

# Diffractive Processes at High Energies.

A.B. Kaidalov  
ITEP, Moscow

## Contents:

- Introduction.
- Pomeron in QCD.
- Diffraction and small- $x$  physics.
- Hard diffraction in hadronic interactions
- Double Pomeron jet production.
- Conclusions.

## ● Introduction

(2a)

Study of diffractive processes gives an important information on both nonperturbative and perturbative QCD dynamics.

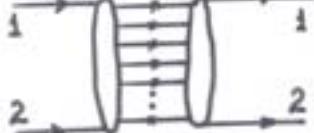
Problems of QCD in nonperturbative region: confinement, chiral symmetry violation. Structure of QCD vacuum.

Some important problems of diffraction:

- The nature of the Pomeron in QCD
- Role of s-channel unitarity and multipomeron exchanges
- QCD and Regge factorizations and their violation in diffractive processes
- Small- $x$  problem and "saturation" of partonic densities as  $x \rightarrow 0$ . Relation to heavy ion collisions.
- Transition from hard to soft regimes

(2)b

- Two complementary views on diffraction
- S-channel view of diffraction.



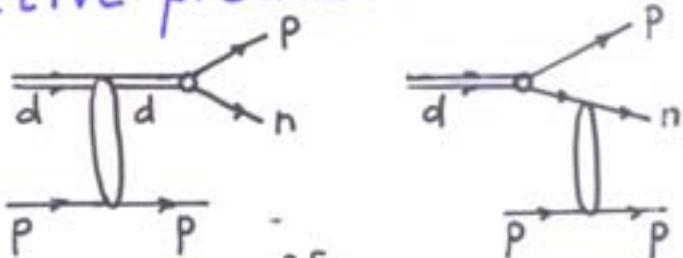
Absorption of an initial wave due to many inelastic channels leads by unitarity to diffractive elastic scattering.

Diffraction is a process, which has a long lifetime  $\tau \sim E_\perp / \mu^2$

E. Feinberg, T. Ya. Po-  
meranchuk

Diffractive production

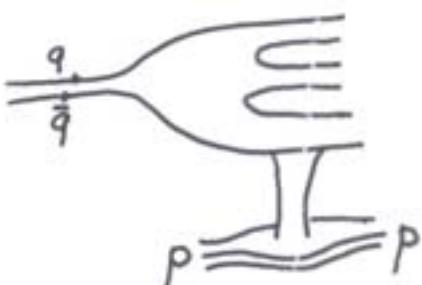
Example  
Dissociation  
of a deuteron



$$\Delta t \approx \frac{2E_\perp}{M^2 - m_d^2}$$

Inelastic diffraction is due to a difference of amplitudes and is smaller compared to elastic scattering.

Dissociation of a hadron into  $q\bar{q}$ -pairs (color dipoles).



(3)

Good and Walker interpretation  
of diffraction.

Diffractive part of  $S$ -matrix  $iD_{ik}^{(s,b)}$   
can be diagonalized by an orthogonal  $Q$   $\uparrow$   
 $\uparrow$   
impact parameter

$$D = Q F Q^T ; \quad F_{ij} = F_i \delta_{ij}$$

$\Psi_i = \sum_k Q_{ik} \varphi_k$  ;  $\varphi_k$  - eigenstates, which  
 $\Psi_1$  - initial state. have only elastic scat.  
 $\downarrow$   
Quark configurations with  
fixed transverse separations.

After diffractive scattering (with  $\hat{F} \neq \hat{I} \cdot F$ )  
a final state is a new superposition of eigen-  
states and thus contains  $\Psi_i$  (with  $i=1, 2, \dots, N$ )

Analog of  $K_L \rightarrow K_S$  regeneration, where  
 $K^\circ$  and  $\bar{K}^\circ$  are "diagonal" states.

If all  $F_i = \frac{1}{2}$  ( $b \leq R$ ) - black disc limit  
- inelastic diffraction is absent.

For  $F_i \leq \frac{1}{2}$

$$\sigma^{(el)}(b,s) + \sigma_D^{(in)}(b,s) \leq \frac{1}{2} \sigma^{(tot)}(b,s) \quad \text{Pumplin's bound}$$

(4)

Diffractive production is related to the dispersion in the absorption of the diffractive eigenstates

$$G_D^{\text{in}}(s, b) = 4(\langle F^2 \rangle - \langle F \rangle^2)$$

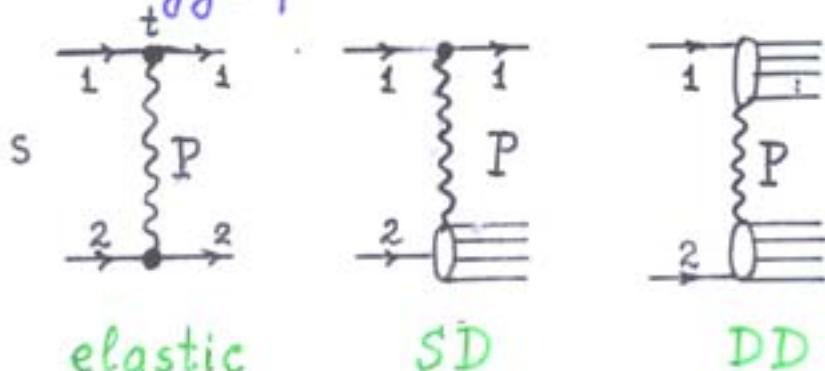
For strong absorption diffractive production is peripheral in  $b$ .

In QCD eigen states - dipoles with definite transverse sizes  $\tau_\perp$ .

For small  $\tau_\perp$   $F \sim \tau_\perp^2$ . Dependence on  $s, b$ ?

- t-channel view

Regge pole model



(5)

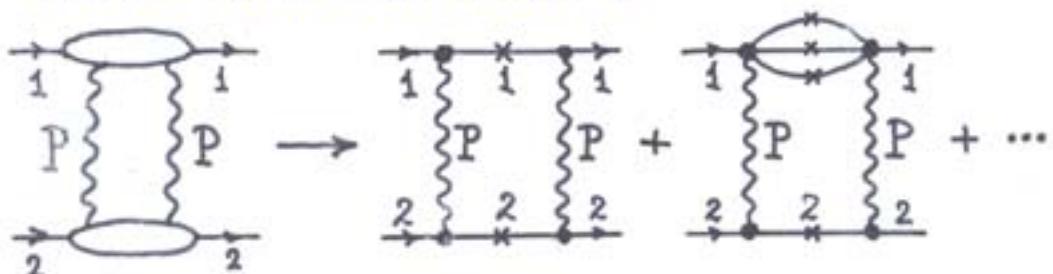
In  $b$ -space Regge amplitudes have a gaussian form.

Note that the Pomeron is very non-local object. It corresponds to the process with  $\tau \sim E/m^2$ .

Pomerons with intercept  $\alpha_P(0) > 1$  leads to a violation of unitarity ( $s \rightarrow \infty$ ).

Regge cuts (multi-Pomeron exchanges in the  $t$ -channel) restore s-channel unitarity.

Gribov's technique for evaluation of cuts contributions

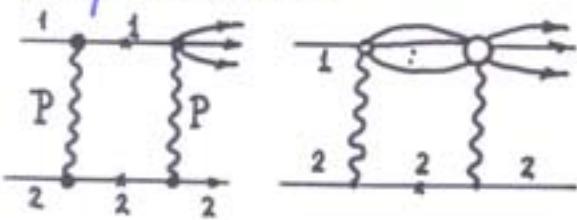


Becomes equivalent to GW formulation, but with known  $s$ -dependence

⑥

Multipomeron contributions to elastic amplitudes are related to amplitudes of diffractive processes.

For inelastic diffraction effects of multipomeron cuts are even more important.



They lead to a peripheral form of amplitudes in  $b$ -space.

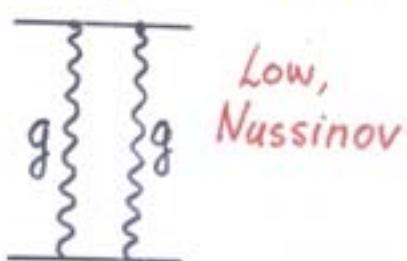
Gribov diagramme technique and AGK-cutting rules allow for systematic study of multipomeron cuts in diffractive processes and multiparticle production.

Thus an investigation of diffractive processes gives an information on structure hadronic fluctuations and a mechanism of high energy interactions.

## ● Pomeron in QCD

(7)

In QCD the Pomeron is usually related to gluonic exchanges in the t-channel

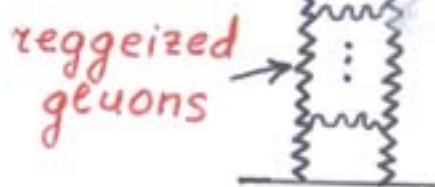


$$\alpha_P(0) = 2S_g - 1 = 1$$

In QCD perturbation theory ladder-type diagrams are important

- BFKL-Pomeron

$$\text{In LO } (\alpha_s \ln \frac{s}{s_0})^n$$



$$\Delta \equiv \alpha_P(0) - 1 = \frac{12 \ln 2}{\pi} \alpha_s; \quad \Delta \approx 0.5$$

Large NLO corrections

V. Fadin, L. Lipatov

Sources of these corrections were discussed

S. Brodsky et.al

Iterative method of solution of BFKL equation (LO and NLL0) J. Andersen

(8)

What is the role of nonperturbative effects?

Are there glueballs on the Pomeron trajectory?

- These problems were investigated in the nonperturbative Wilson loop approach.

A.K, Yu. Simonov

In this framework usual  $(q\bar{q} - \beta_1 A_2, \dots)$  trajectory are calculated and agree with experiment.

Predicted spectrum of glueballs in a good agreement with lattice results.

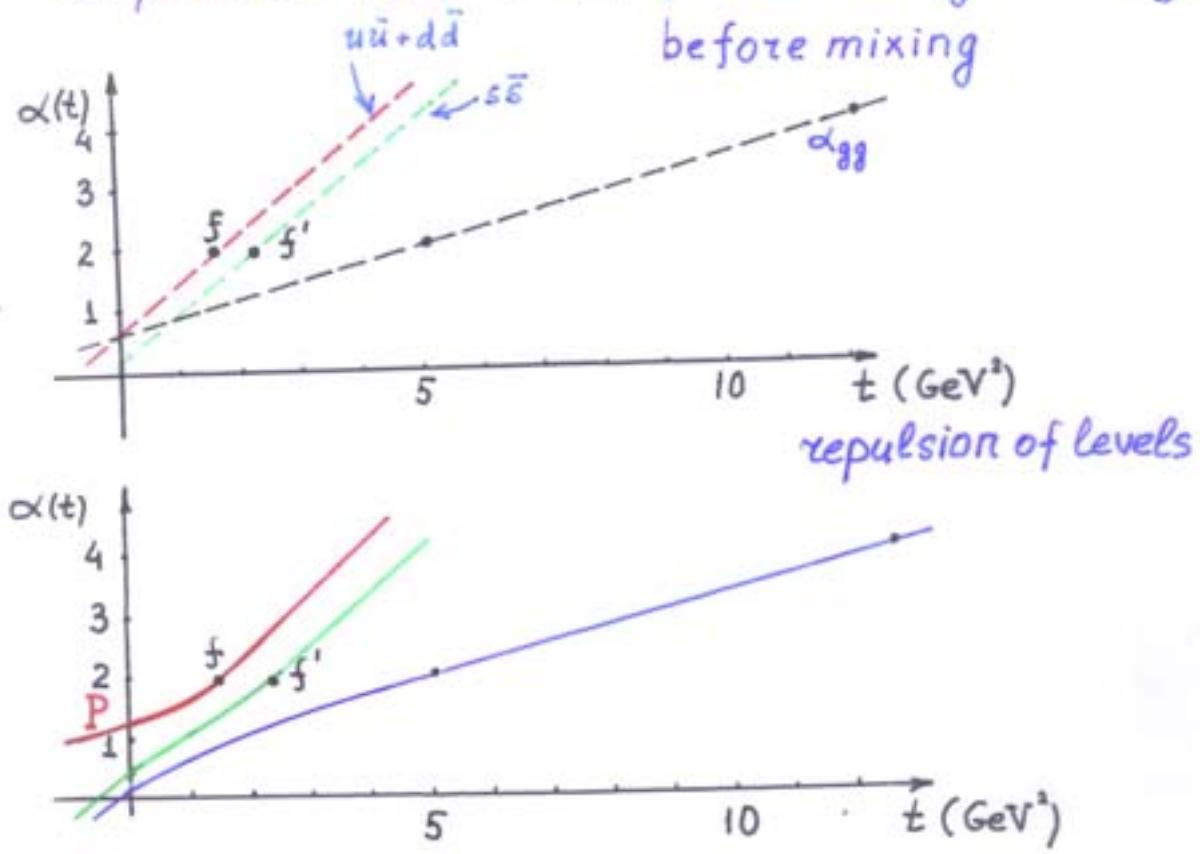
The lowest state  $0^+$   $M = 1.58 \text{ GeV}$

Slope of gg-trajectories  $\alpha'_{gg} = \frac{4}{3} \alpha'_{q\bar{q}} = 0.4 \text{ GeV}^{-2}$

Mixing of gg and q $\bar{q}$  trajectories in the small-t region

Important role of  $q\bar{q}$ -gluons mixing.

(9)



After mixing and account of semihard interactions of gluons

$$\alpha_p(0) = 1.15 \div 1.25$$

Very rich physics of the Pomeron  
(confinement, glueballs, quark-gluon mixing,  
chiral sym. and role of pions, semihard  
interactions)

Note that in this approach Pomeron contains both soft and hard effects

- physical Pomeron.

In the region  $p_\perp < 1 \text{ GeV}$  notion of point-like quarks and gluons is not a relevant one

- New areas of applications

- a) Small- $x$  physics.

Studied experimentally in  $e p (\mu p, \nu p)$  interactions.

New data from  $e p$  collider - HERA allow to investigate the region of very small  $x$

$$Q^2 = -q^2 ; \quad x = \frac{Q^2}{2pq} = \frac{Q^2}{W^2 + Q^2} \quad (W^2 \gg m^2)$$

$$W^2 \equiv S = (p+q)^2$$

$$\sigma_{\gamma^* p}^{(\text{tot})}(W^2, Q^2) = \frac{4\pi^2 \alpha_{\text{em}}}{Q^2} F_2(x, Q^2)$$

For large  $Q^2$

$$F_2(x, Q^2) = \sum_i e_i^2 x (q_i(x, Q^2) + \bar{q}(x, Q^2))$$

Experiments at HERA demonstrated

- Fast increase of  $F_2(x, Q^2)$  as  $x \rightarrow 0$

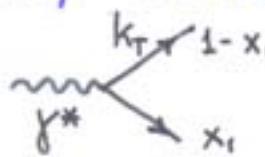
$$\sigma_{\gamma^* p}^{(\text{tot})} \sim \left(\frac{1}{x}\right)^{\lambda(Q^2)} = \left(\frac{W^2}{Q^2}\right)^{\lambda(Q^2)}$$

$\lambda(Q^2)$  increases with  $Q^2$  and  $\approx 0.3$  at  $Q^2 \sim 10^2 \text{ GeV}^2$

Diffractive dissociation of  $\gamma^*$  exists even at large  $Q^2$ .  $\Delta_{\text{eff}} \approx 0.2$

(14)

Two types of  $q\bar{q}$ -configurations  
of virtual photons



a) Small size

$$k_T \sim Q, z \sim \frac{1}{k_T} \sim \frac{1}{Q};$$

b) Large size

$$k_T \sim \Lambda_{QCD} \ll Q; z \sim \frac{1}{\Lambda}$$

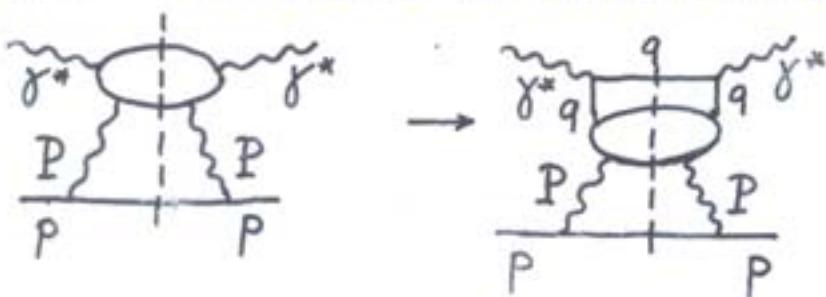
$$\sigma_s \sim \frac{1}{Q^2}; \sigma_L \sim \frac{1}{\Lambda^2} (w_L \sim \frac{1}{Q^2})$$

The model based on this picture and Reggeon theory A. Capella, E. Ferreiro, A. K. C. Salgado gives a good simultaneous description of  $F_2$  and diffractive production ( $F_2^D$ ) in a broad region of  $Q^2$ .

(see also E. Gotsman, E. Levin, U. Maor;  
K. Golec-Biernat, M. Wüsthoff)

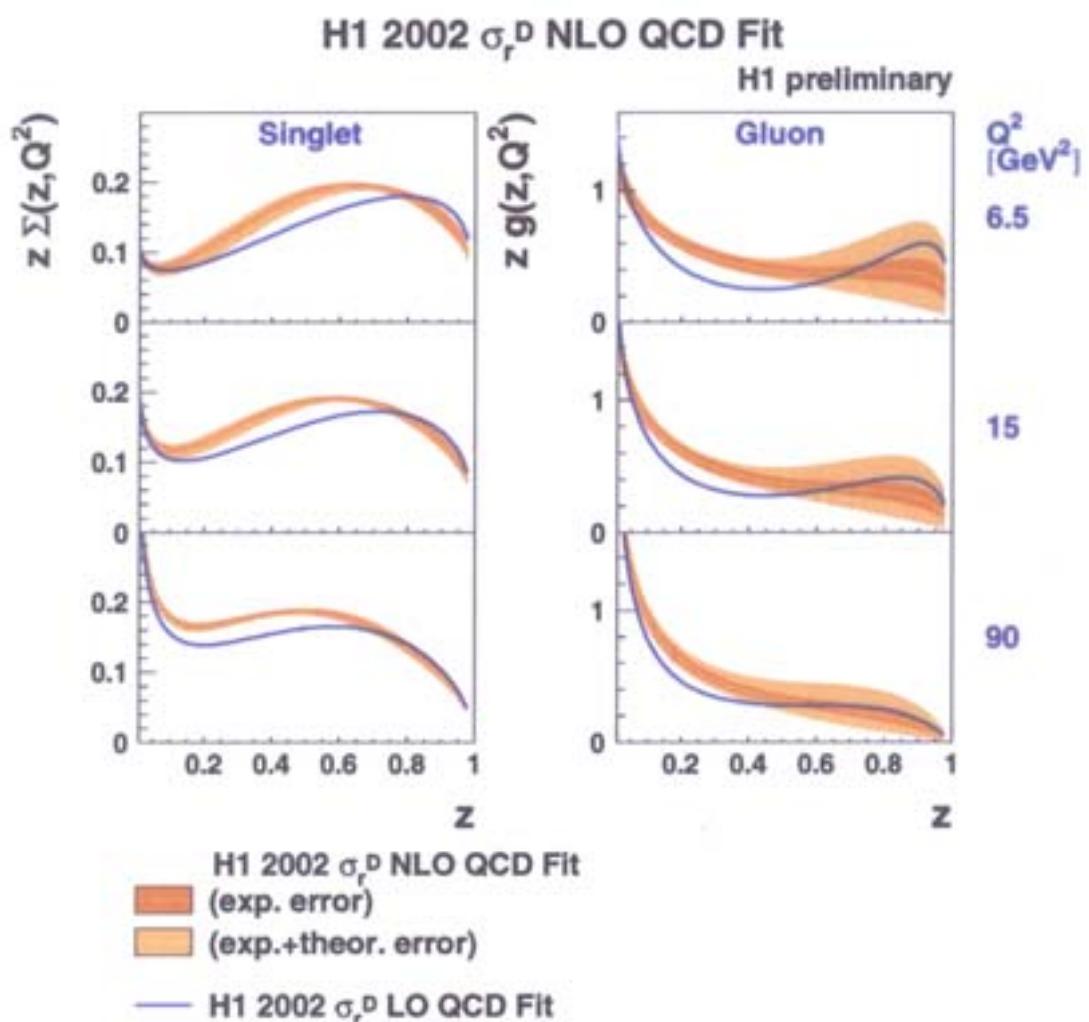
Interaction of small size component can be described in perturbation theory.

At large  $Q^2$  inclusive diffraction dissociation of a photon can be described in terms of quark distributions in the Pomerons.



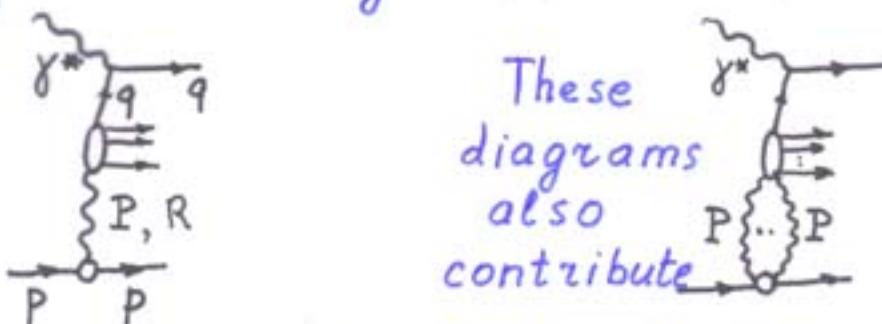
## QCD fits of $F_2^{D(3)}$ data

Extraction of the gluon and quark densities in the pomeron from a DGLAP fit to H1 data



- Structure of the Pomeron and hard diffraction in hadronic interactions.

From analysis of HERA diffractive data it is possible to find distributions of quarks and gluons in the "Pomeron."

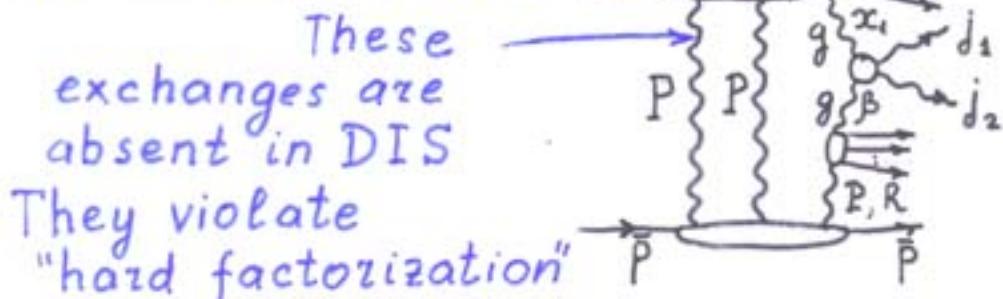


However standard QCD evolution takes place.

J. Collins

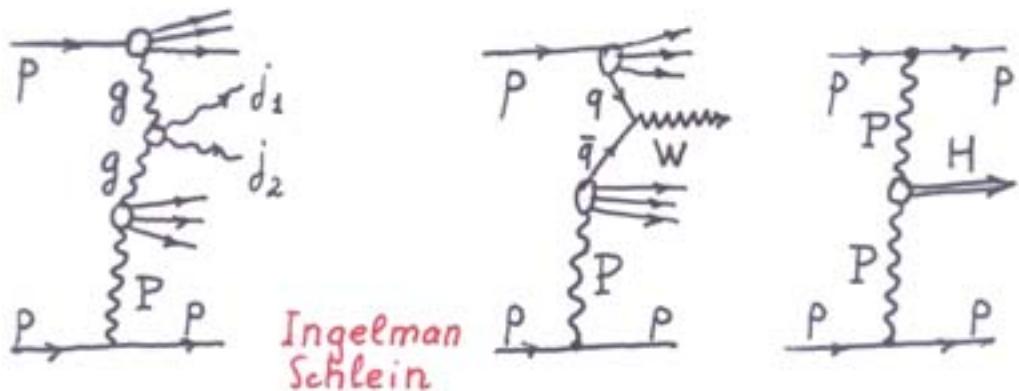
Large uncertainties in the gluonic content of the "Pomeron". New H1 analysis.

For hadronic interactions situation is more complicated

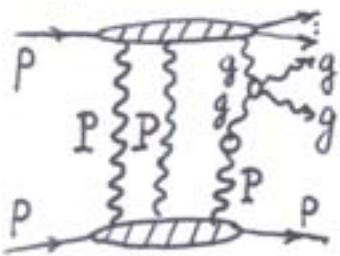


(1k)

- Hard diffraction in  $p\bar{p}$



- In these processes the rescattering effects are important



They strongly reduce U. Maor <sup>et.al</sup>  
cross sections. A. Bialas,  
R. Peschanski,  
Violation of both QCD  
(hard) and Regge factori-  
zation.

The suppression depends on energy and on  
the  $x$  of a parton (from the upper side) due  
to different sizes of initial configurations

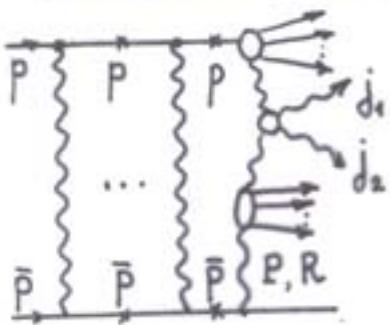
A.K, V.A. Khoze, A.D Martin, (2001)  
M.G. Ryskin

Interesting field for QCD physics at LHC.

Soft color interaction model gives a  
reasonable value for suppression  
(but not for  $\beta$ -dependence) R. Enberg

(12)

Usually these effects are taken into account in eikonal approximation (elastic rescatterings only)



The suppression factor  
(survival probability)

$$S^2 = \frac{\int |M(s, b, \dots)|^2 e^{-\Omega(b)} d^2 b}{\int |M(s, b, \dots)|^2 d^2 b}$$

However inelastic intermediate states can play an important role.

see also GLM

Eigen states with small absorption will lead to smaller suppression

Consider this effects in the 2-channel model KMR model (for details see )  
KMR.

Eigen states absorption cross sections differ strongly (3÷4 times)

In partonic model they correspond to configurations of different sizes

Large size - large  $\sigma$  - state 1

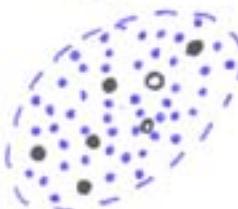
Small(er) size - smaller  $\sigma$  - state 2

(13)

Next step: relation to partonic configurations with different  $x$ . KKM R



Small size - mostly valence quarks  
 $x \sim 1$



Large size - mostly gluons and sea  
 $x \ll 1$

In this approach it is possible to explain  
diffractive production of jets at Tevatron  
CDF

Not only an absolute magnitude but  
also  $\beta$ -dependence differs from predic-  
tions, based on HERA data (Note  $\beta^{-1}$   
behaviour of CDF data for small  $\beta$ ) Fig.  
K. Goulianos

Kinematics:

$$\bar{\xi} = 0.06 \quad M^2 = \bar{\xi} \cdot S = 2 \cdot 10^5 \text{ GeV}^2$$

$$M_{jj}^2 = x_1 \beta M^2 \sim 10^3 \text{ GeV}^2$$

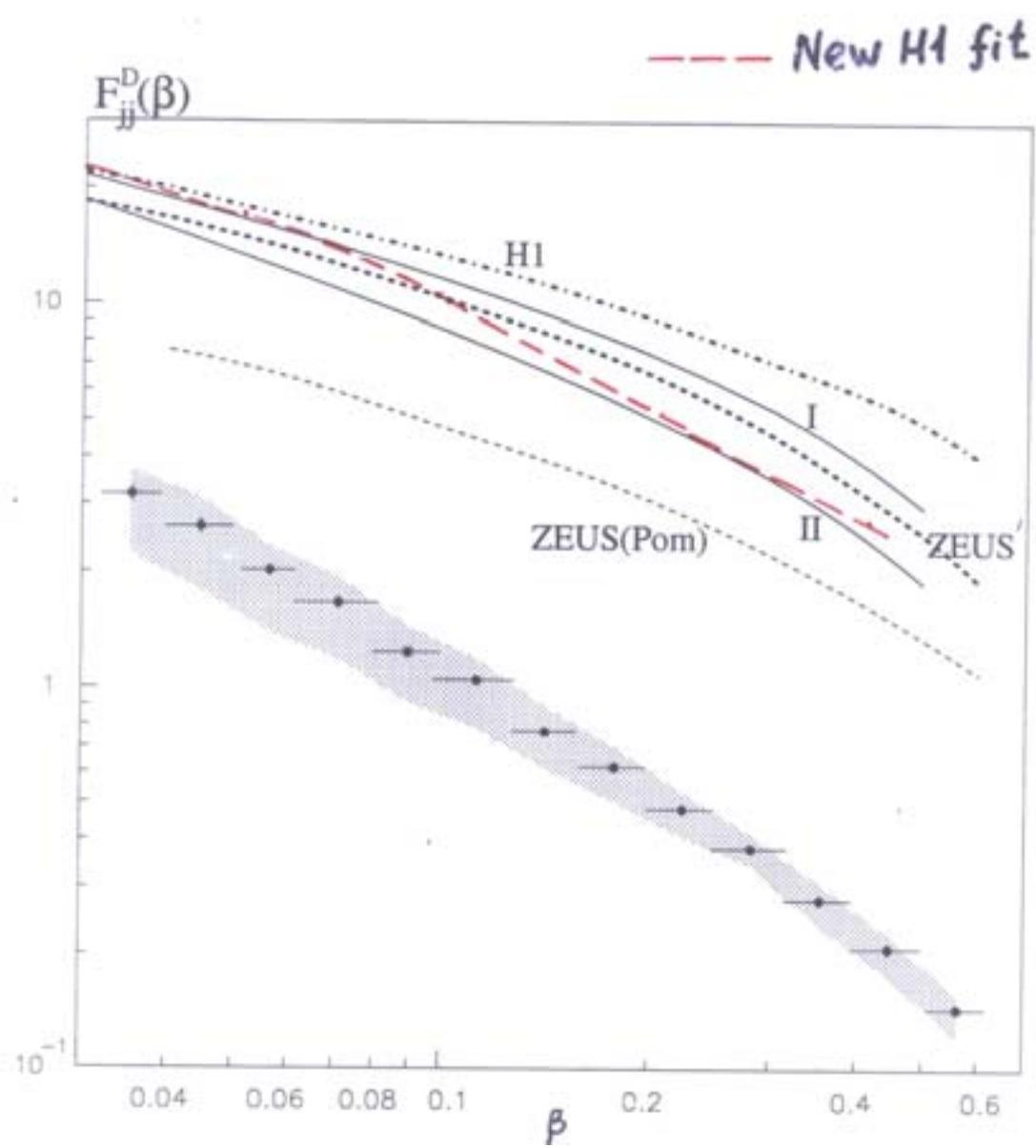
$$x_1 \cdot \beta \approx 5 \cdot 10^{-3}$$

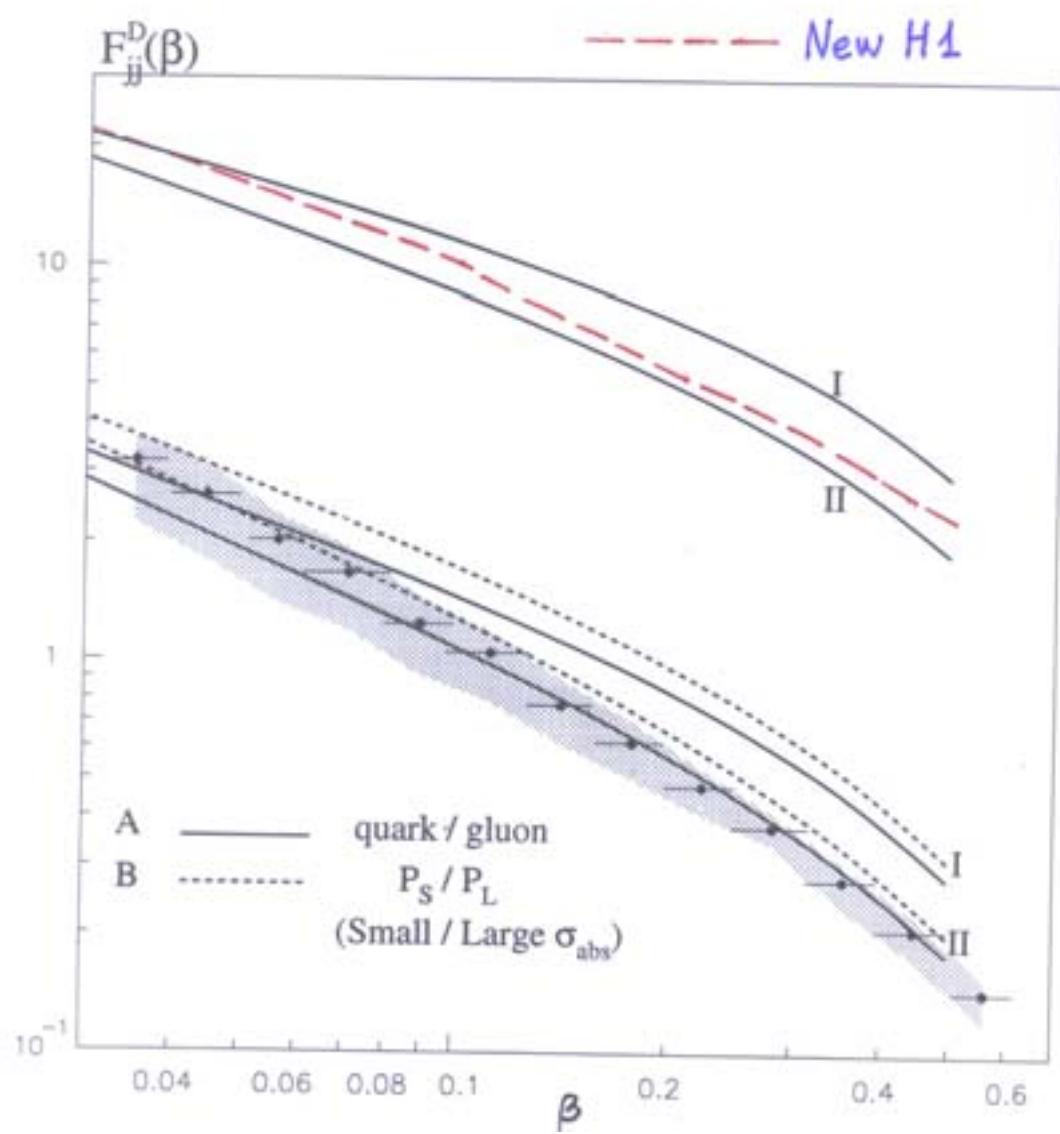
$\beta \geq 0.25 \rightarrow x_1 \lesssim 0.02$  mostly gluons

$\beta \sim 0.025 \rightarrow x_1 \sim 0.2$  mostly valence q

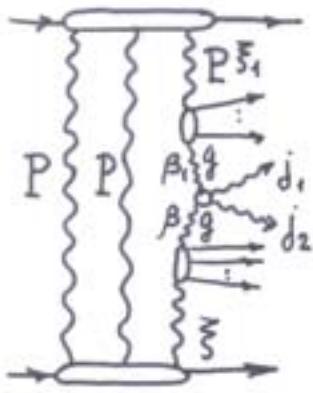
Thus in this model suppression factor  
increases as  $\beta$  decreases (for CDF kinemat.)

In this model it is possible to reproduce  
CDF results without free parameters. Fig.





- Double Pomerzon jet production



This process is observed at Tevatron

Test of factorization  
by CDF

$$R_1 = \frac{d\sigma_{SD}^{jj}}{d\sigma_{in}^{jj}} = \frac{F_P(\xi) \cdot f_p^g(\beta)}{x \cdot f_p^g(x)} |S_1|^2$$

$$R_2 = \frac{d\sigma_{DP}^{jj}}{d\sigma_{SD}^{jj}} = \frac{F_P(\xi_1) \cdot f_p^g(\beta_1)}{x_1 f_p^g(x_1)} \frac{|S_2|^2}{|S_1|^2}$$

$$x_1 = \xi_1 \cdot \beta_1$$

$$\frac{R_1}{R_2} = \frac{F_P(\xi) f_p^g(\beta) x_1 f_p^g(x_1) \cdot (|S_1|^2)^2}{F_P(\xi_1) f_p^g(\beta_1) x_1 f_p^g(x) \cdot |S_2|^2}$$

KKMR

(PL 2003)

If  $\xi = \xi_1$ ,  $\beta = \beta_1$  ( $x = x_1$ )

A. Bialas,  
R. Peschanski

$$R \equiv R_1 / R_2 = (|S_1|^2)^2 / |S_2|^2$$

For single Regge exchange ( $|S_i| = 1$ )

$$R = 1$$

With account of absorption

$$|S_1|^2 = 0.1, |S_2|^2 = 0.05$$

KMR

$$R = 0.2$$

$$R_{exp} = 0.19 \pm 0.07$$

## Conclusions

- Diffractive processes give an important information on different aspects of QCD.
- Pomeron in QCD has a very rich dynamical structure.
- Investigation of hard diffractive processes allows one to study breaking of both Regge and "hard" factorizations and transition from soft to hard regimes in QCD.
- Small- $x$  physics is related to QCD at high density. Shadowing effects are very important in this region.