

PSR J1614-2230 AND THE COMPSTAR EOS FOR QUARK MATTER

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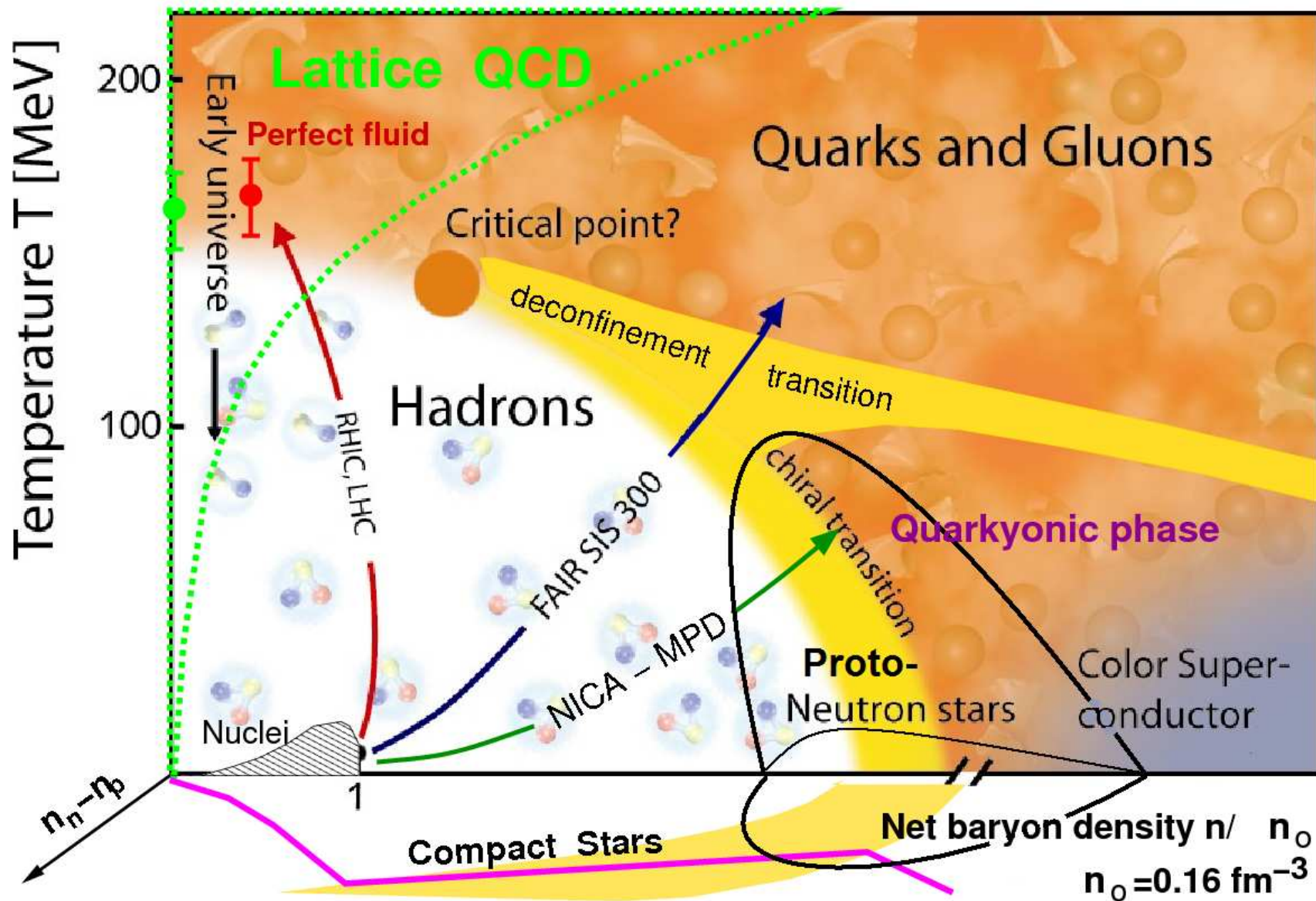
Bogoliubov Laboratory for Theoretical Physics, JINR Dubna, Russia

- Cold dense matter EoS - constraint from PSR J1614-2230
- Color superconducting quark matter and hybrid stars
- Supernovae and HIC in the QCD phase diagram - hybrid models at finite T, n
- CompOSE - CompStar Online Supernova EoS



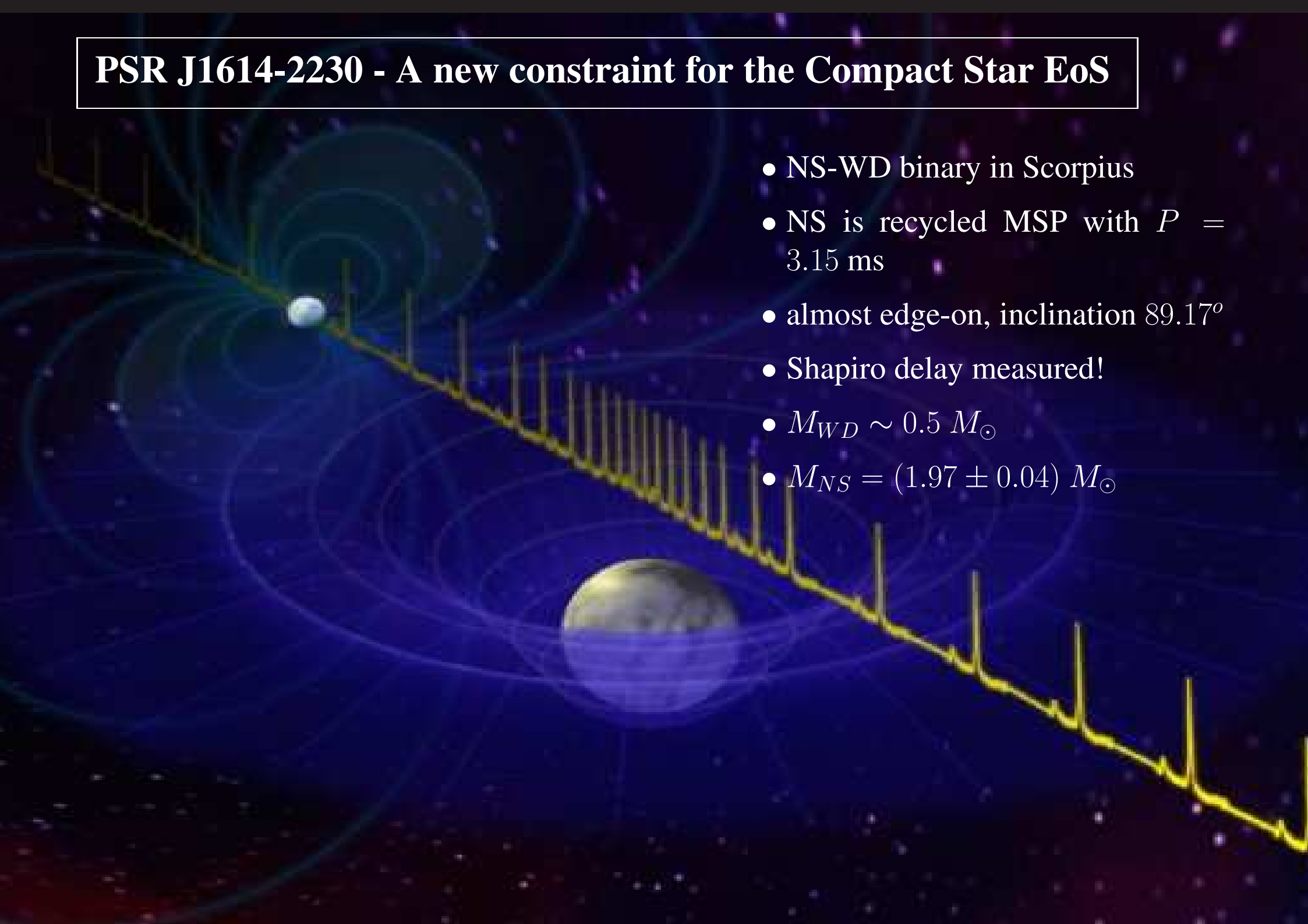
52nd Cracow School of Theoretical Physics, Zakopane 25.05.2012

Extreme States of Matter - The Phase Diagram



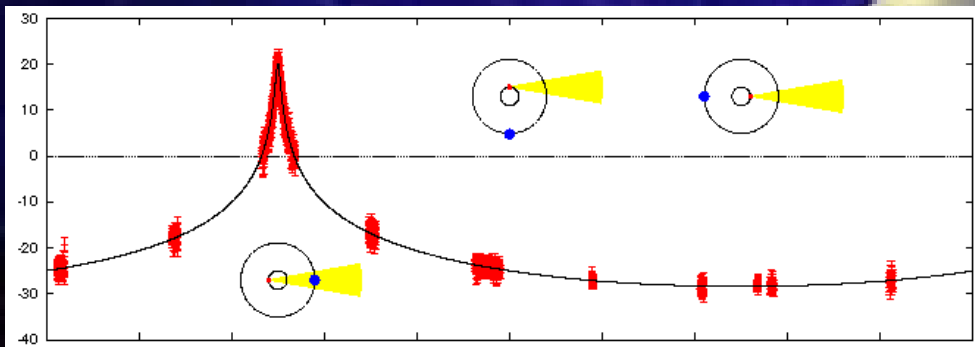
PSR J1614-2230 - A new constraint for the Compact Star EoS

- NS-WD binary in Scorpius
- NS is recycled MSP with $P = 3.15$ ms
- almost edge-on, inclination 89.17°
- Shapiro delay measured!
- $M_{WD} \sim 0.5 M_\odot$
- $M_{NS} = (1.97 \pm 0.04) M_\odot$



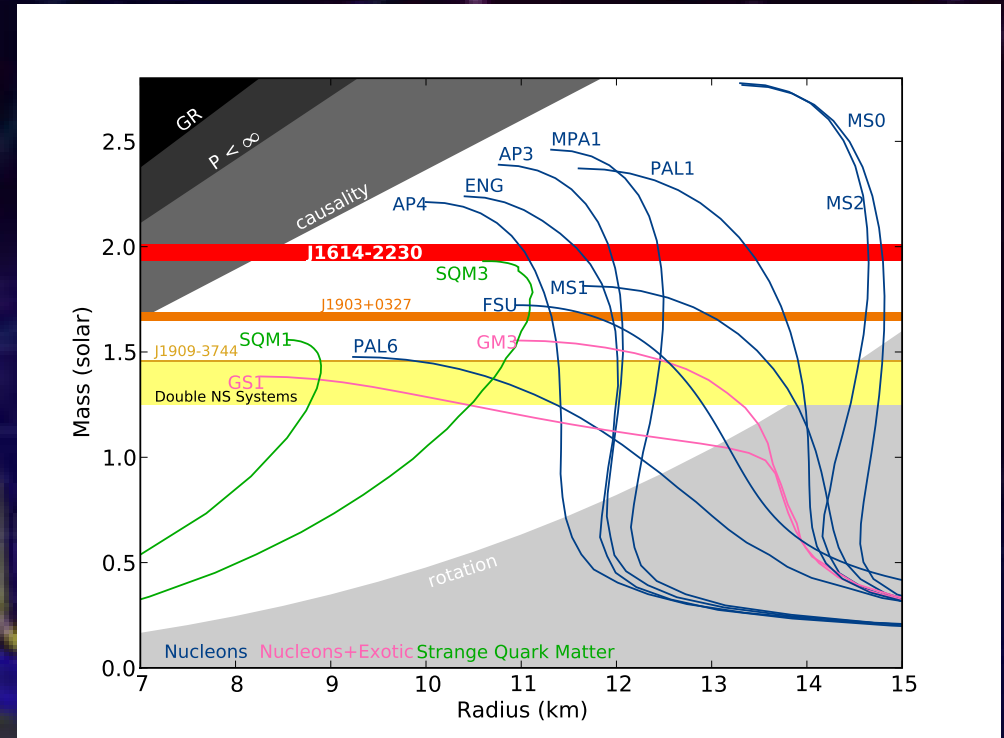
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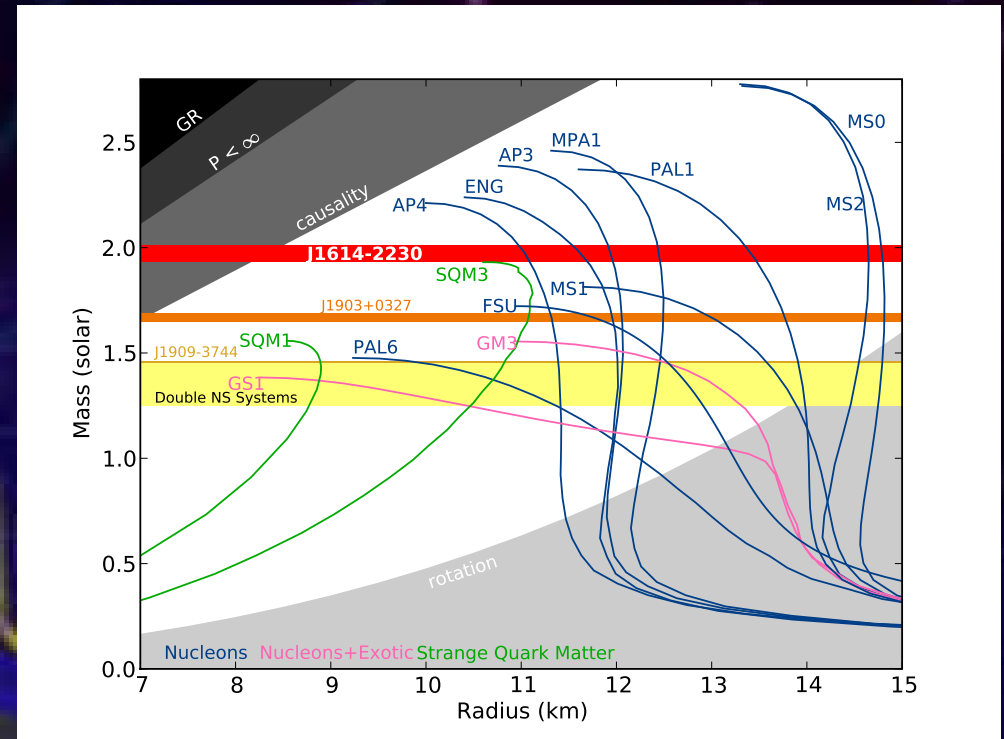
Demorest et al., Nature 467, 1081 (2010)

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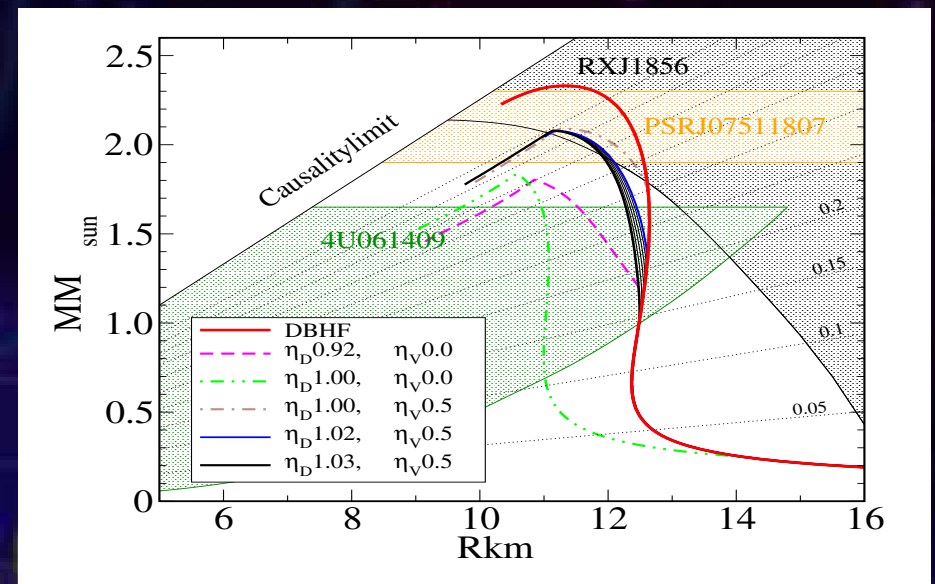


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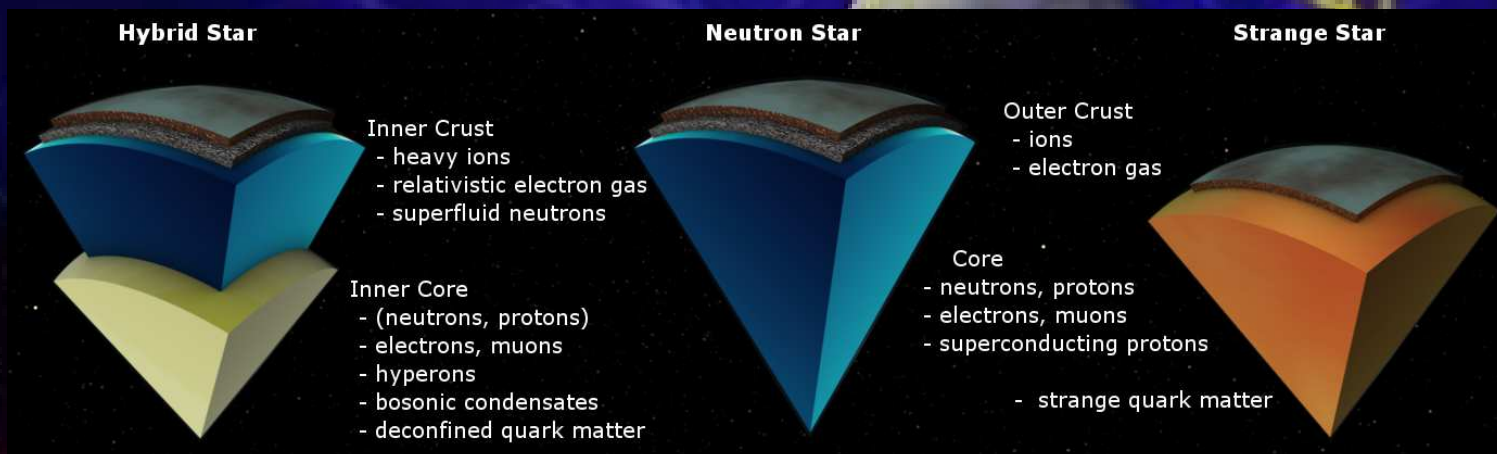
Some “soft” EoS are now ruled out !

What about hybrid stars? Strong constraints for quark matter!

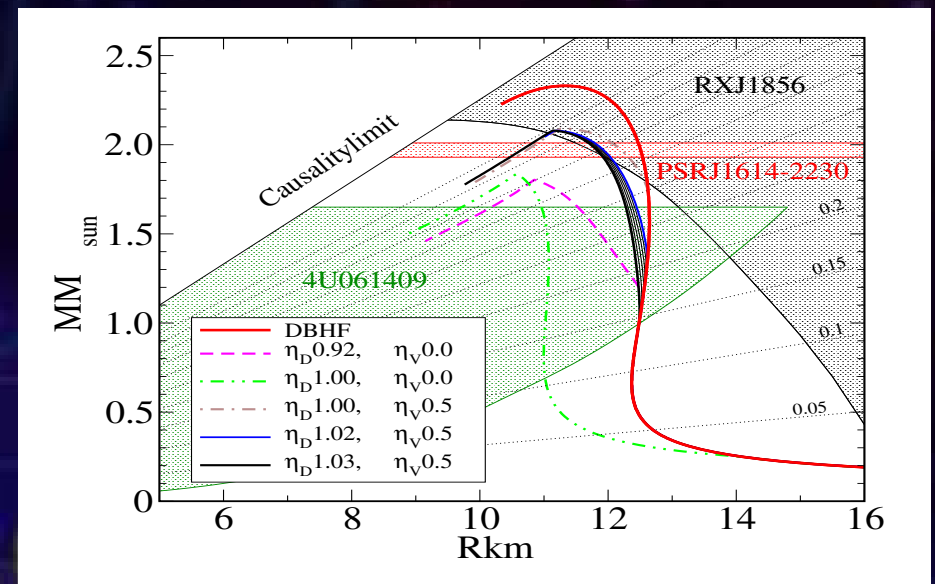
PSR J1614-2230 - A new constraint for the Compact Star EoS



Klähn et al., PLB 654, 170 (2007)



PSR J1614-2230 - A new constraint for the Compact Star EoS



CompStar, in preparation (2010)

State-of-the-art hybrid EoS model:

- Chiral symmetry restoration
- Color superconductivity
- Vector meanfield “stiffening”

PSR J1614-2230 - A new constraint for the Compact Star EoS

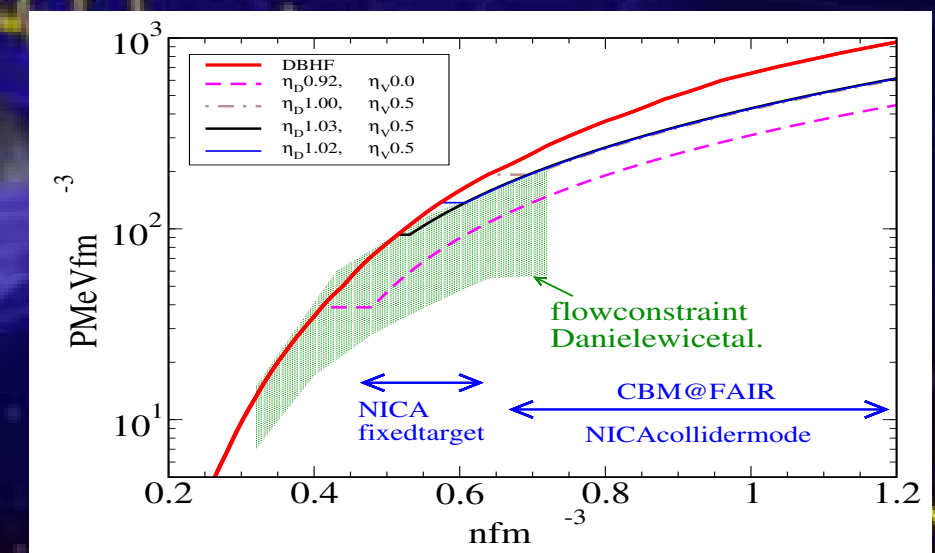
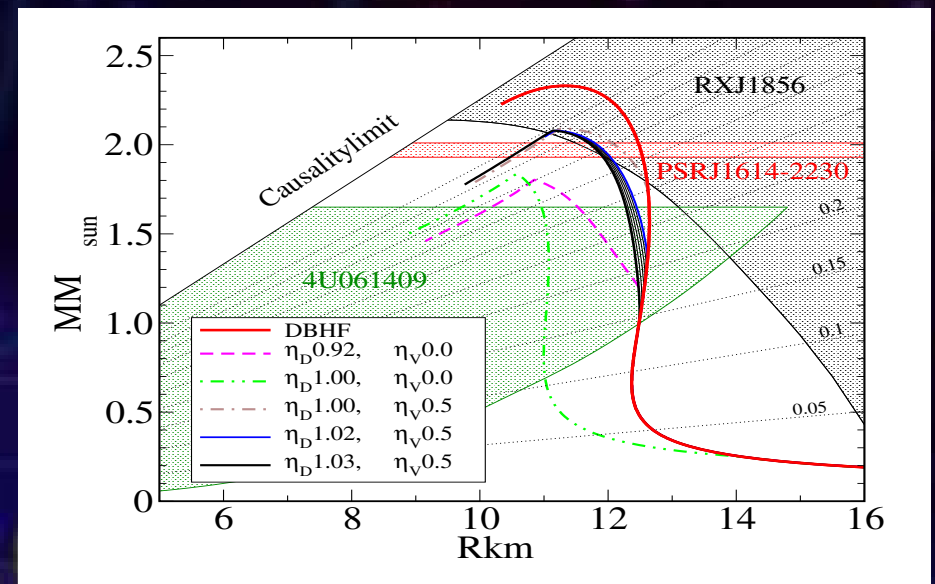
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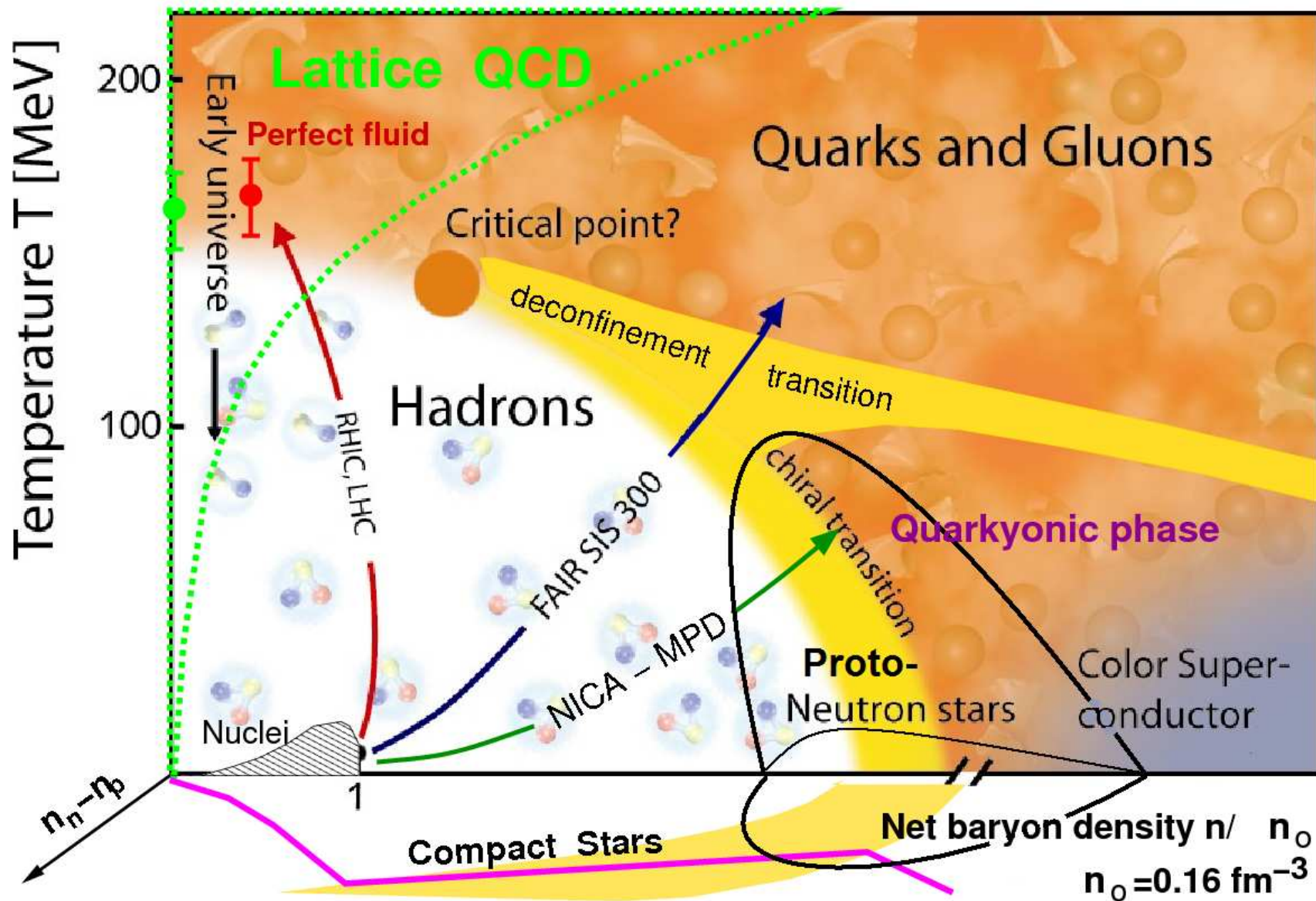
Constraints from heavy-ion collisions:

- Flow constraint at high densities
- Not too early onset of quark matter

⇒ **QCD phase diagram**



Extreme States of Matter - The Phase Diagram



CHIRAL MODEL FIELD THEORY FOR QUARK MATTER

- Partition function as a Path Integral (imaginary time $\tau = i t$)

$$Z[T, V, \mu] = \int \mathcal{D}\bar{\psi} \mathcal{D}\psi \exp \left\{ - \int^{\beta} d\tau \int_V d^3x [\bar{\psi} [i\gamma^\mu \partial_\mu - m - \gamma^0 (\mu + \lambda_8 \mu_8 + i\lambda_3 \phi_3)] \psi - \mathcal{L}_{\text{int}} + U(\Phi)] \right\}$$

Polyakov loop: $\Phi = N_c^{-1} \text{Tr}_c [\exp(i\beta \lambda_3 \phi_3)]$ Order parameter for **deconfinement**

- Current-current interaction (4-Fermion coupling) and KMT determinant interaction

$$\mathcal{L}_{\text{int}} = \sum_{M=\pi,\sigma,\dots} G_M (\bar{\psi} \Gamma_M \psi)^2 + \sum_D G_D (\bar{\psi}^C \Gamma_D \psi)^2 - K [\det_f(\bar{q}(1 + \gamma_5)q) + \det_f(\bar{q}(1 - \gamma_5)q)]$$

- Bosonization (Hubbard-Stratonovich Transformation)

$$Z[T, V, \mu] = \int \mathcal{D}M_M \mathcal{D}\Delta_D^\dagger \mathcal{D}\Delta_D e^{-\sum_{M,D} \frac{M_M^2}{4G_M} - \frac{|\Delta_D|^2}{4G_D} + \frac{1}{2} \text{Tr} \ln S^{-1}[\{M_M\}, \{\Delta_D\}, \Phi] + U(\Phi) + V_{\text{KMT}}}$$

- Collective quark fields: Mesons (M_M) and Diquarks (Δ_D); Gluon mean field: Φ
- Systematic evaluation: **Mean fields** + **Fluctuations**
 - Mean-field approximation: **order parameters** for phase transitions (gap equations)
 - Lowest order fluctuations: **hadronic correlations** (bound & scattering states)
 - Higher order fluctuations: hadron-hadron **interactions**

NJL MODEL FOR NEUTRAL 3-FLAVOR QUARK MATTER

Thermodynamic Potential $\Omega(T, \mu) = -T \ln Z[T, \mu]$

$$\begin{aligned} \Omega(T, \mu) = & \frac{\phi_u^2 + \phi_d^2 + \phi_s^2}{8G_S} + \frac{|\Delta_{ud}|^2 + |\Delta_{us}|^2 + |\Delta_{ds}|^2}{4G_D} + \frac{K \phi_u + \phi_d + \phi_s}{16G_S^3} - \frac{(\mu^* - \mu)^2}{4G_V} \\ & - T \sum_n \int \frac{d^3p}{(2\pi)^3} \frac{1}{2} \text{Tr} \ln \left(\frac{1}{T} S^{-1}(i\omega_n, \vec{p}) \right) + U(\Phi) + \Omega_e - \Omega_0. \end{aligned}$$

Inverse Nambu – Gorkov Propagator $S^{-1}(i\omega_n, \vec{p}) = \begin{bmatrix} \gamma_\mu p^\mu - M(\vec{p}) + \mu\gamma^0 & \widehat{\Delta}(\vec{p}) \\ \widehat{\Delta}^\dagger(\vec{p}) & \gamma_\mu p^\mu - M(\vec{p}) - \mu\gamma^0 \end{bmatrix},$

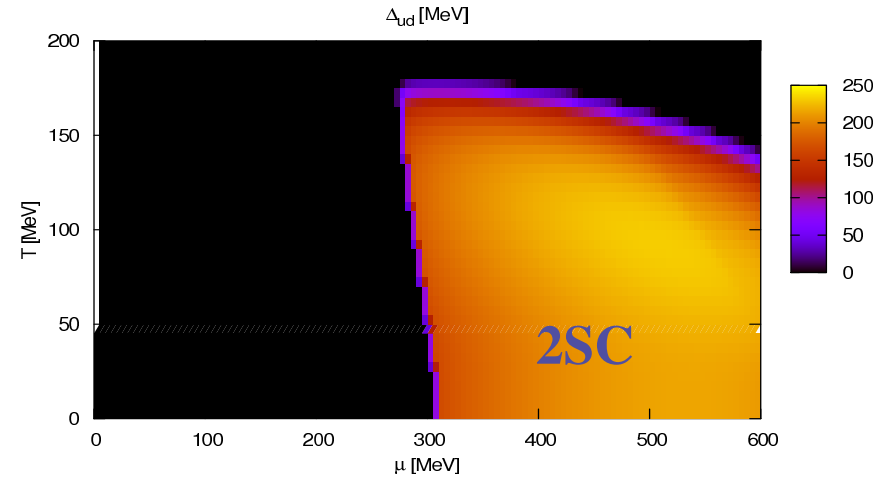
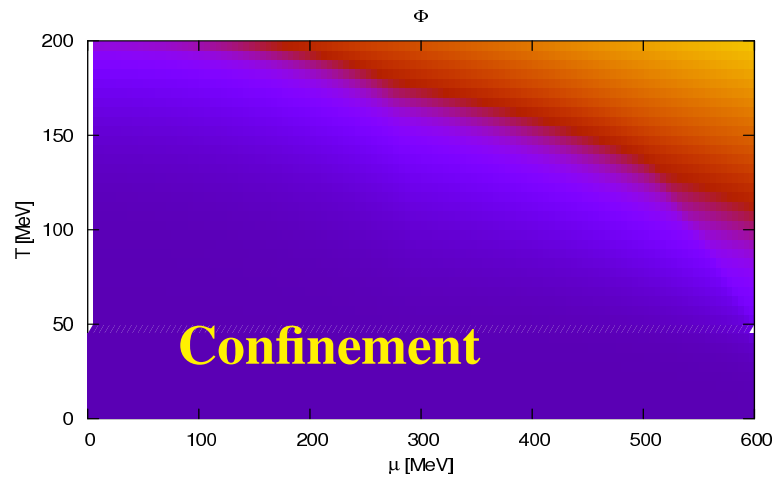
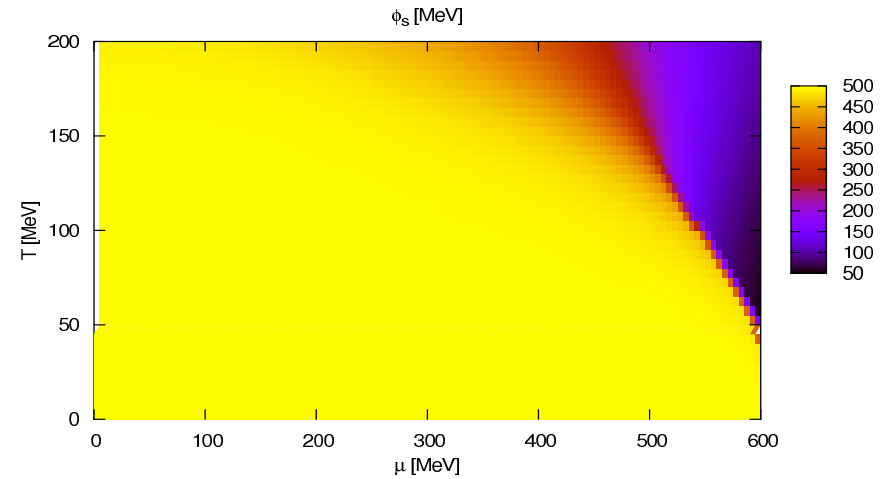
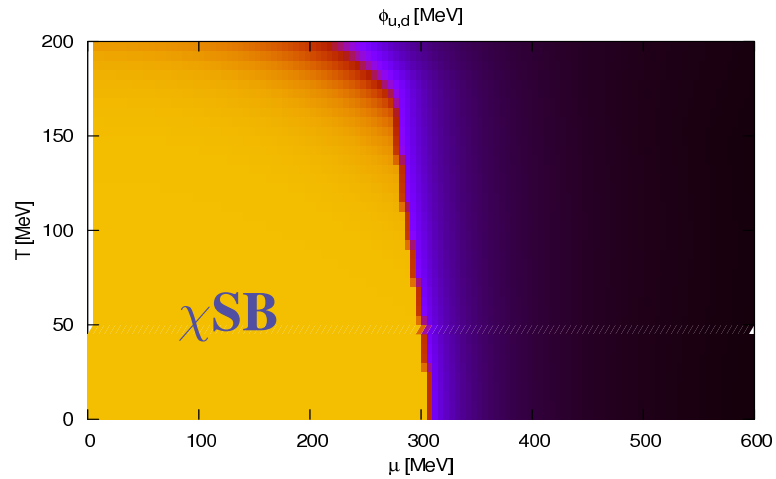
Fermion Determinant ($\text{Tr} \ln \mathbf{D} = \ln \det \mathbf{D}$): $\ln \det[\beta S^{-1}(i\omega_n, \vec{p})] = 2 \sum_{a=1}^{18} \ln\{\beta^2[\omega_n^2 + \lambda_a(\vec{p})^2]\}.$

Result for the thermodynamic Potential (Meanfield approximation)

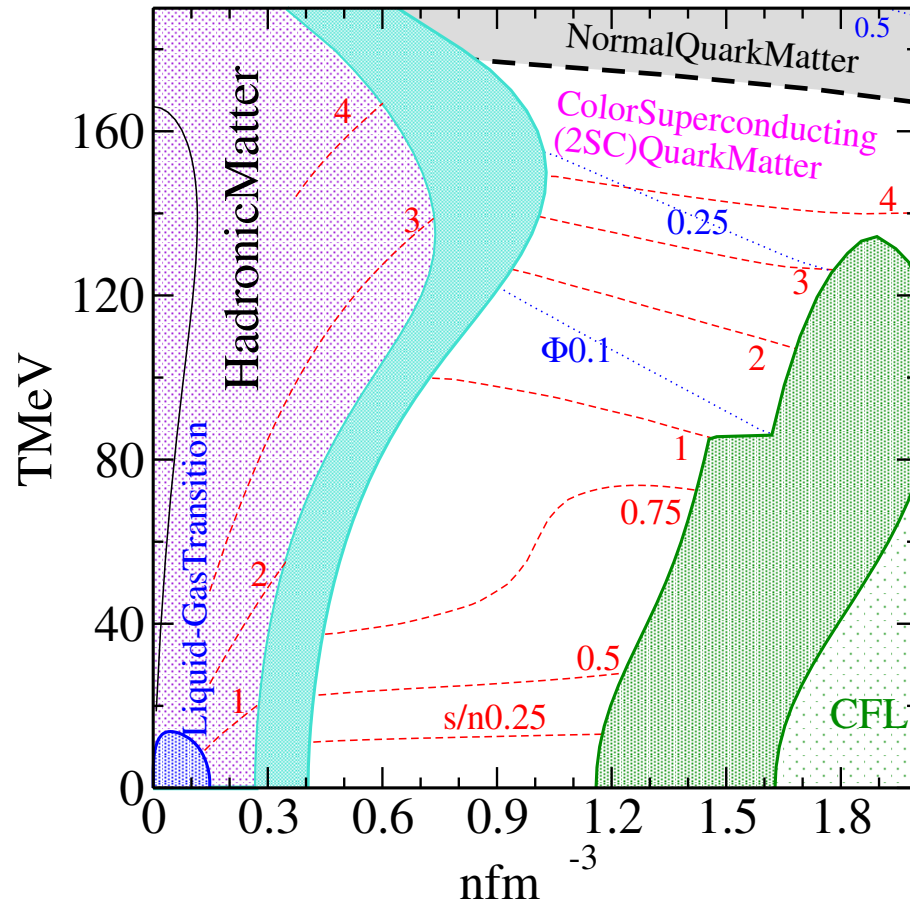
$$\begin{aligned} \Omega(T, \mu) = & \frac{\phi_u^2 + \phi_d^2 + \phi_s^2}{8G_S} + \frac{|\Delta_{ud}|^2 + |\Delta_{us}|^2 + |\Delta_{ds}|^2}{4G_D} + \frac{K \phi_u + \phi_d + \phi_s}{16G_S^3} - \frac{(\mu^* - \mu)^2}{4G_V} \\ & - \int \frac{d^3p}{(2\pi)^3} \sum_{a=1}^{18} \left[\lambda_a + 2T \ln \left(1 + e^{-\lambda_a/T} \right) \right] + U(\Phi) + \Omega_e - \Omega_0. \end{aligned}$$

Color and electric charge neutrality constraints: $n_Q = n_8 = n_3 = 0, n_i = -\partial\Omega/\partial\mu_i = 0,$
Equations of state: $P = -\Omega,$ etc.

PHASES OF QCD @ EXTREMES: NO COLOR NEUTRALITY



PHASE DIAGRAM FOR SYMMETRIC MATTER (HIC)

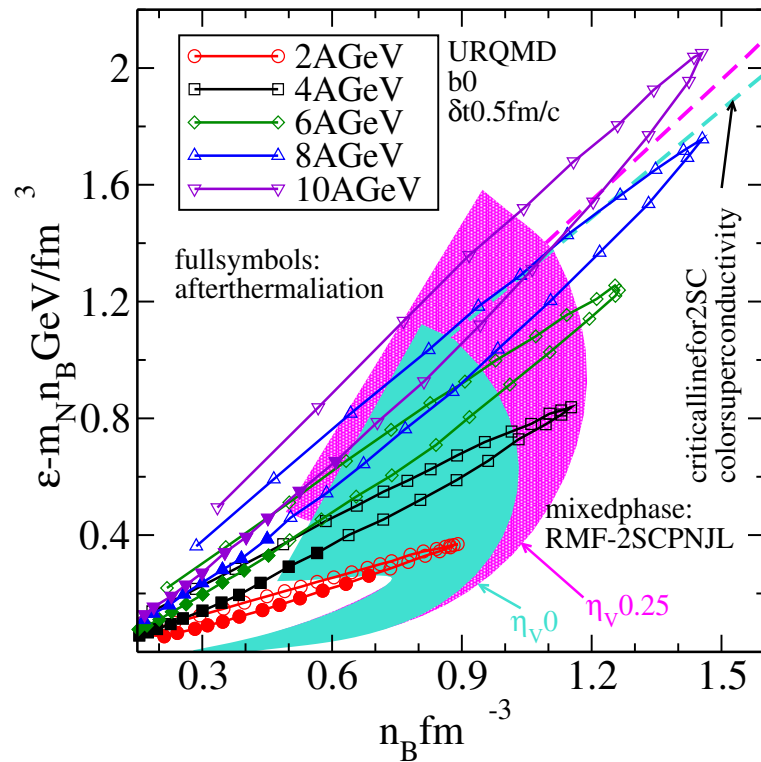


DB, Sandin, Skokov, NICA WhitePaper (2009)

- Critical density for chiral restoration $n_\chi \geq 1.5 n_0$ **increasing (!)** with low T
- Almost crossover (masquerade!), i.e. small density jump, small latent heat/ time delay in heavy-ion coll.!
- High $T_c \approx 0.9T_d$ for 2SC phase due to Polyakov loop.
- 2SC - CFL phase transition at $n \geq 6 n_0$ with density jump and latent heat/ time delay!
Provided the temperature can be kept low $T \leq 100$ MeV

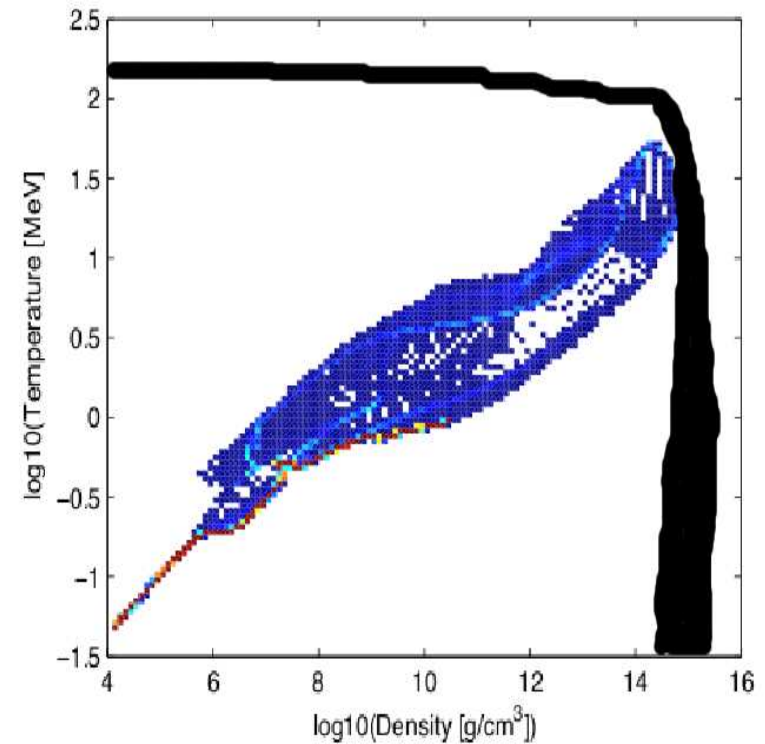
EXPLORING THE QCD PHASE DIAGRAM: TRAJECTORIES

Heavy-Ion Collisions:



D.B., Skokov, Sandin, NICA WhitePaper (2009)

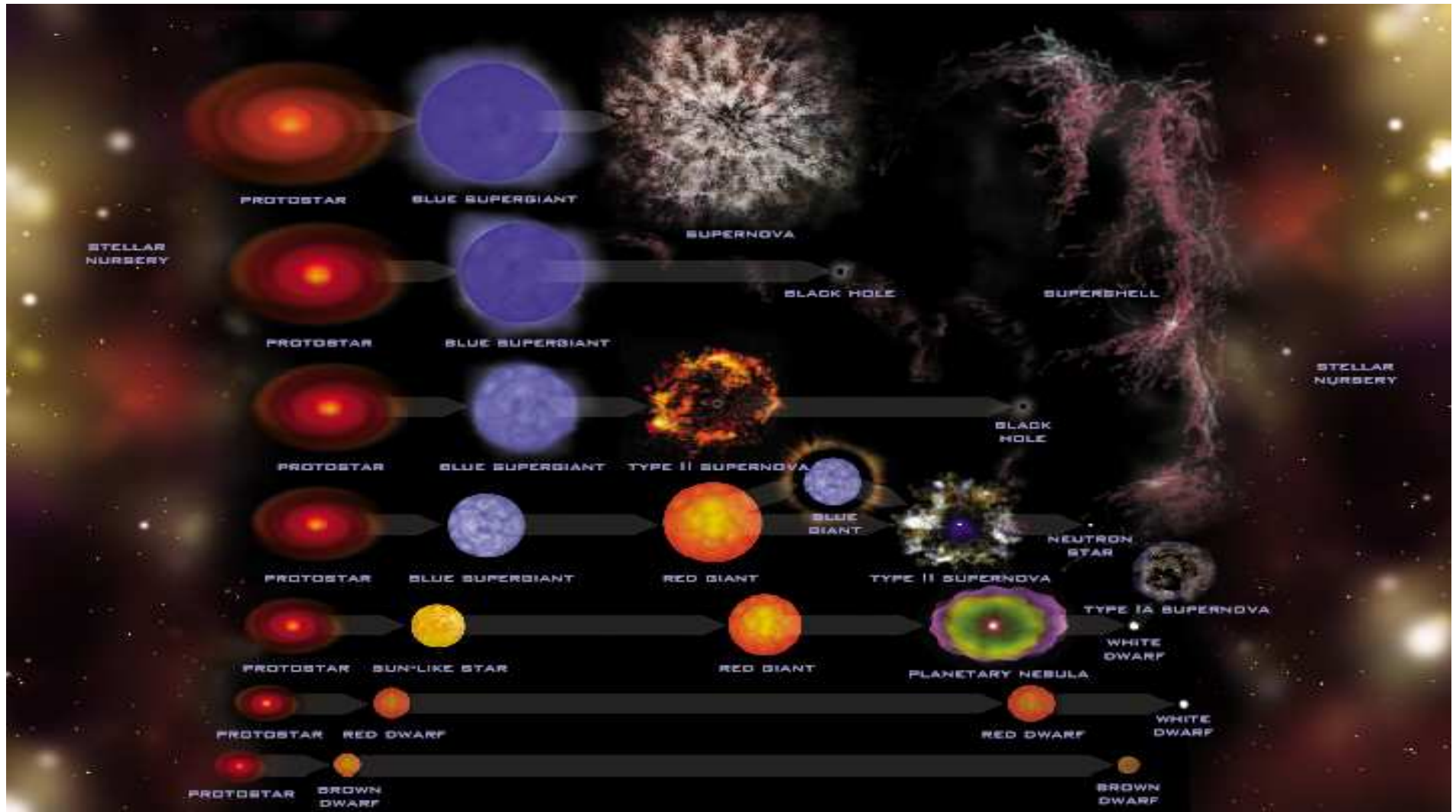
Supernova Explosions (15 M_⊙):



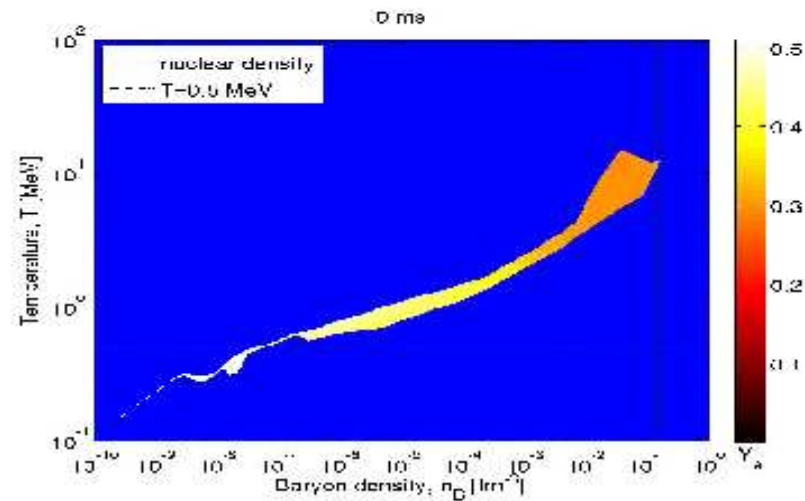
Liebendoefer et al. (2005)

Sagert et al., PRL 102 (2009)

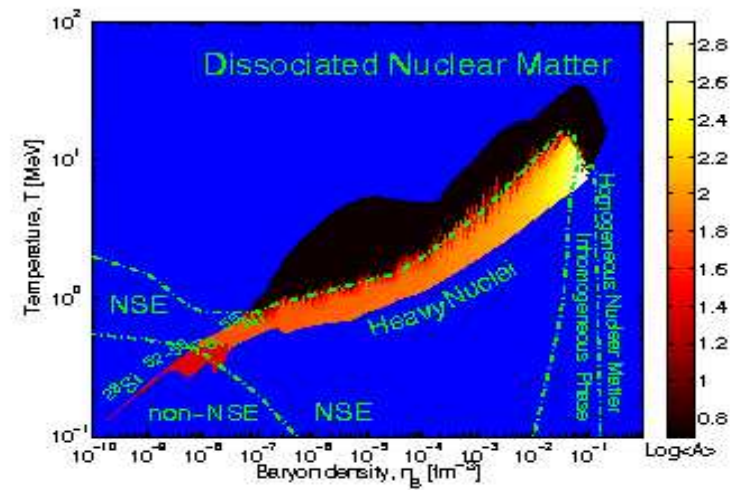
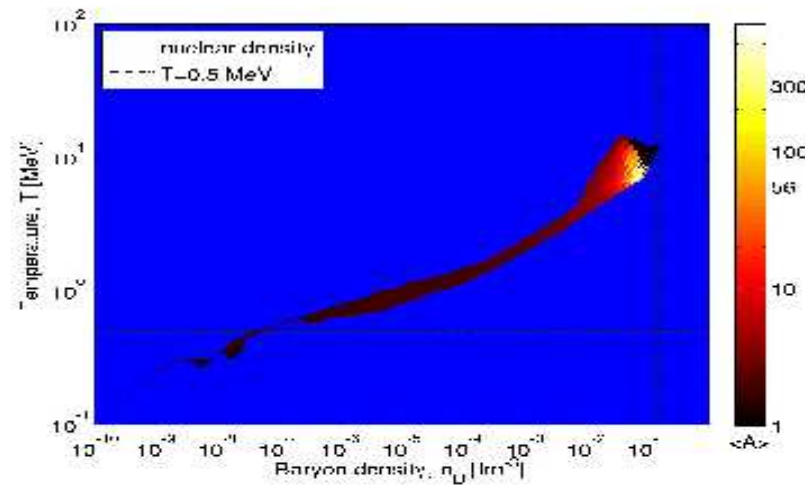
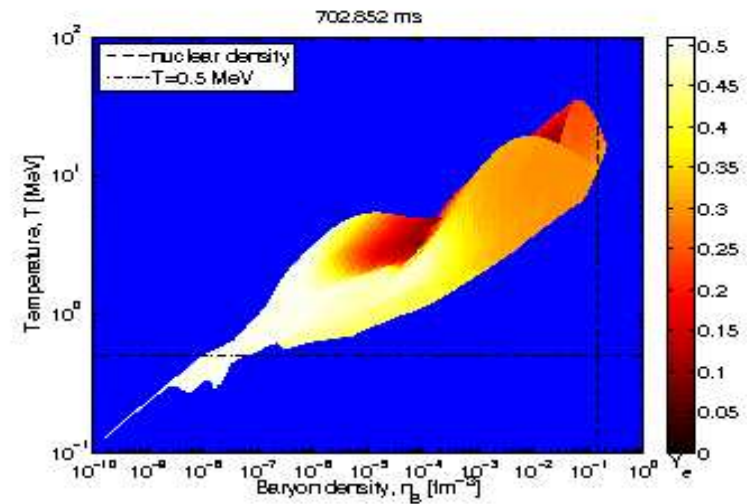
SUPERNOVAE - COMPACT STARS - BLACK HOLES



SUPERNOVA POSTBOUNCE EVOLUTION IN THE PHASE DIAGRAM

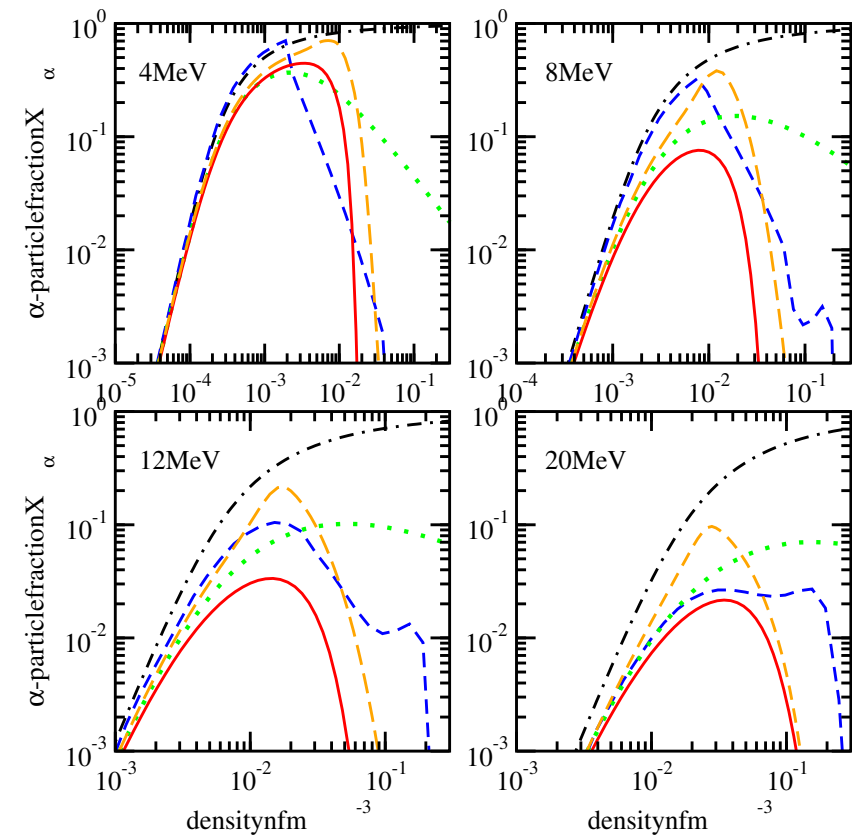
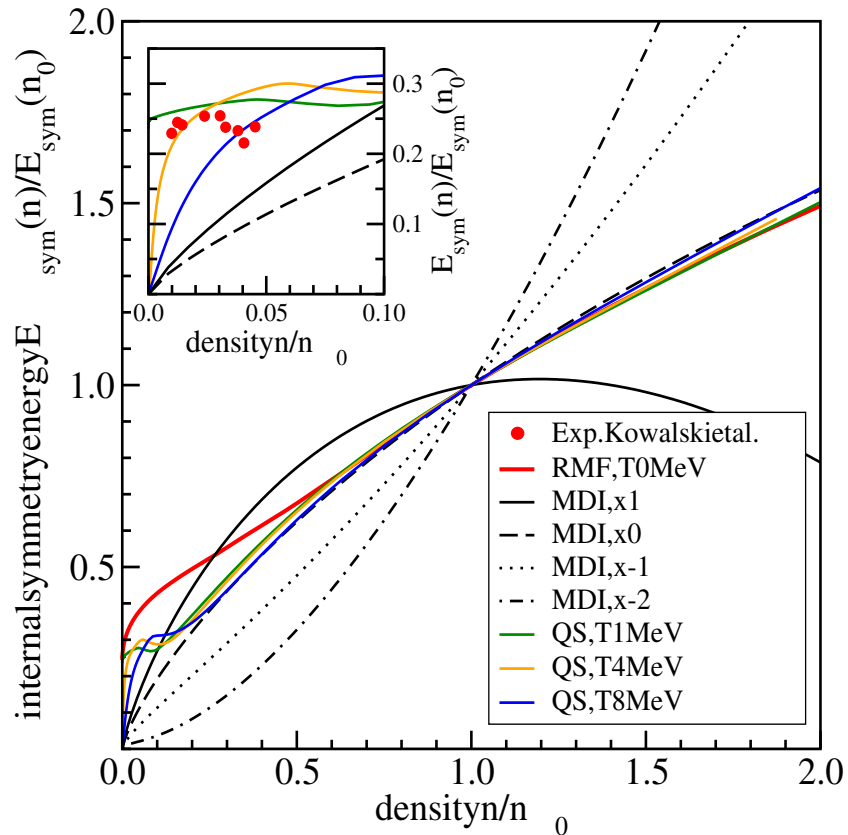


(Loading animation)



T. Fischer, D.B., et al., Yad. Fiz. 75 (2012) [arxiv:1103.3004]

TOWARDS NEW SUPERNOVA EOS: CLUSTERS AT LOW-DENSITIES



- Clusters important in plunge phase of SN collapse ($0.01 < n/n_0 < 0.1$)
- Low-density symmetry energy with clusters describes experiment (Kowalski et al.)

Typel, Röpke, Klähn, D.B., Wolter, Phys. Rev. C81 (2010); arxiv:0908.2344 [nucl-th]
Natowitz et al. (12 coauthors), Phys. Rev. Lett. (2010); arxiv:1001.1102 [nucl-th]

BAG VS. PNJL MODEL IN THE PHASE DIAGRAM

Figure: The MIT bag model^a, $Y_p \simeq 0.3$

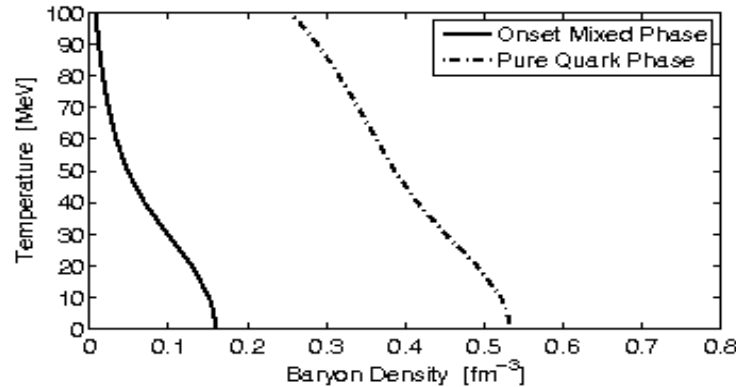
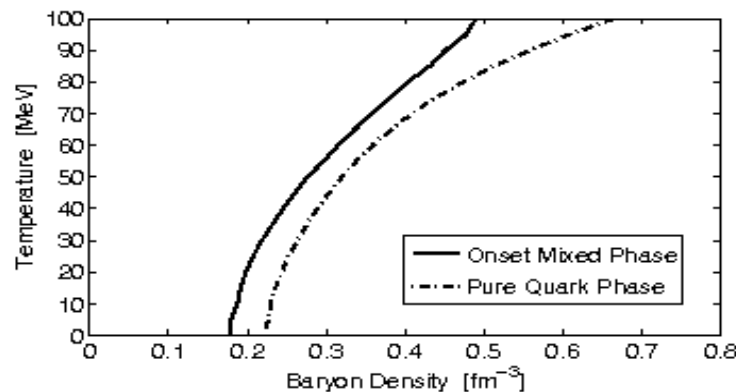


Figure: The PNJL model^b, $Y_p \simeq 0.3$



^aSagert et al. (2009)

^bSandin and Blaschke (2008)

Quark matter descriptions and the mixed phase

- 1 The MIT bag model
(Fermi-gas, the bag pressure B defines confinement)

$$B^{1/4} = 145, \dots, 200 \text{ MeV}$$
- 2 The PNJL model
(Based on the QCD Lagrangian)
 - Similar critical densities:
 - $n_c(T \simeq 0) \simeq 0.17 \text{ fm}^{-3}$ (MIT bag)
 - $n_c(T \simeq 0) \simeq 0.18 \text{ fm}^{-3}$ (PNJL)
 - Different behavior of the critical density for finite T
 - $n_c(T)$ reduces for increasing T (MIT bag)
 - $n_c(T)$ increases for increasing T (PNJL)
- 3 The problem: the transition from quarks confined in hadrons to the quark-gluon plasma at finite T and n_B
 - Construction of the coexistence region/mixed phase
(Maxwell construction, Gibbs conditions)
 - Thermodynamics
(required for use in astrophysical applications)

EVOLUTION OF CENTRAL MASS ELEMENTS IN SHEN/PNJL PHD

Figure: 20 M_{\odot} , non-exploding model

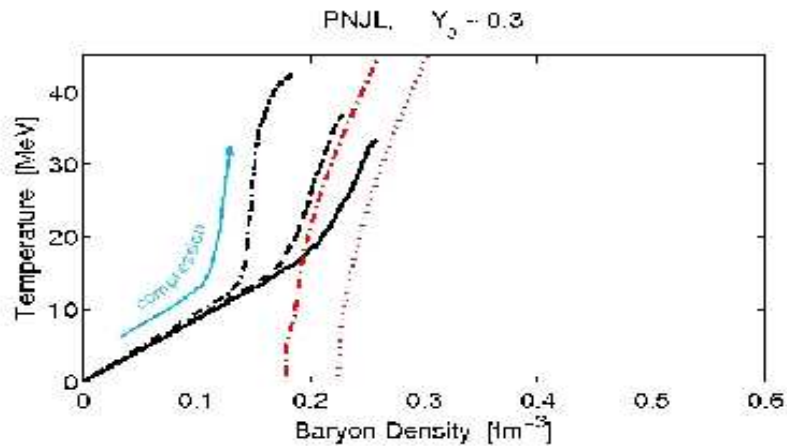
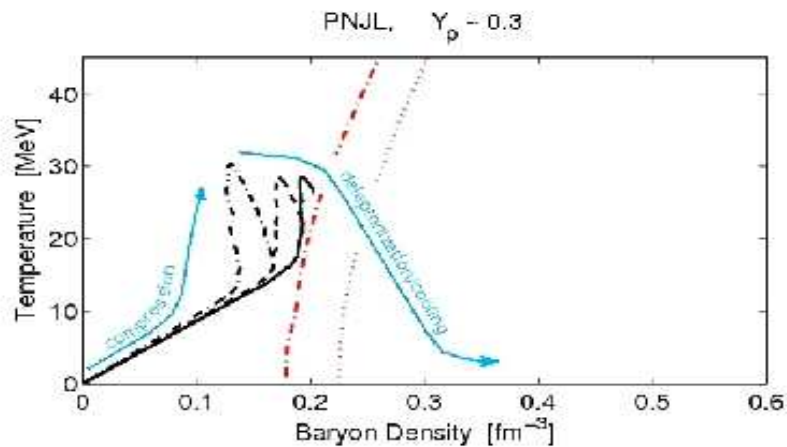


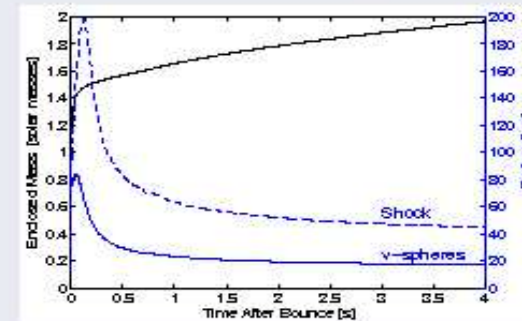
Figure: 20 M_{\odot} , ν -driven explosion



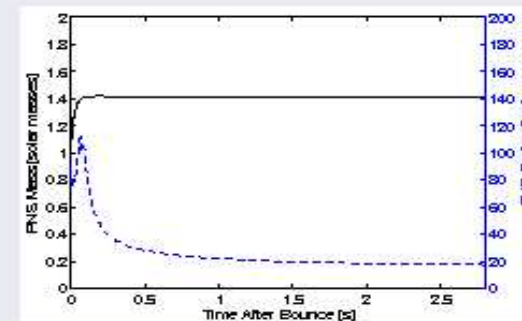
The appearance of quark matter in PNSs

1 Non-exploding models

- Central n_B and T increase on timescale ~ 1 second
- Continued rise of the enclosed mass



2 Explosion models



PHASE DIAGRAM / COMPACT STARS FOR SHEN/BAG MODEL

Figure: (MIT bag) $Y_p \simeq 0.1$, $Y_p \simeq 0.3$, $Y_p \simeq 0.5$

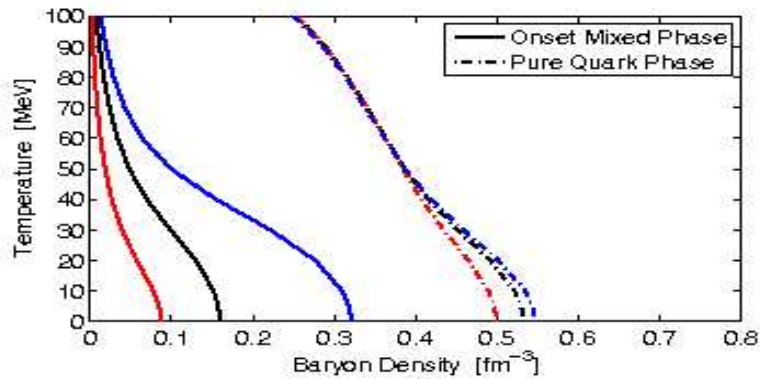
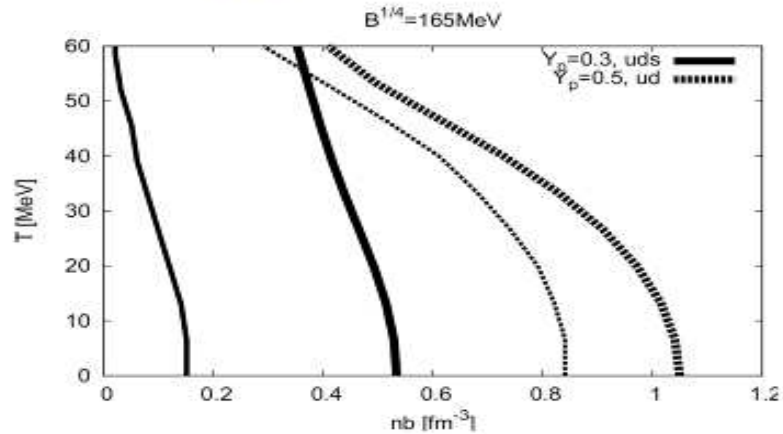


Figure: The MIT bag model

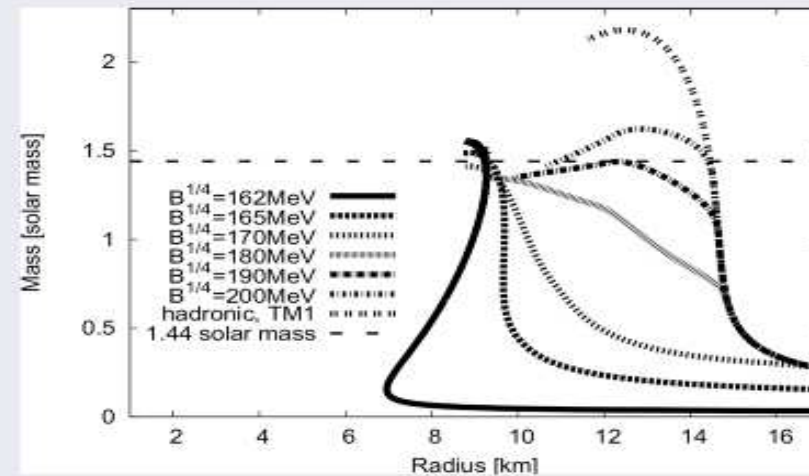


Requirements of the model and dependencies

- 1 Isospin asymmetry

$$n_c = n_c(T, Y_p)$$

- 2 Maximum Mass (Mass-Radius relation)



- 3 Consistent with data from heavy-ion collisions

- 4 Timescales to establish equilibrium
(production of strangeness)



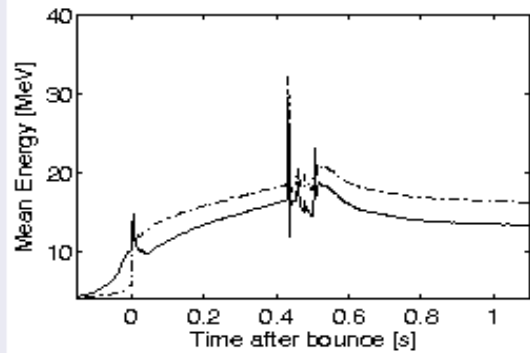
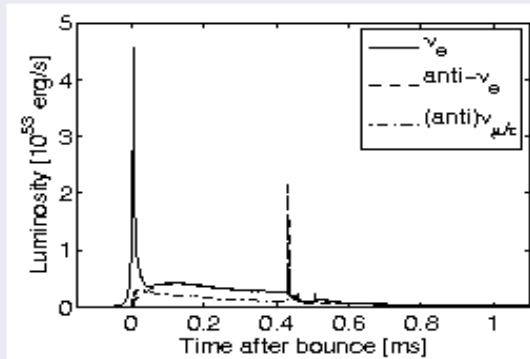
$$m_u \simeq m_d \simeq 0, m_s \simeq 100 \text{ MeV}$$

EXTRA NEUTRINO BURST FROM QUARK-HADRON TRANSITION

The neutrino observables

- ① No direct signal from the phase transition
- ② Shock crossing over the neutrinospheres

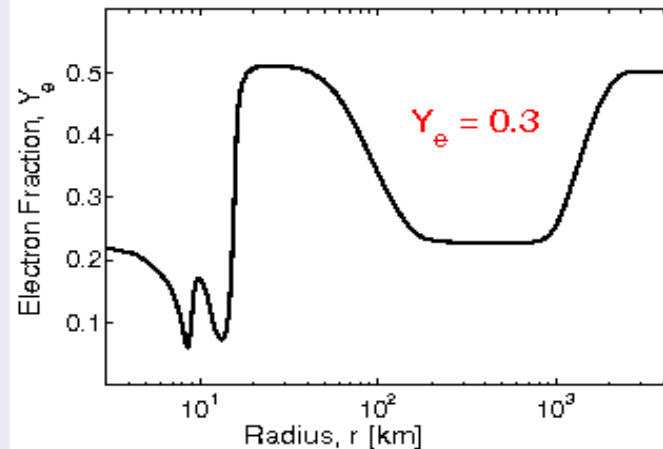
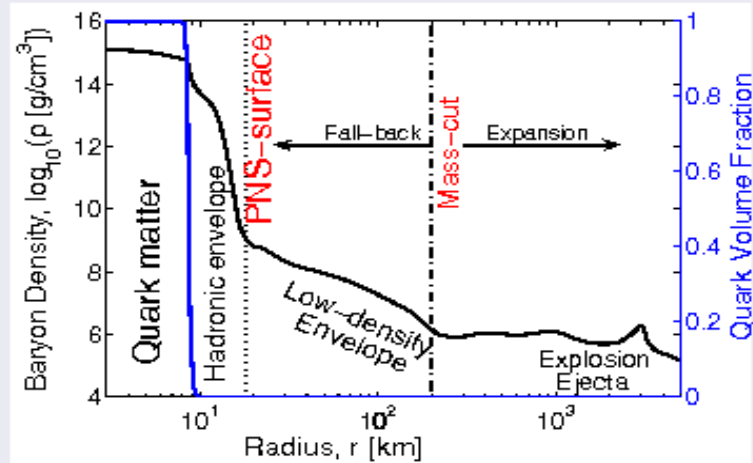
→ Neutrino burst dominated by $\bar{\nu}_e$



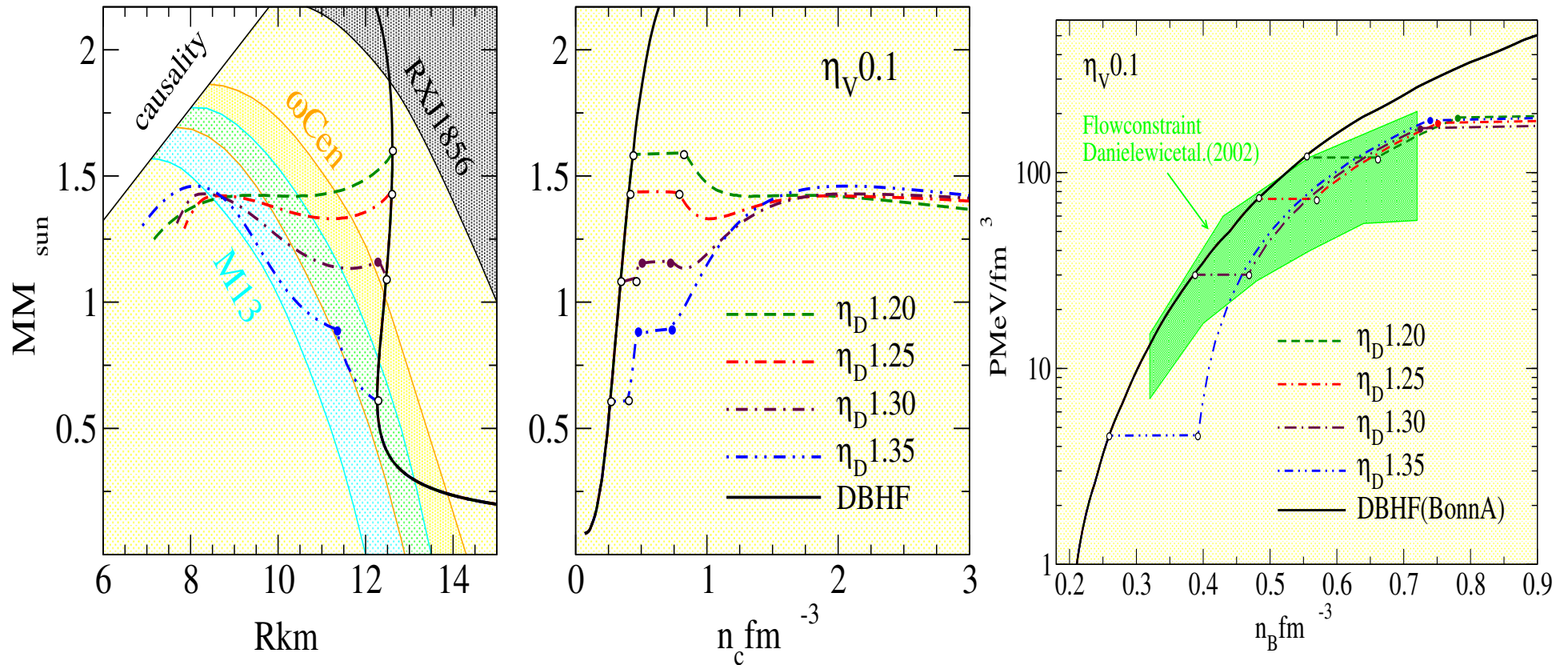
- ③ Detection of the "QCD-burst" (ICEC,SK)^a

^aDasgupta et al. (2010)

QCD degrees of freedom: possible site for the r -process



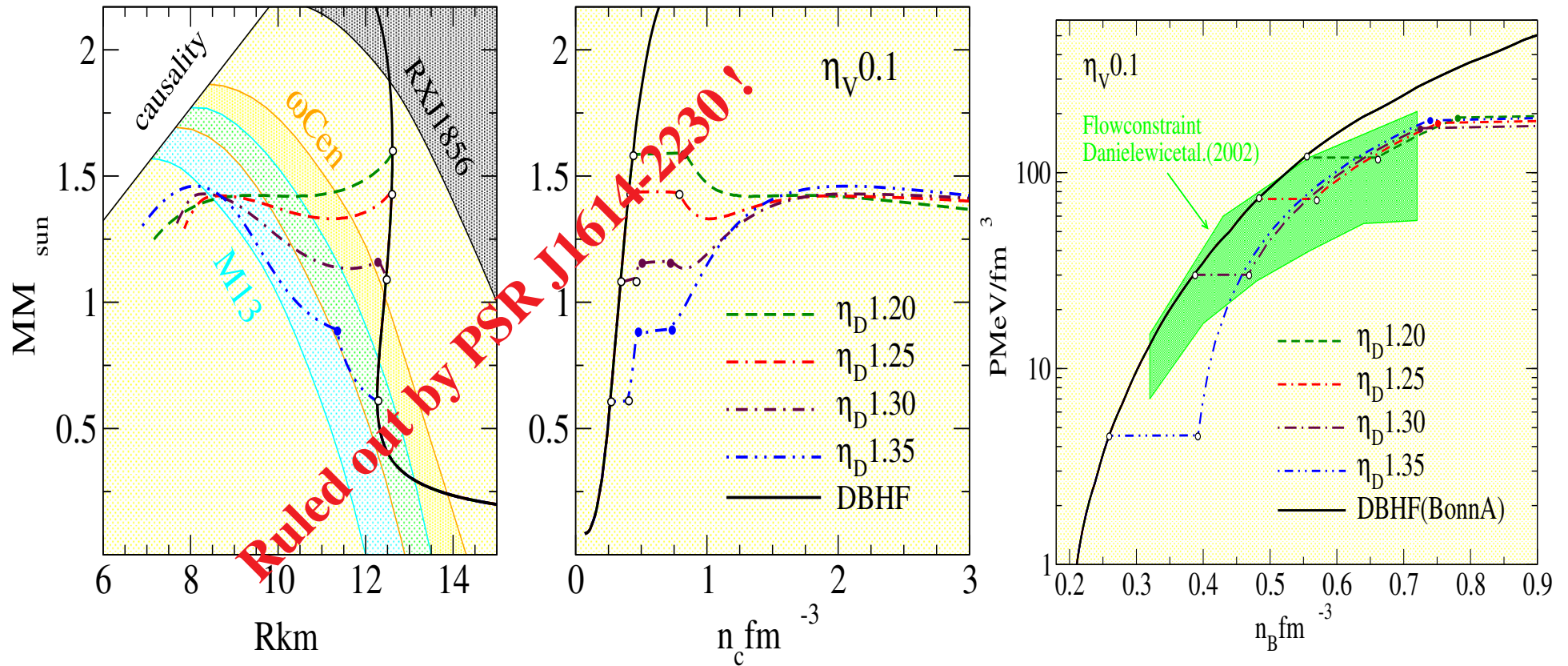
HYBRID-EOS ROBUST? ROLE OF KMT DET - TWINS!



- Mass - radius constraints from quiescent LMXB's and RXJ 1856 \Rightarrow Small AND large stars? NJL with KMT allows for mass twins! Direct transition DBHF-CFL possible!
- Flow constraint \Rightarrow PT not too early! No direct DBHF-CFL trans.!

D.B., Klähn, Łastowiecki, Sandin, J. Phys. G 37, 094063 (2010); arxiv:1002.1299 [nucl-th]

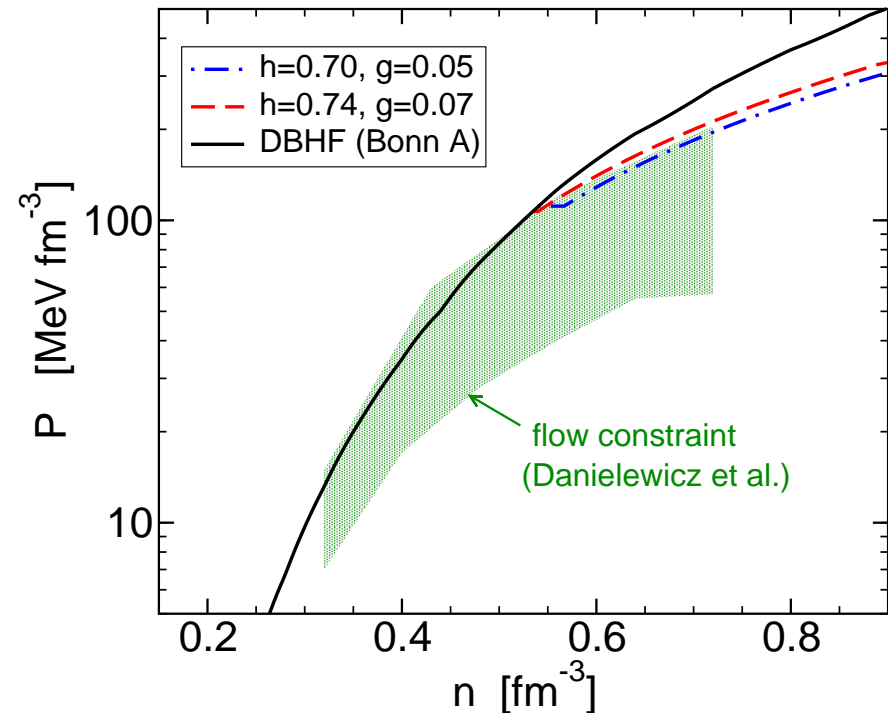
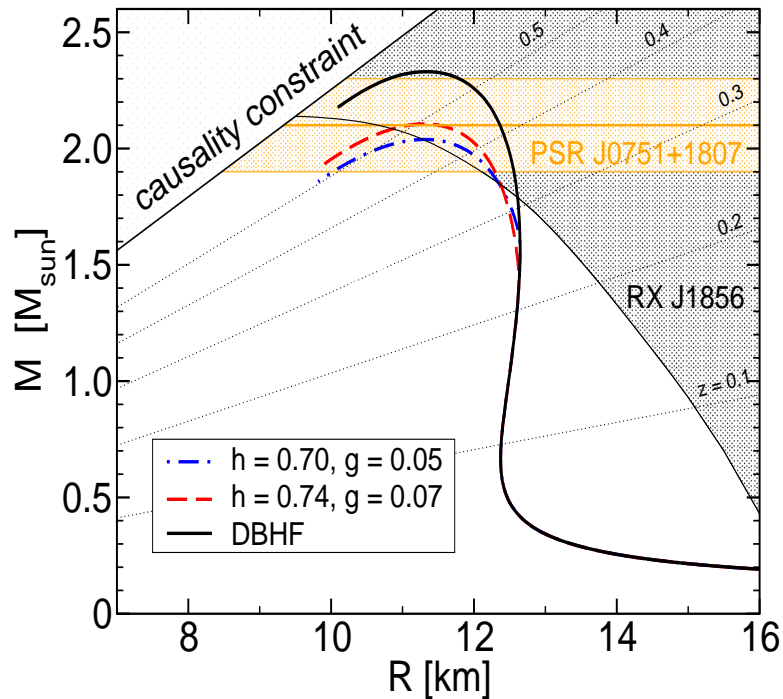
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D.B., Klähn, Lastowiecki, Sandin, *J. Phys. G* **37**, 094063 (2010); arxiv:1002.1299 [nucl-th]

HYBRID-EoS ROBUST? CONSTRAINTS & COVARIANT NCQM



- Covariant, nonlocal interaction model:

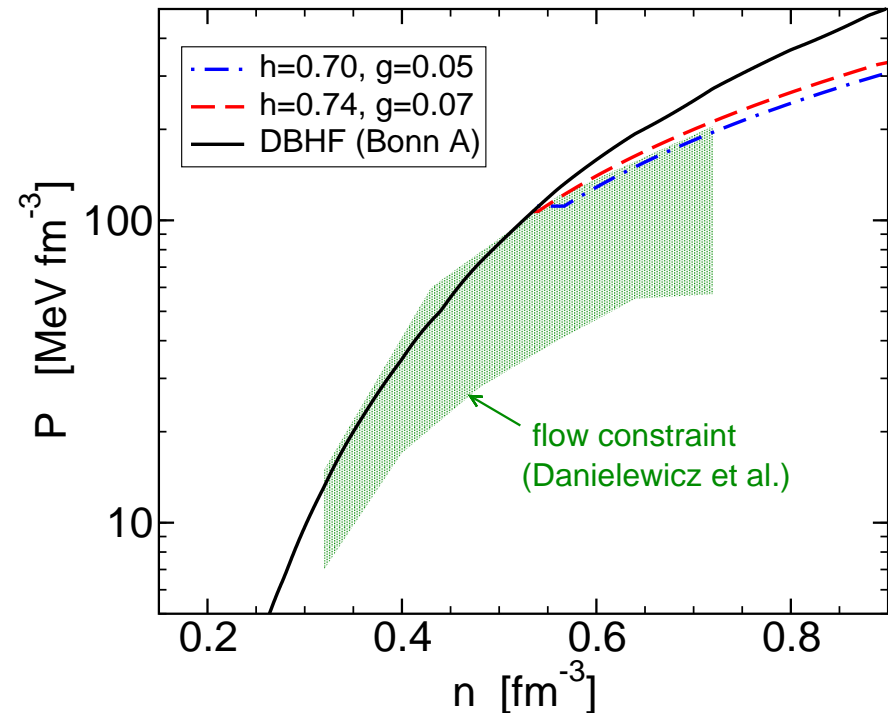
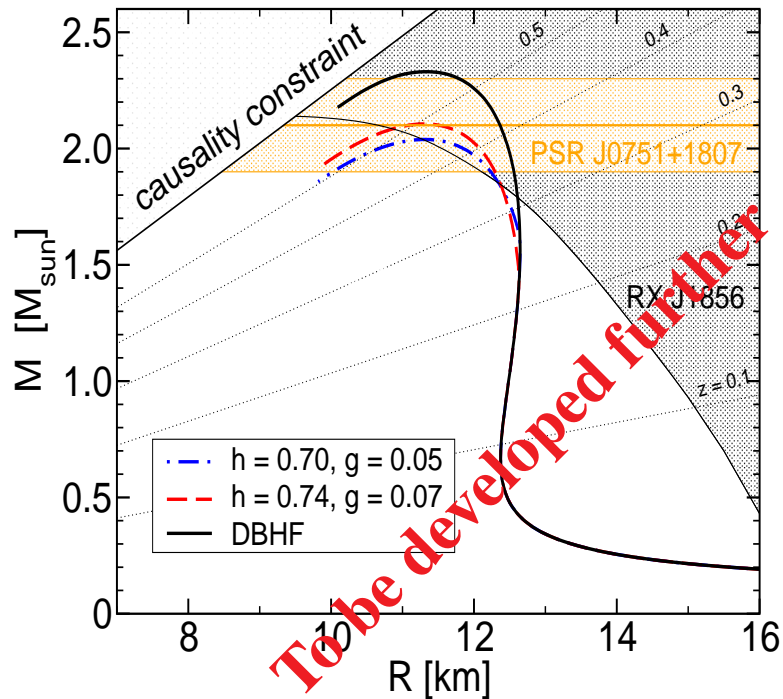
$$\mathcal{L}_{\text{int}} = - \int d^4x \left\{ \frac{G_S}{2} j_S^f(x) j_S^f(x) + \frac{H}{2} [j_D^a(x)]^\dagger j_D^a(x) + \frac{G_V}{2} j_V^\mu(x) j_V^\mu(x) \right\}$$

- Nonlocal currents, e.g.

$$j_S^f(x) = \int d^4z g(z) \bar{\psi}(x + \frac{z}{2}) \Gamma_f \psi(x - \frac{z}{2}),$$

D.B., Gomez-Dumm, Grunfeld, Klähn, Scoccola, PRC 75, 065804 (2007); [arxiv:nucl-th/0703088]
Recent developments: Radzhabov et al., arxiv:1012.0664; Horvatic et al., arxiv:1012.2113

HYBRID-EoS ROBUST? CONSTRAINTS & COVARIANT NCQM



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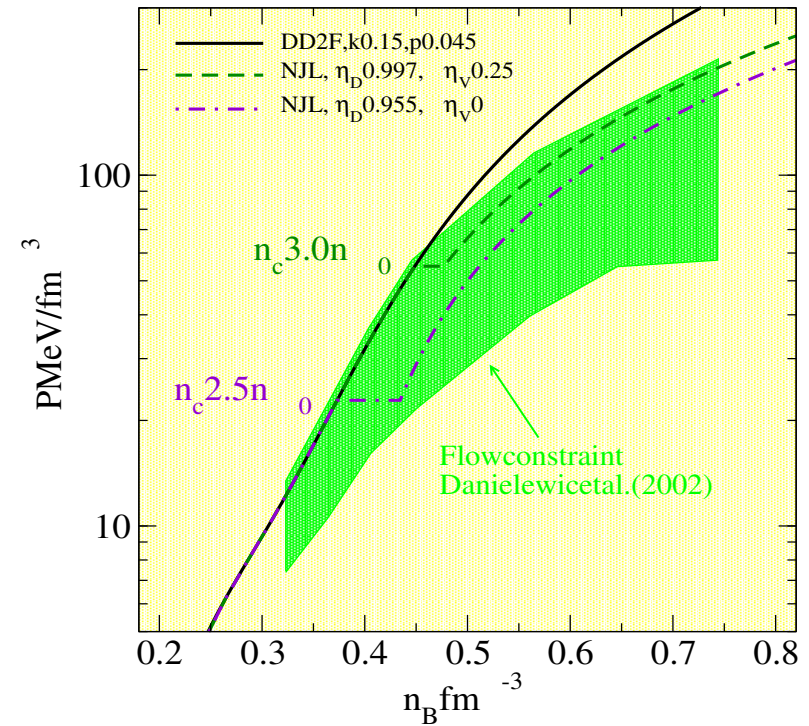
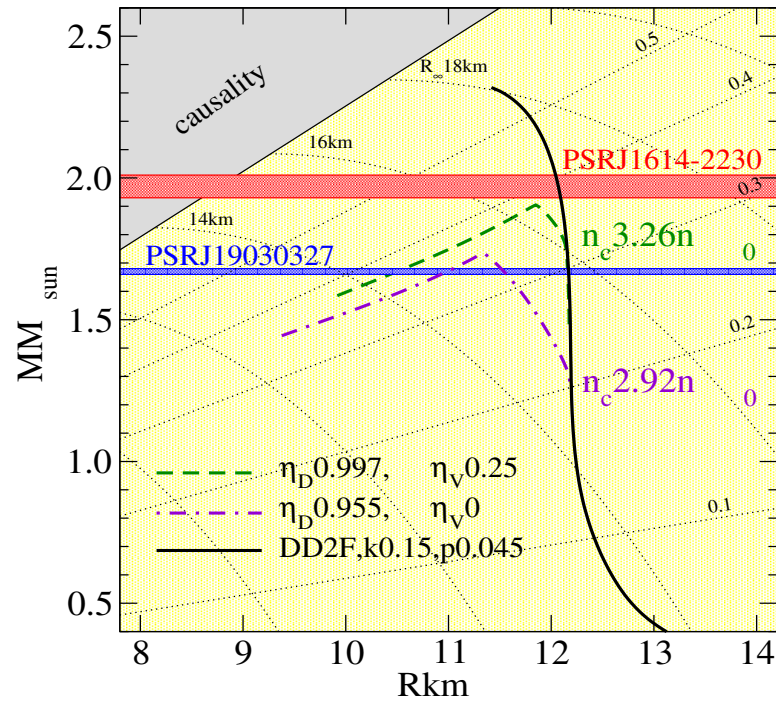
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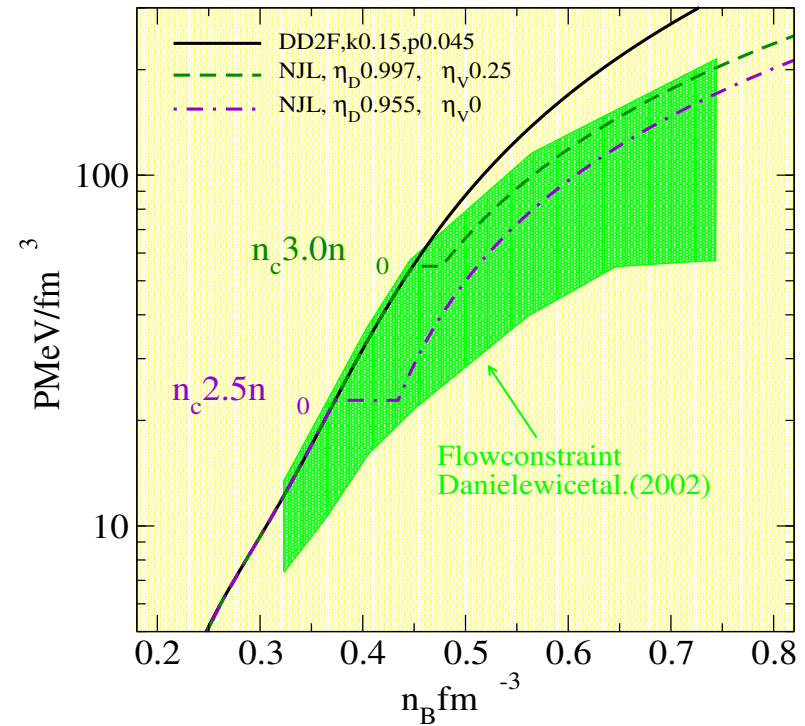
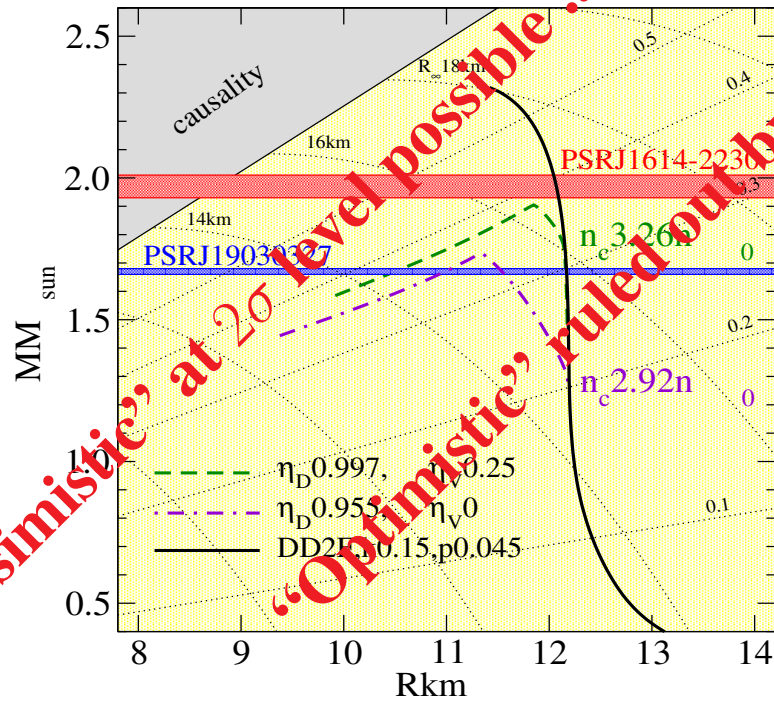
MASS-RADIUS CONSTRAINT AND FLOW CONSTRAINT



- Large Mass ($\sim 2 M_{\odot}$) and radius ($R \geq 12$ km) \Rightarrow stiff EoS;
- Flow in Heavy-Ion Collisions \Rightarrow not too stiff EoS !

**Sandin et al., CompOSE project (2009-10); See also:
 Klähn, D.B., Sandin, Fuchs, Faessler, Grigorian, Röpke, Trümper, PLB 654, 170 (2007)**

MASS-RADIUS CONSTRAINT AND FLOW CONSTRAINT

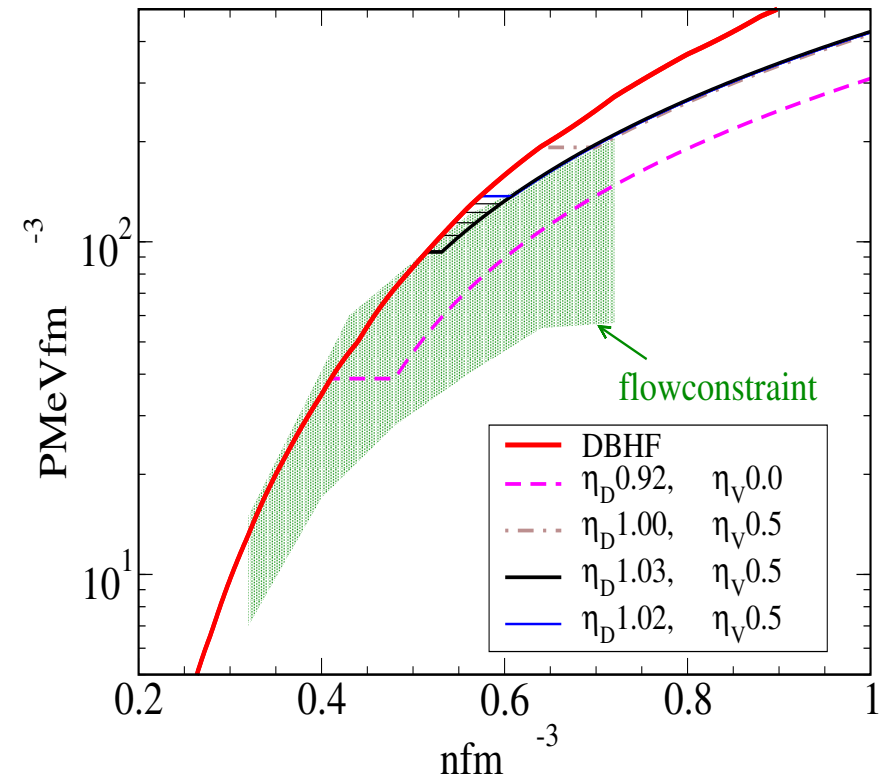
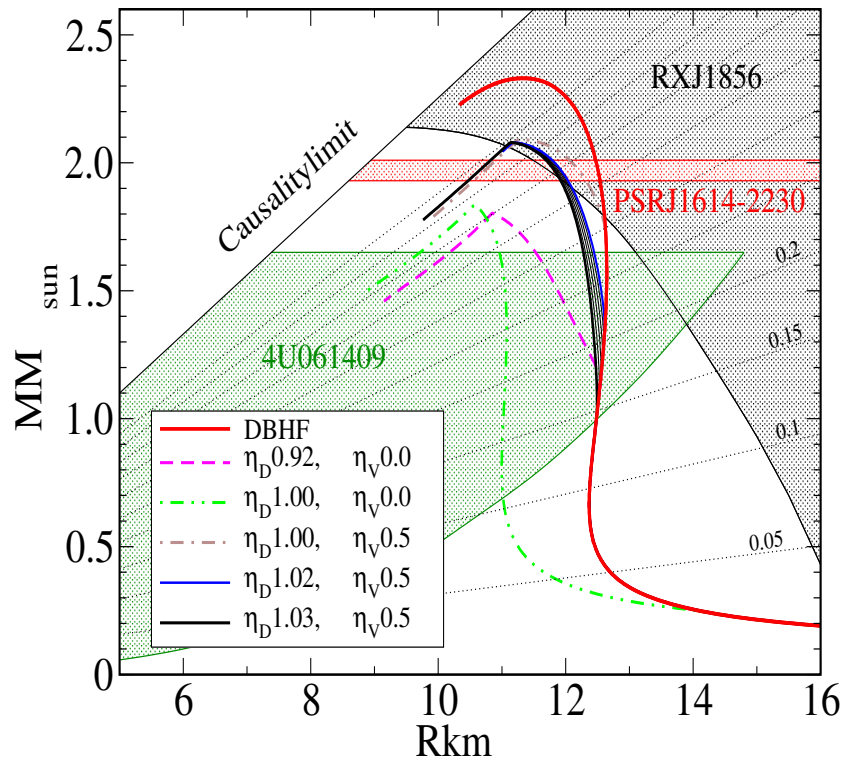


- Large Mass ($\sim 2 M_{\odot}$) and radius ($R \geq 12$ km) \Rightarrow stiff EoS;
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 Klähn, D.B., Sandin, Fuchs, Faessler, Grigorian, Röpke, Trümper, PLB 654, 170 (2007)

“Pessimistic”, at 2 σ level possible ...
 “Optimistic”, ruled out by PSR J1614-2230 !

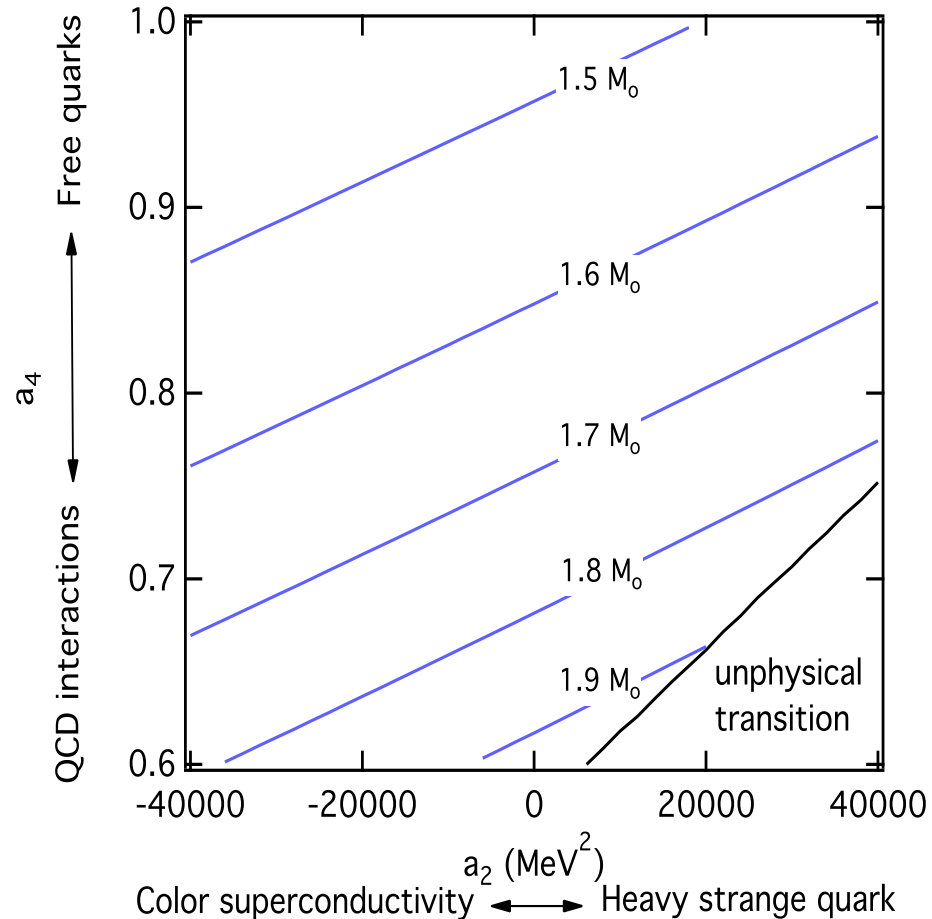
MASS-RADIUS CONSTRAINT AND FLOW CONSTRAINT



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Klähn, D.B., Sandin, Fuchs, Faessler, Grigorian, Röpke, Trümper, PLB 654, 170 (2007)

CONSTRAINTS FROM PSR J1614-2230 FOR QUARK MATTER EOS



Özel, Psaltis, Ransom, Demorest, Alford,
arxiv:1010.5790 [astro-ph] (2010)

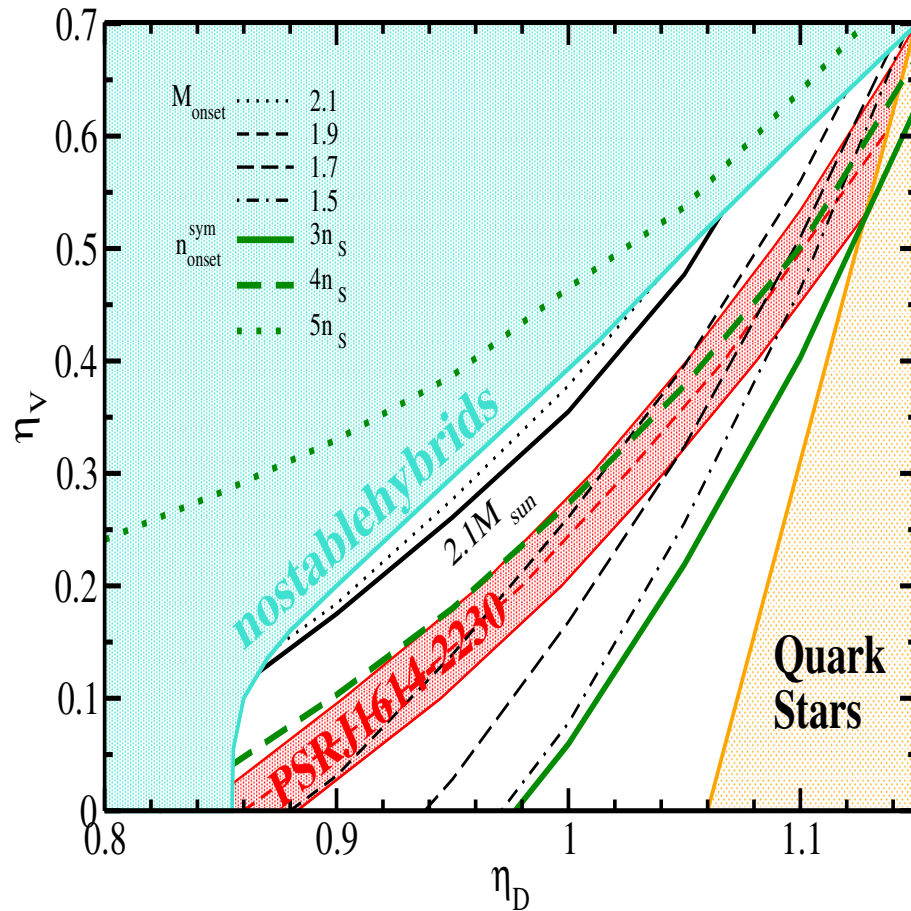
Phenomenological Quark Matter EoS:

$$\Omega_{\text{QM}} = -\frac{3}{4\pi}a_4\mu^4 + \frac{3}{4\pi^2}a_2\mu^2 + B_{\text{eff}}$$

If the critical density for chiral restoration/deconfinement is reached in the compact star core, then $M_{\text{J1614}} = 1.97 \pm 0.04 M_\odot$ implies the following:

- Quark matter is strongly interacting, QCD corrections (a_4) important
- Quark matter is color superconducting:
 $a_2 \leq 0$

CONSTRAINTS FROM PSR J1614-2230 FOR QUARK MATTER EOS

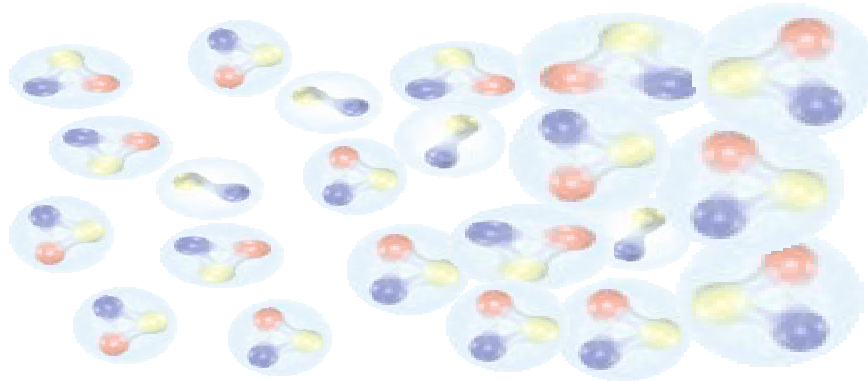


DB, Klähn, Łastowiecki, Miller; in prep. (2010)

$M_{\text{J1614}} = 1.97 \pm 0.04 M_{\odot}$ implies the following:

- KMT interaction term cannot be admitted without a compensating effect (Fierz'd KMT, change of gluon condensate (bag pressure), ...)
- If PSR J1614 is a hybrid star it must be in the 2SC phase ! No strange quarks (CFL phase) admitted !
- A maximum star mass $M_{\text{max}} \sim 1.9 M_{\odot}$ requires that the critical density for chiral restoration/deconfinement in symmetric matter is $n_{\chi} \geq 4 n_0$
- Conversely: Onset of (CSC) quark matter in compact stars at $1.5 M_{\odot}$ requires $n_{\chi} \sim 3 n_0$ in symmetric matter, but would fulfill the Demorest constraint only for extreme η_D and η_V .

WHAT HAPPENS ON “HAPPY ISLAND”?



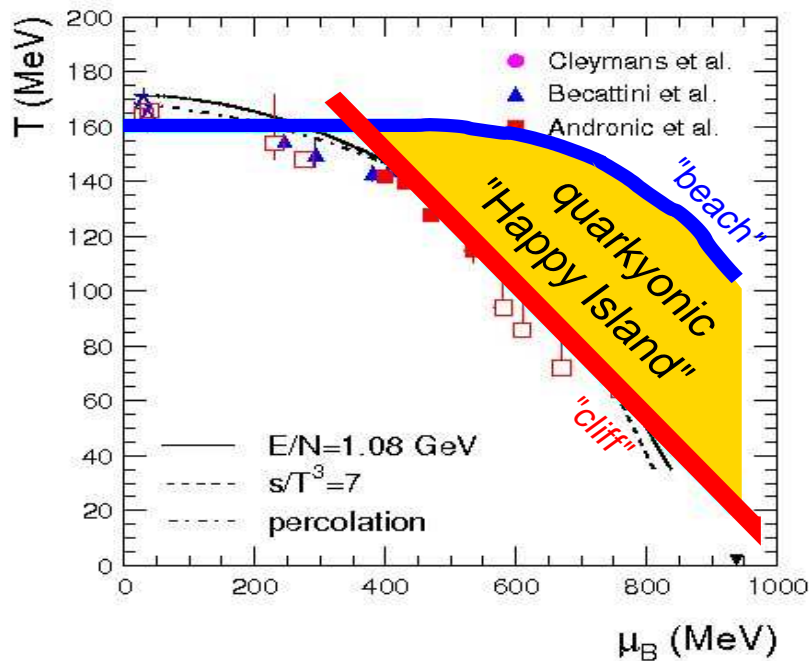
“beach”: hadron resonances \rightarrow QGP

“cliff”:

- (unmodified) vacuum bound state energies
- fast chemical equilibration

Explanation:

Andronic et al., arxiv:0911.4806



Strong medium dependence of rates for flavor (quark) exchange processes

Reason:

- lowering of thresholds
- increase of hadron size (Pauli principle)
 \rightarrow geometrical overlap (percolation)

D.B., Berdermann, Cleymans, Redlich, Part. Nucl. Phys. Lett. (2011), arxiv:1102.2908; Few Body Syst. (2011) arxiv:1109.5391

COMPOSE - COMPSTAR ONLINE SUPERNOVA EOS

Reference manual
version 1.0

CompOSE

CompStar Online Supernovæ Equations of State

fertilising the fields of nuclear physics and astrophysics

www.compstar-esf.org/compose*
compose@compstar-esf.org[†]

European Science Foundation
Research Networking Program
CompStar

November 22, 2010

General Requirements:

- Densities: $10^{-8} \leq n/n_0 \leq 10$
- Temperatures: $0 \leq T \leq 200$ MeV
- Proton fractions: $0 \leq Y_p \leq 0.6$; $\beta = 1 - 2Y_p$

New Developments:

- Dissolution of clusters due to Pauli blocking
- Realistic high-density modeling: DD-RMF/3FSC PNJL
- Thermodynamics of 1st order PT; pasta phases

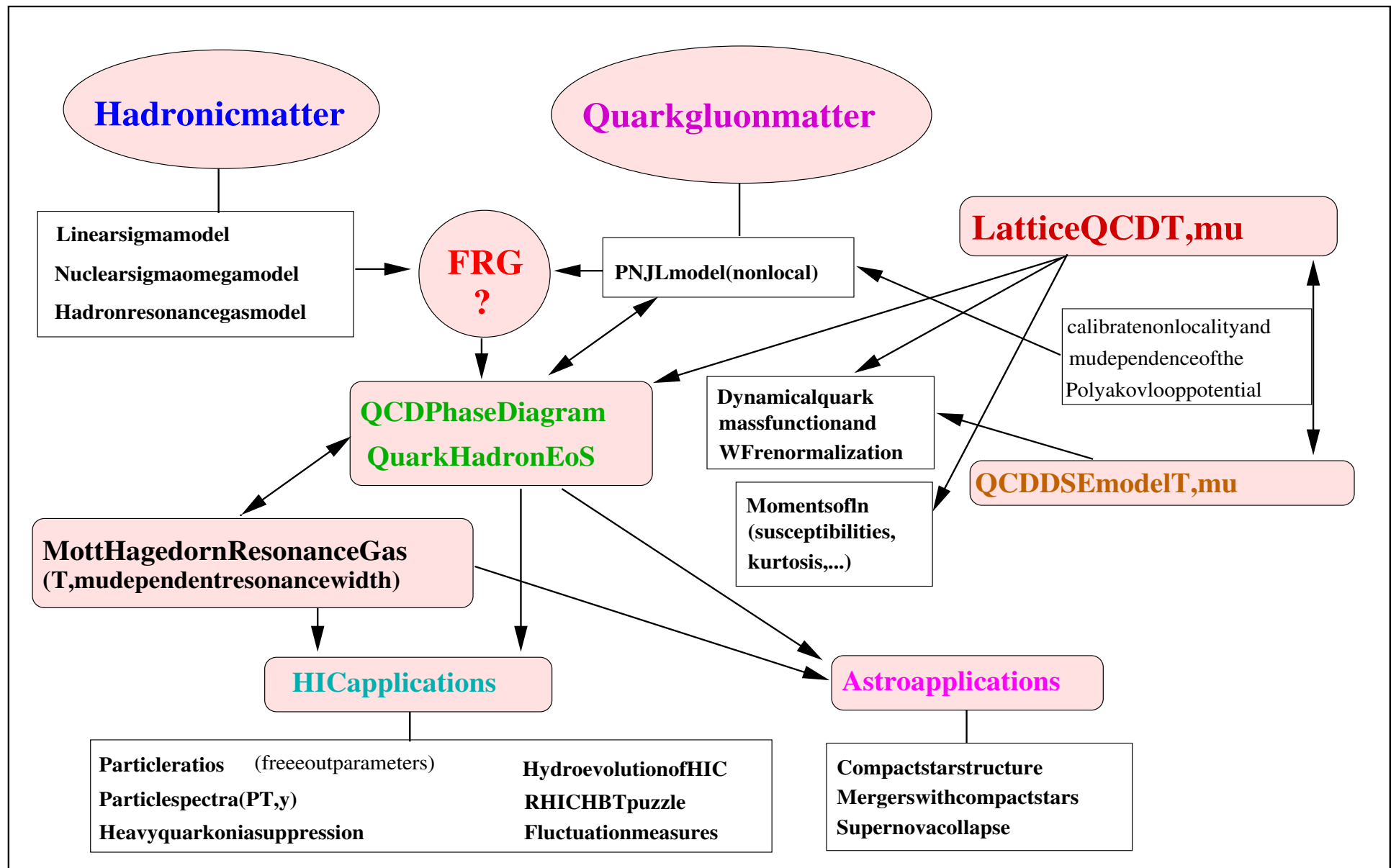
I. For Contributors:

- How to prepare EoS tables
- How to submit EoS tables
- Extending CompOSE

II. For Users:

- Hadronic EoS: Statistical, Skyrme, DBHF, ...
- Quark Matter EoS: Bag, PNJL, ...
- Phase transition: Maxwell, Gibbs, Pasta, ...

ROADMAP FOR PHASE DIAGRAM AND EOS RESEARCH



SUMMARY

- Hadron production in HIC → Triple point in QCD phase diagram!
- Compressed nuclear matter: **quarkyonic phase (QP)**! Coexisting chiral symm. + conf.
- Here: PNJL model as microscopic formulation of the QP
- Prospects for HIC (CBM & NICA) and Supernovae: color superconducting (quarkyonic) phases accessible!

OUTLOOK: NEXT STEPS ...

- Walecka model as limit of PNJL model: chiral transition effects in nuclear EoS
- Beyond meanfield: mesons and baryons in the PNJL, higher clusters: sextetting
- Astrophysics: Maximum mass & cooling of quarkyonic stars; quarkyonic supernovae
- HIC: signals of CSC phase transition (dilepton enhancement?)

INVITATION: CONTRIBUTE TO THE NICA WHITE PAPER



Draft v 3.03

June 20, 2010

SEARCHING for a QCD MIXED PHASE at the NUCLOTRON-BASED ION COLLIDER FACILITY (NICA White Paper)

<http://theor.jinr.ru/twiki-cgi/view/NICA/WebHome>

<http://theor.jinr.ru>

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INVITATION: VISIT WROCLAW & UNIVERSITY

