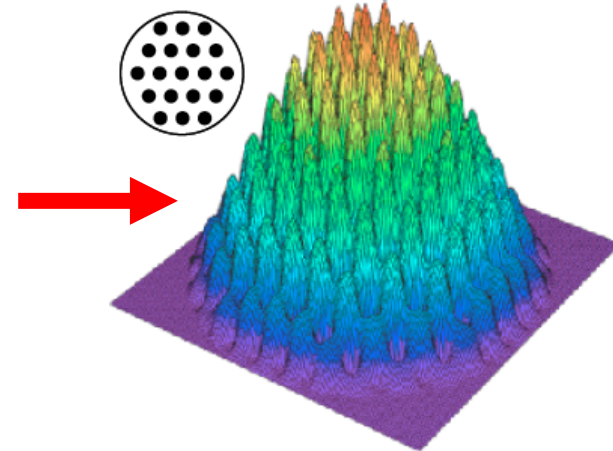
1 GHz



10 GHz



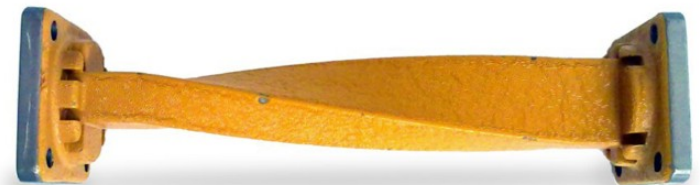
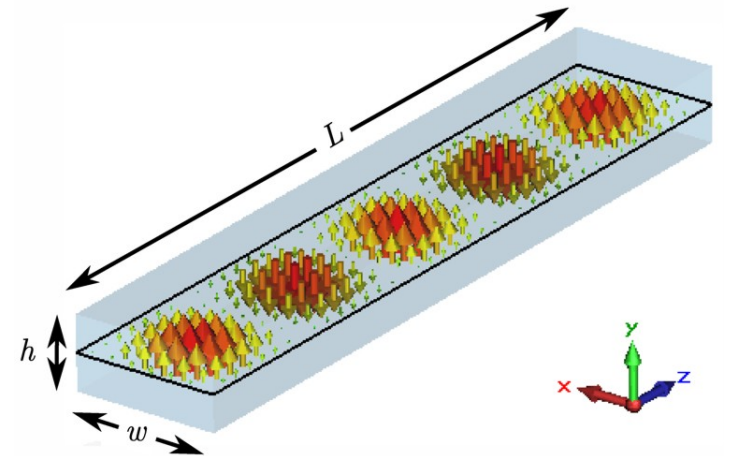
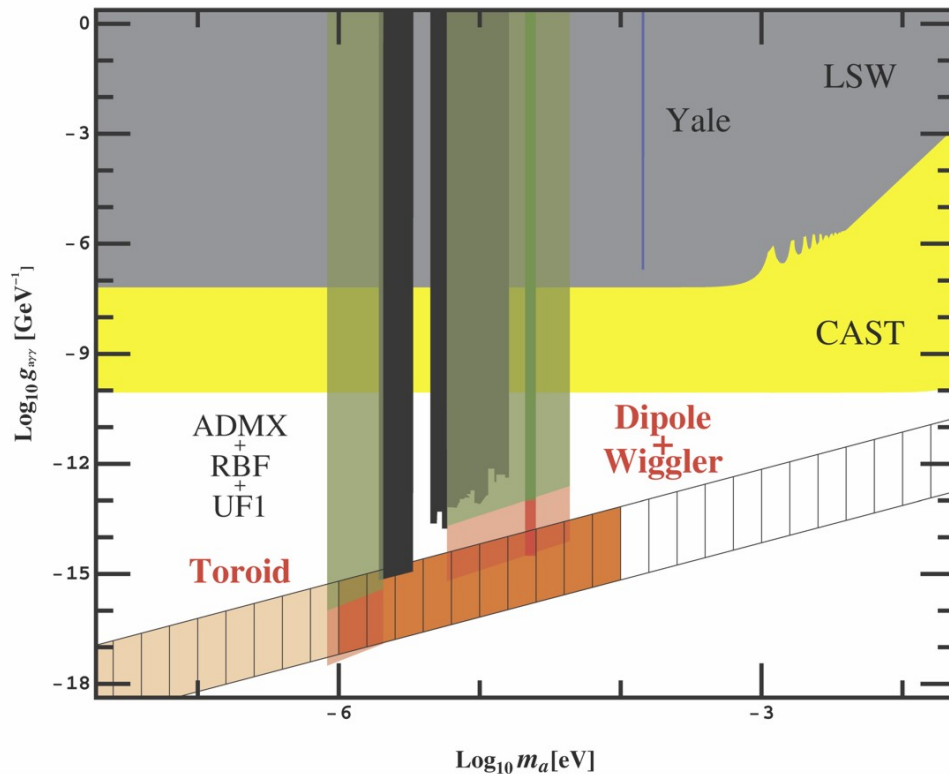
100 GHz



Prospects for Searching Axion-like Particle Dark Matter with Dipole, Toroidal and Wiggler Magnets

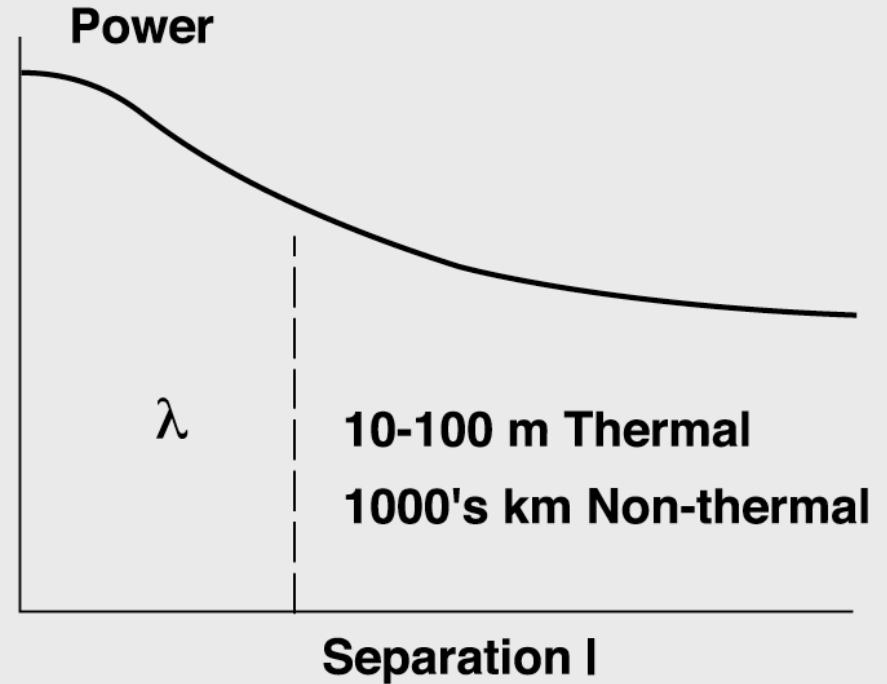
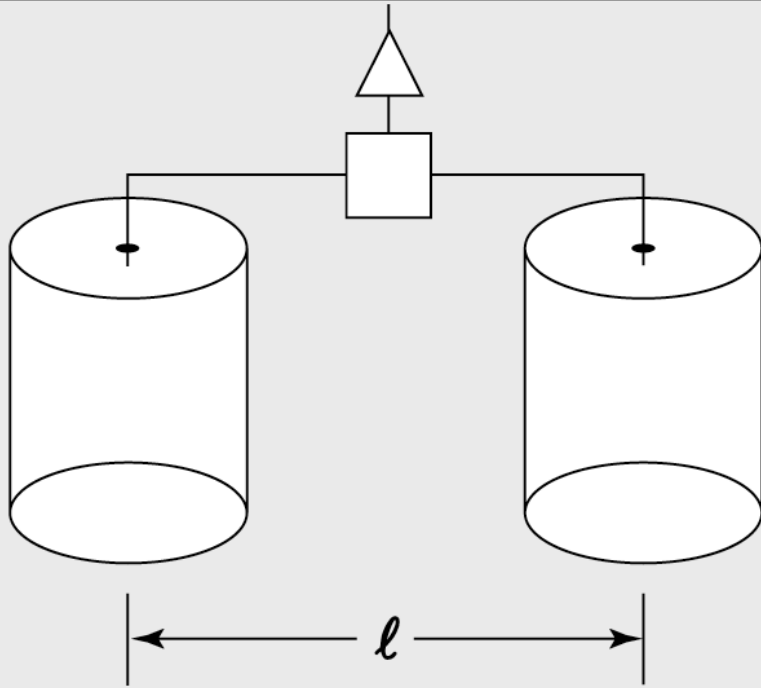
Oliver K. Baker¹, Michael Betz², Fritz Caspers², Joerg Jaeckel³, Axel Lindner⁴,
Andreas Ringwald⁴, Yannis Semertzidis⁵, Pierre Sikivie⁶, Konstantin Zioutas⁷.

arXiv:1110.2180v1 (10 Oct 2011)



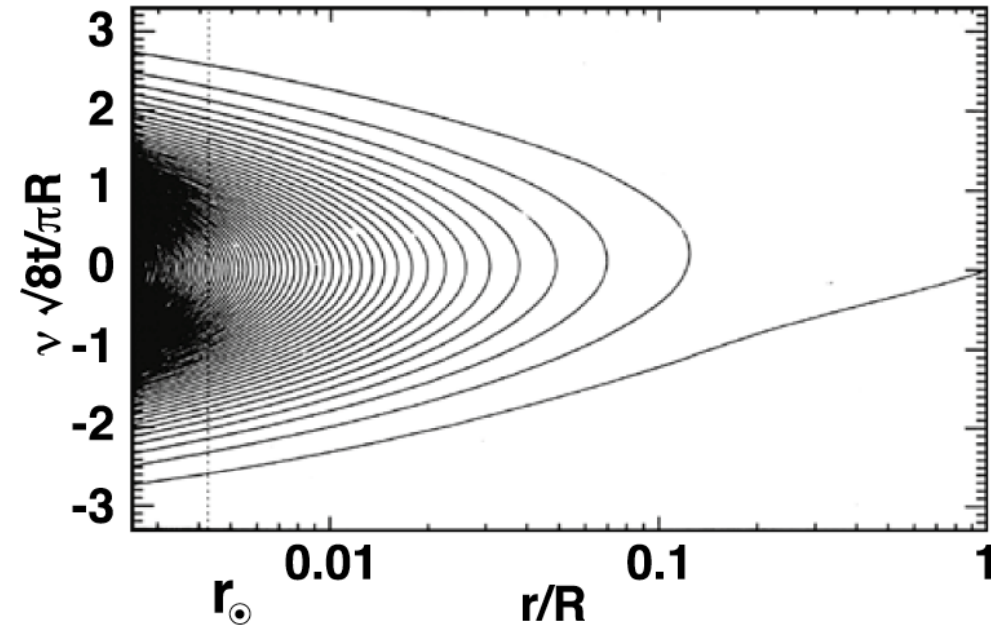
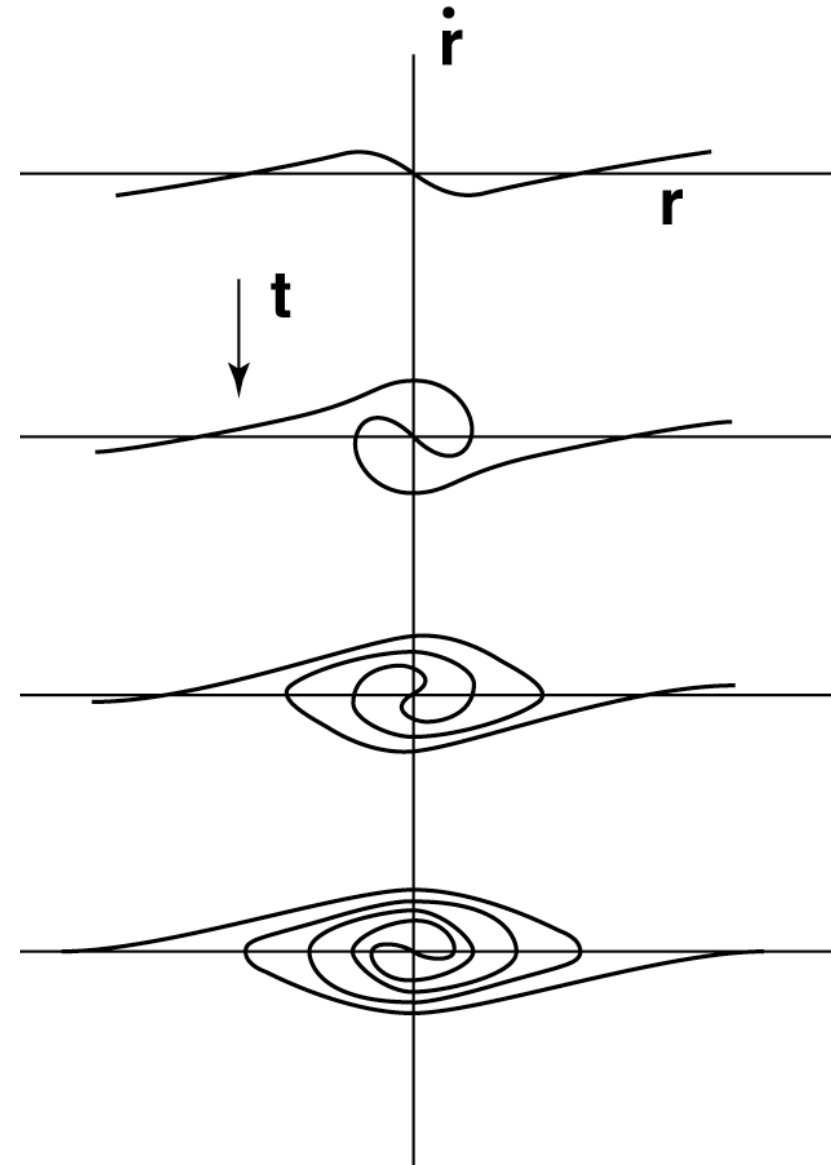
What if the axion is found?

The Study of Unique Quantum System



And should the axion possess fine-structure, it would constitute a “movie” of the formation of our Milky Way galaxy

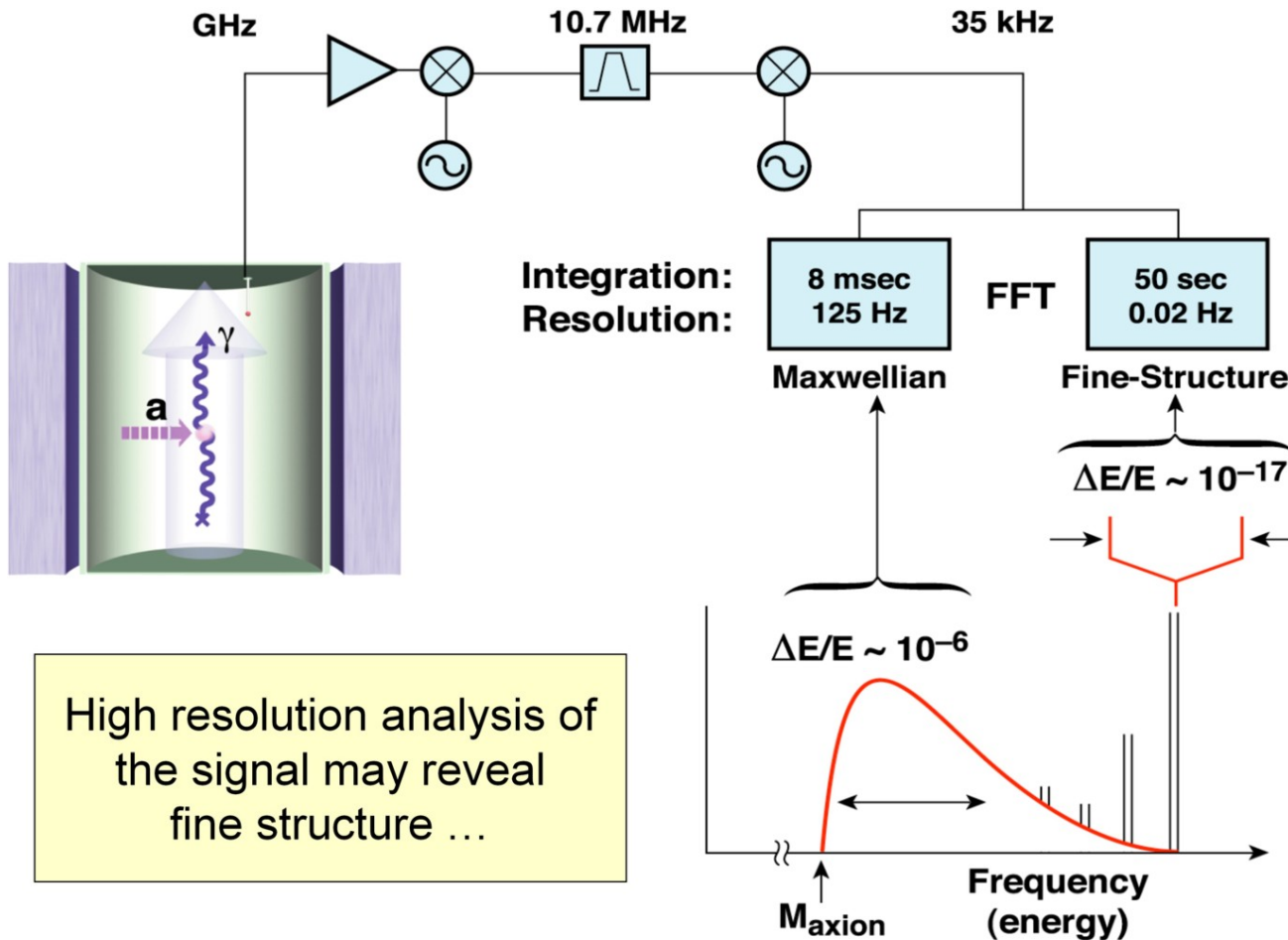
1D Infall and the Folding of Phase Space



- **Model begins with**
 - Zero Temperature CDM
 - Hubble expansion
 - Initial density perturbation $r = 0$
- **Grows self-consistent potential**

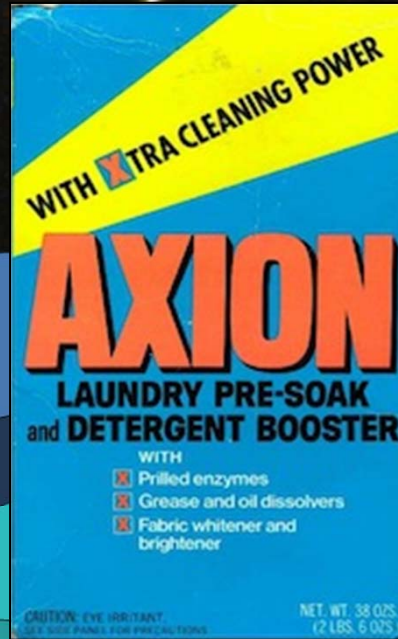
Fine Structure in the Axion Spectrum

- Axion distribution on a 3-dim sheet in 6-dim phase space
- Is “folded up” by galaxy formation
- Velocity distribution shows narrow peaks that can be resolved
- More detectable information than local dark matter density



P.Sikivie
& collaborators

Dark Energy 73%
(Cosmological Constant)



Ordinary Matter 4%
(of this only about 10% luminous)

Dark Matter 23%

Neutrinos 0.1–2%